

The Tourist Problem...

Given: A list of tourist, each with his/her list of places to visit. To do: Schedule bus rides for them so that each tourist visits all the places in his/her list.

Tourist	Places of Interest
Aaron	SZG, BG, JB
Betty	CG, JG, BG
Cathy	VC, SI, OR
David	JG, CG, OR
Evans	CG, JG, SZG
Frances	BG, SZG, JB
Gary	CG, OR
Harry	JG, CG

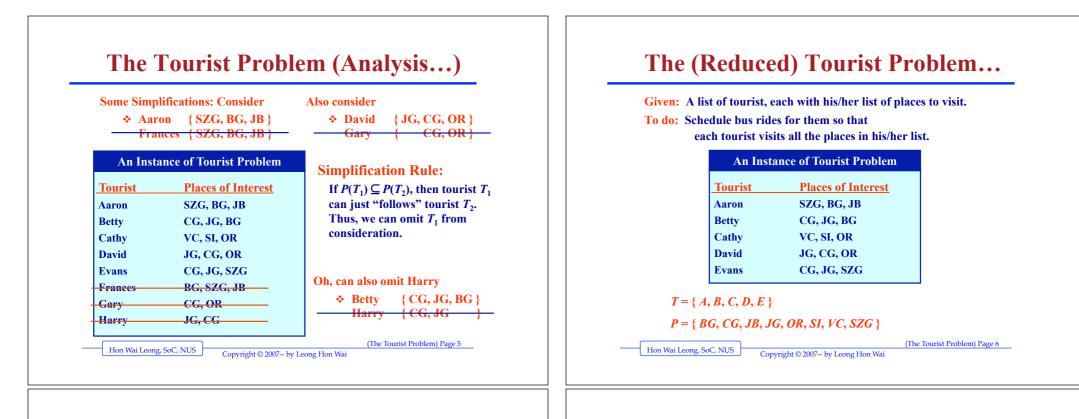
The Tourist Problem (Entities)

Good to know the entities we are dealing with...

- ***** The Tourists:
 - $T = \{A, B, C, D, E, F, G, H\}$
- * The Attractions (Places):
 P = { BG, CG, JB, JG, OR, SI, VC, SZG }

Places of Attraction			
Place	Common Name	Place	Common Name
BG	Botanical Gardens	CG	Chinese Gardens
JB	Jurong Birdpark	JG	Japanese Gardens
OR	Orchard Road	SI	Sentosa Island
SZG	Spore Zoological Gardens	VC	VivoCity

Hon Wai Leong, SoC, NUS



The Tourist Problem – v0

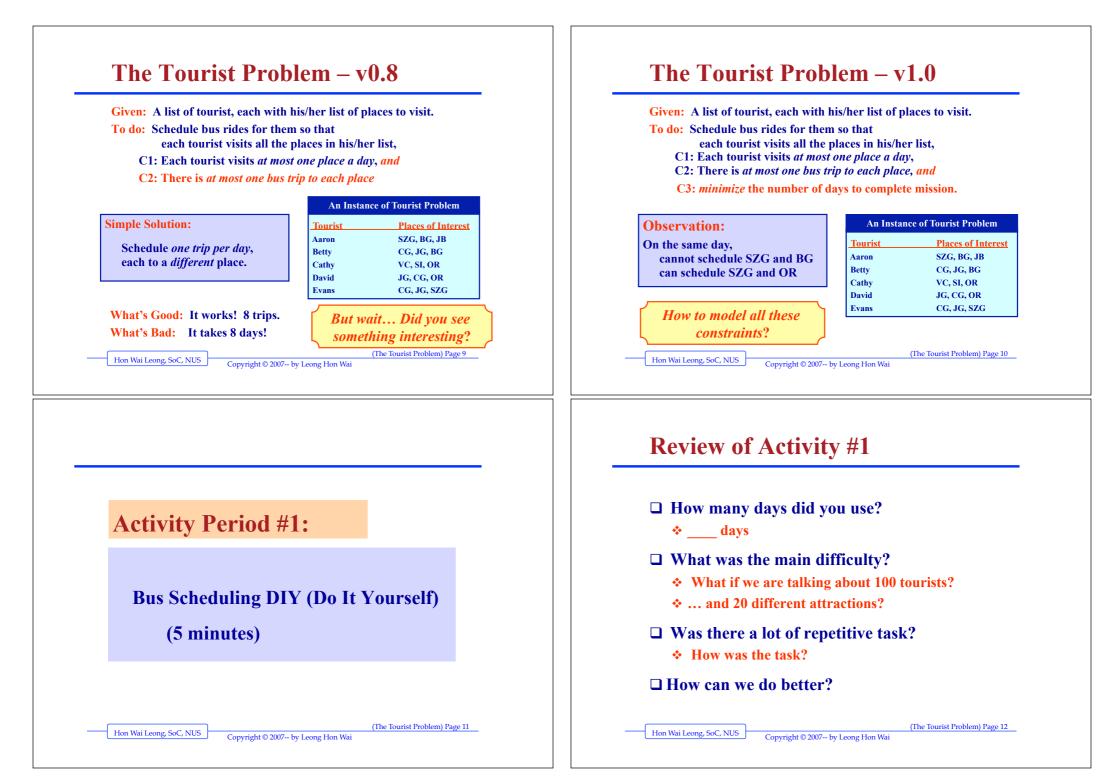
Given: A list of tourist, each with his/her list of places to visit. To do: Schedule bus rides for them so that each tourist visits all the places in his/her list.

