

## Software Validation CS 4271 Lecture 11, 12

Abhik Roychoudhury  
National University of Singapore

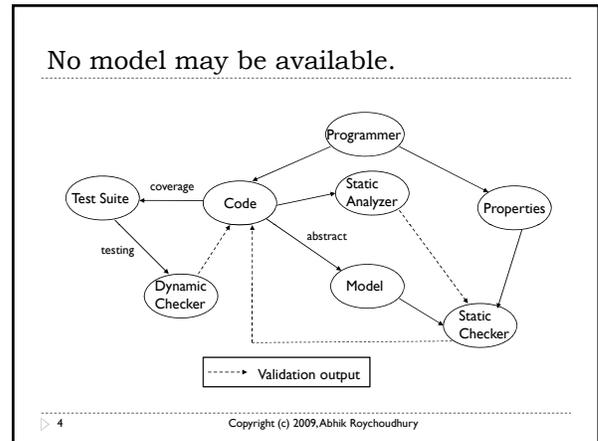
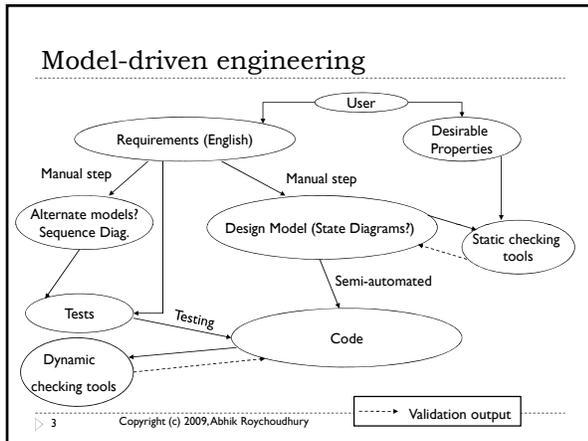
<http://www.comp.nus.edu.sg/~abhik/>

Copyright 2009 by Abhik Roychoudhury

### Software construction

- ▶ From a design model
  - ▶ In safety-critical domains – automotive, avionics.
  - ▶ D0 I78C – software in airborne systems.
- ▶ Or, hand-constructed
  - ▶ Usual practice – audio, video and other domains.
  - ▶ UML models only for guidance.

Copyright (c) 2009, Abhik Roychoudhury



### Programming

Creativity

+

Precision

CSS219 2010-11 by Abhik

### The art of debugging

"A **software bug** (or just "bug") is an error, flaw, mistake, ... in a computer program that prevents it from behaving as intended (e.g., producing an **incorrect result**). ... Reports detailing bugs in a program are commonly known as **bug reports**, fault reports, ... change requests, and so forth."  
--- Wikipedia

Copyright (c) 2009, Abhik Roychoudhury

### Tools?




We should automatically produce the bug report via analysis of program and/or execution trace

Bug report is a small fragment of the program.

7

### Organization

- ▶ Dynamic checking of programs
  - ▶ Dynamic slicing
  - ▶ Hierarchical slicing
  - ▶ Fault Localization
  - ▶ Directed testing
- ▶ Static checking of programs – Not covered.
  - ▶ Predicate abstraction
  - ▶ Abstraction refinement

8

Copyright (c) 2009, Abhik Roychoudhury

### What is dynamic checking?

- ▶ Check program executions, not source code.
- ▶ How to generate program executions?
  - ▶ Testing (coverage based)
  - ▶ Testing (specification based)
- ▶ How to check program executions
  - ▶ Data and control dependencies (slicing)
  - ▶ By comparing against other program executions (fault localization).

9

Copyright (c) 2009, Abhik Roychoudhury

### SW Debugging: Social aspects



Software-controlled devices are ubiquitous --- automotive control, avionics control and consumer electronics

Many of these software are safety-critical

⇒ should be validated extensively.