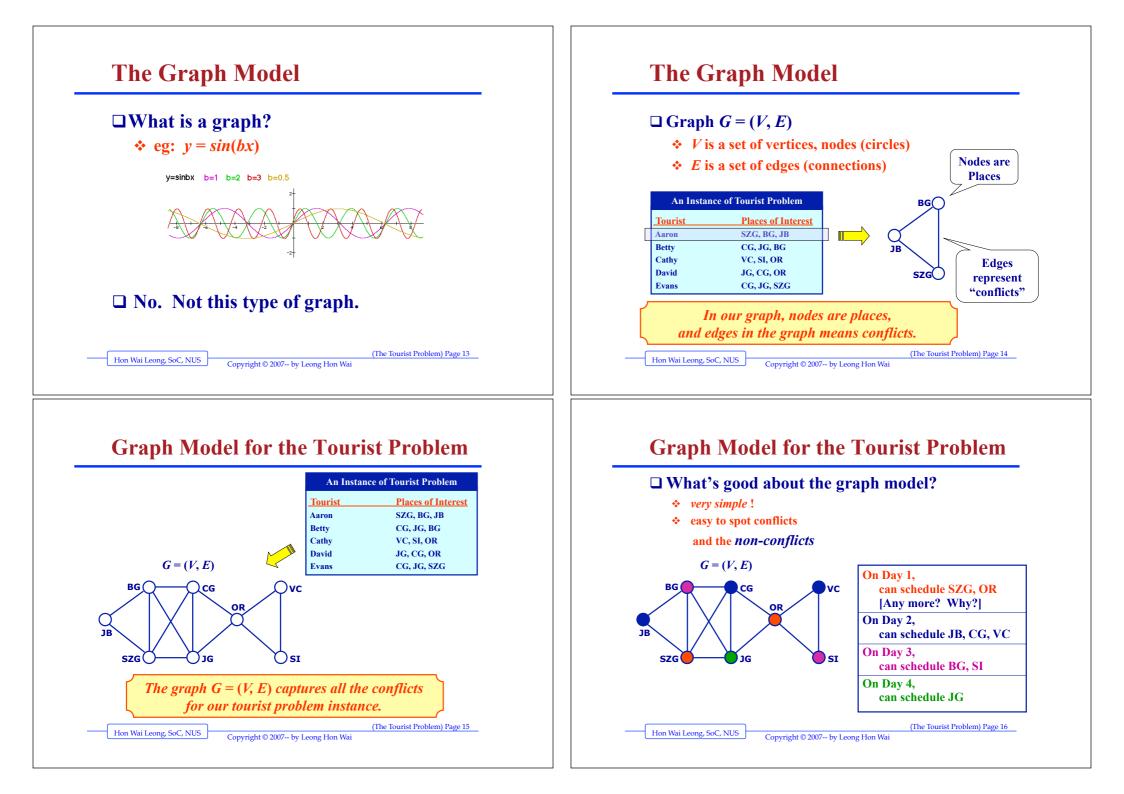
An Instance of Tourist Problem Solution: (Singapore 1-Day Tour) Tourist **Places of Interest** SZG, BG, JB Aaron Put all the tourists on one bus. Betty CG, JG, BG Visit all eight places in 1 day. Cathy VC, SI, OR David JG, CG, OR Evans CG, JG, SZG What's Good: It works! One bus, one-day. Not What's Bad: Too rushed. NO time to see anything! interesting! (The Tourist Problem) Page 7 Hon Wai Leong, SoC, NUS Copyright © 2007-- by Leong Hon Wai

The Tourist Problem – v0.5

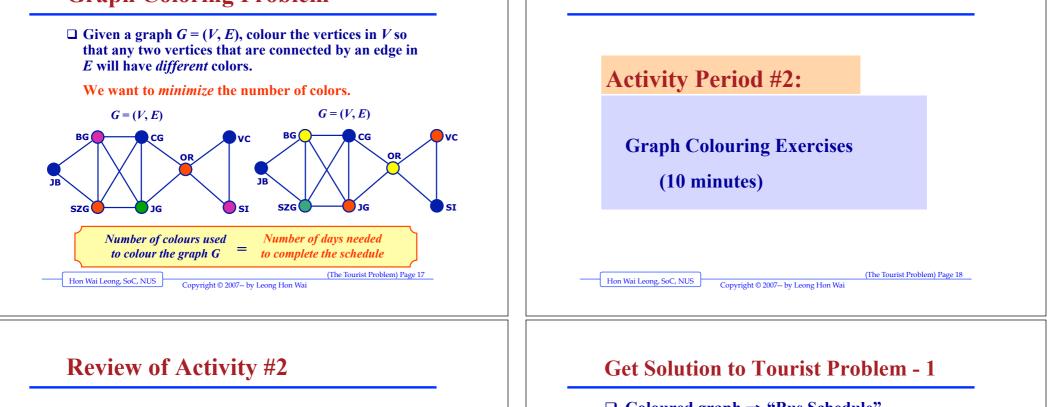
Given: A list of tourist, each with his/her list of places to visit. To do: Schedule bus rides for them so that each tourist visits all the places in his/her list, *and* C1: Each tourist visits *at most one place a day*.

	An Instar	An Instance of Tourist Problem	
Simple Solution: Schedule one trip to every place every day.	Tourist Aaron Betty Cathy David	Places of Interest SZG, BG, JB CG, JG, BG VC, SI, OR JG, CG, OR	
What's Good: It works! Finish in 3 What's Bad: Wasteful! 24 bus tr	•	CG, JG, SZG num!) Also, not interestin	
Hon Wai Leong, SoC, NUS Copyright © 2007 by	7 Leong Hon Wai	(The Tourist Problem) Page 8	



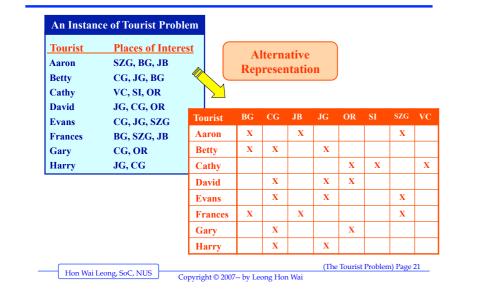


Graph Coloring Problem

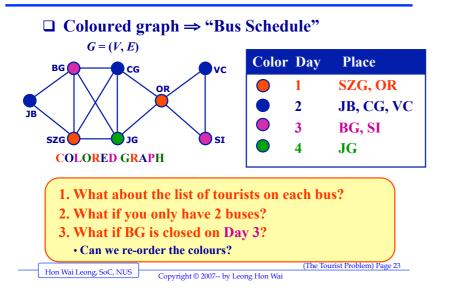


 \Box Coloured graph \Rightarrow "Bus Schedule" □ Is Graph Colouring fun? G = (V, E)Did you really used different colours? **Color Day** Place VC CG □ How many colours was did you use (Q1)? SZG, OR 1 OR 2 JB, CG, VC □ What about the *cycles* (Q2): JB 3 BG, SI * Q2(a): C_6 (a cycle of length 6)? SZG JG) SI **♦** Q2(b): C₅ (a cycle of length 5)? 4 JG **COLORED GRAPH** * What else can you say? □ What about the graph in Q3? 1. What about the list of tourists on each bus? Can we get it from the graph model? □ What about Q4? NO. Why NOT. ***** Why (The Tourist Problem) Page 20 (The Tourist Problem) Page 19 Hon Wai Leong, SoC, NUS Hon Wai Leong, SoC, NUS Copyright © 2007-- by Leong Hon Wai Copyright © 2007-- by Leong Hon Wai

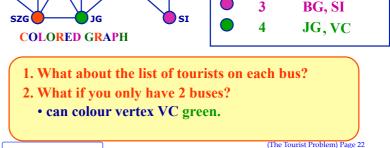
The Tourist Problem...



Get Solutions to Tourist Problem (3)



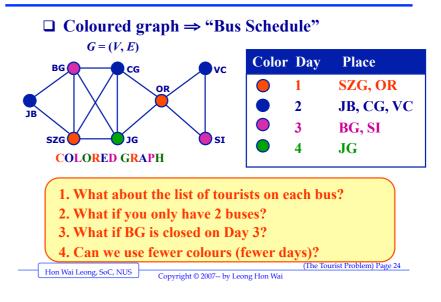
Get Solutions to Tourist Problem (2) \Box Coloured graph \Rightarrow "Bus Schedule" G = (V, E)**Color Day** Place BG CG VC SZG. OR 1 OR 2 JB, CG, VC JB 3 BG, SI

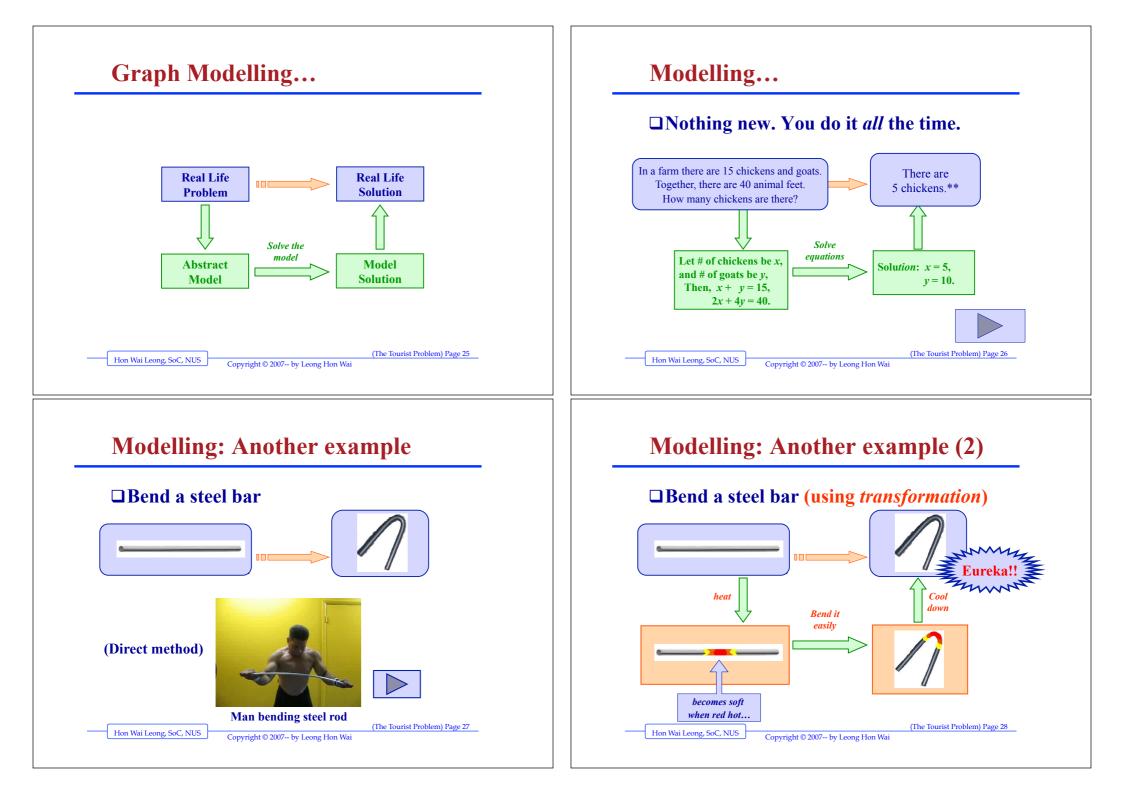


Get Solutions to Tourist Problem (3)

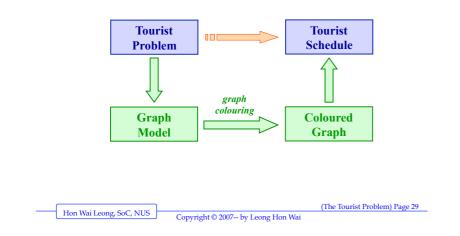
Copyright © 2007-- by Leong Hon Wai

Hon Wai Leong, SoC, NUS





Tourist Problem & Graph Colouring



Moral of the Story

The Tourist Problem:

- ***** Some problems are **EASY**. (*don't* complicate them)
- Get a simple solution first.
 then analyze it, improve it, refine it.
- * Solution depend on the questions asked
- * It is important to ask questions.
- * Theoretical modeling and analysis are beneficial

□ Modeling

Hon Wai Leong, SoC, NUS

- * Abstract modeling *simplifies* problem and solution!
- * Abstract model is *transferable*.
- * Models don't answer everything.

(The Tourist Problem) Page 31 Copyright © 2007-- by Leong Hon Wai

Modelling in Tourist Problem

Recap: Our Graph modelling...

Graph Model	Tourist Problem		
Nodes	places		
Edges / Conflicts	tourist want to visit both places		
Colors	bus trips to places		
Others	The tourists		

Hon Wai Leong, SoC, NUS Copyright © 2007-- by Leong Hon Wai

Graph Colouring & Applications

□ Where *else* is Graph Colouring used?

- The Tourist Problem [done]
- * Map Colouring
- * Fish in a Tank
- * Frequency assignment in wireless networks
- * Time Table Scheduling
- * And a whole lot more...

Experience the fun of problem solving

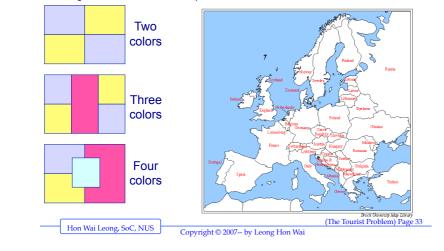
Hon Wai Leong, SoC, NUS

(The Tourist Problem) Page 32 Copyright © 2007-- by Leong Hon Wai

(The Tourist Problem) Page 30

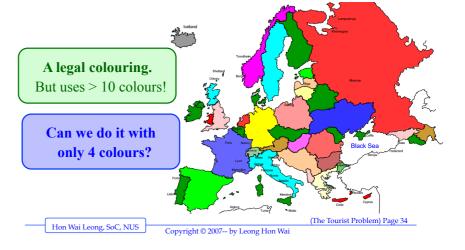
The Map Coloring Problem

We want to color countries, oceans, lakes, and islands on a map so that no two adjacent areas have the same color.

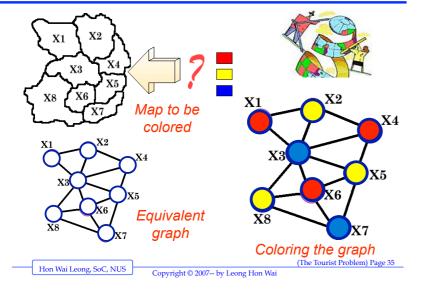


The Map Coloring Problem

We want to color countries, oceans, lakes, and islands on a map so that no two adjacent areas have the same color.



Map and Graph Coloring



The Four Color Conjecture

Question:

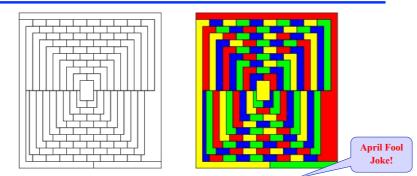
Hon Wai Leong, SoC, NUS

Can *all* map be coloured using only four colours?

Copyright © 2007-- by Leong Hon Wai

(The Tourist Problem) Page 36

Does four colour suffices?



Martin Gardner published in Scientific American (*April* 1975) this map of 110 regions. He claimed that the map *requires five colors* and constitutes a counterexample to the four-color theorem.

However, the coloring of Wagon, obtained algorithmically using <u>Mathematica</u>, clearly shows that this map is, in fact, four-colorable.

Source: http://mathworld.wolfram.com/Four-ColorTheorem.html

Hon Wai Leong, SoC, NUS

Copyright © 2007-- by Leong Hon Wai

(The Tourist Problem) Page 37

150 years of history...

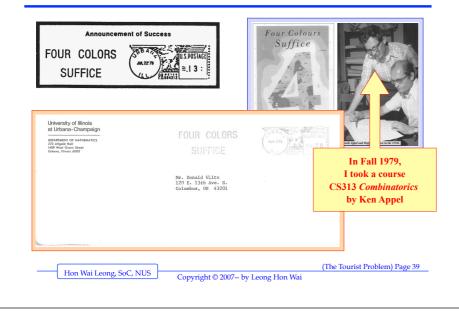
- □ 1852 Conjecture (*Guthrie* → *DeMorgan*)
- □ 1878 Publication (*Cayley*)
- □ 1879 First proof (Kempe)
- □ 1880 Second proof (*Tait*)
- □ 1890 Rebuttal (*Heawood*)
- □ 1891 Second rebuttal (Petersen)
- □ 1913 Reducibility, connexity (Birkhoff)
- □ 1922 Up to 25 regions (Franklin)
- **1969** Discharging (*Heesch*)
- **1976 Four Color Thm (Appel & Haken) @UIUC**
- □ 1995 Streamlining (*Robertson & al.*)
- **2005 COQ proof (***Gonthier***)**

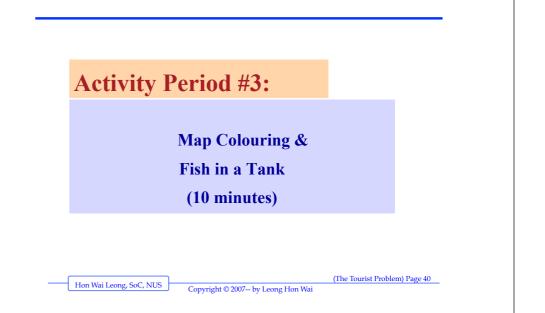


Hon Wai Leong, SoC, NUS

(The Tourist Problem) Page 38 Copyright © 2007-- by Leong Hon Wai

Four Color Theorem Proof @ UIUC



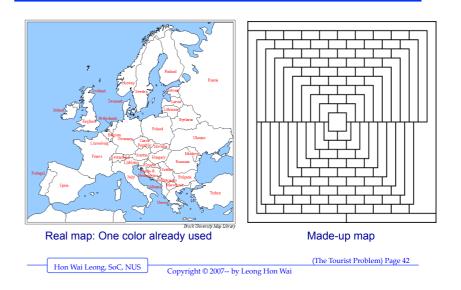


Review of Hands-on Activity #3

- How many colours did the map need?
 You should never need more than 4 colours
- Did you know about the "Four-Colour Theorem"?
- □ How many fish tanks did you need?

Activity 4: Color These Maps

Use as few colors as possible



Summary of Problem Modelling

Copyright © 2007-- by Leong Hon Wai

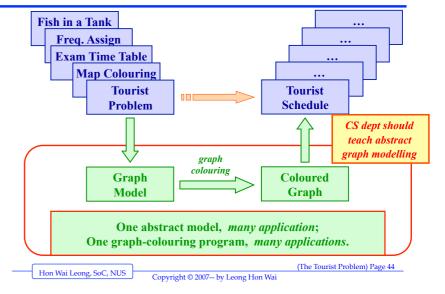
(The Tourist Problem) Page 41

(The Tourist Problem) Page 43

	Tourist Problem	Fish in a tank	Frequency Assignment	Map Coloring
Nodes	places	fishes	radio stations	Countries
Edges / Conflicts	tourist want to visit both places	cannot be placed in same tank	interference if placed too near	share a common border
Colors	bus trips to places	fish tanks	signal frequencies	color
Others	The tourists			

Copyright © 2007-- by Leong Hon Wai

Why CS dept teach abstract problems?



Hon Wai Leong, SoC, NUS

Hon Wai Leong, SoC, NUS

References...

On Graph Coloring and Applications:

- 1. http://www.geom.uiuc.edu/~zarembe/graph3.html
- 2. <u>http://www.colorado.edu/education/DMP/activities/graph/ddghnd03.html</u>
- 3. Lots of other links available

On the Four Color Theorem:

- 1. http://en.wikipedia.org/wiki/Four_color_theorem
- 2. http://www.maa.org/reviews/fourcolors.html
- 3. http://www.math.gatech.edu/~thomas/FC/fourcolor.html
- 4. http://www.mathpages.com/home/kmath266/kmath266.htm

Hon Wai Leong, SoC, NUS

(The Tourist Problem) Page 45 Copyright © 2007-- by Leong Hon Wai

End of Talk on

Tourist Problem!

If you want to contact me,

go email, MSN, FB at leonghw@comp.nus.edu.sg



School of Computing

Copyright © 2007-- by Leong Hon Wai

Hon Wai Leong, SoC, NUS

(The Tourist Problem) Page 46