10

Copyright (c) 2009, Abhik Roychoudhury

### SW Debugging: Economics

- ▶ How often do bugs appear ?
- ▶ How many of them are critical?
- ▶ How much money does a company gain by using sophisticated debugging tools?
- ▶ Could it be avoided simply by sparing one more programmer?

11

Copyright (c) 2009, Abhik Roychoudhury

### SW Debugging: Economics

- SW project with 5 million LOC (note: Windows Vista is 50 million LOC !!)
- Assume linear scaling up of errors
  - Actually could be more errors --- we make more mistakes as the SW grows long and arduous.
- 1 hr to fix each major error
  - Actually much more
  - \$40K salary per year

$$13 * \frac{5000000}{1000} = 65,000 \text{ bugs}$$

$$\frac{65,000}{44} \text{ weeks} = 1477 \text{ weeks} = \frac{1477}{50} \approx 30 \text{ years} = \$1.2 \text{ M}$$

12

Copyright (c) 2009, Abhik Roychoudhury

### SW Debugging: tools

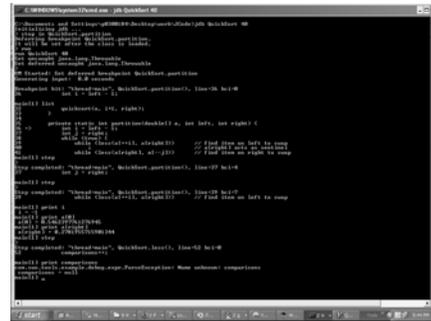
*“Even today, debugging remains very much of an art. Much of the computer science community has largely ignored the debugging problem..... over 50 percent of the problems resulted from the time and space chasm between symptom and root cause or inadequate debugging tools.” (Hailpern & Santhanam, IBM Sys Jnl, 41 (1), 2002)*

- > Need methods and tools to trace back to the root cause of bug from the manifested error
- > What about the current tools?

13

Copyright (c) 2009, Abhik Roychoudhury

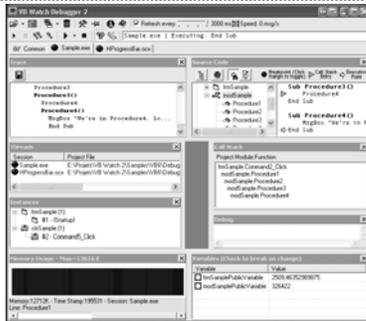
### jdb on windows XP



14

Copyright (c) 2009, Abhik Roychoudhury

### VB watch debugger



15

Copyright (c) 2009, Abhik Roychoudhury

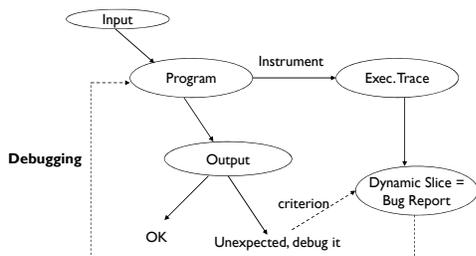
### So, what did we see?

- ▶ Command line tool for Java
  - ▶ User can set breakpoints, and
  - ▶ Replay an execution, and
  - ▶ Watch it at the breakpoints.
- ▶ Lack of GUI is not the issue here.
  - ▶ Can easily collect and visualize more program info.
- ▶ Lack of automation is the problem!
  - ▶ Need automated trace analysis.

16

Copyright (c) 2009, Abhik Roychoudhury

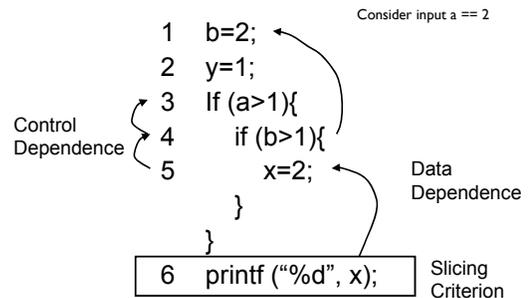
### Dynamic Slicing for Debugging



17

Copyright (c) 2009, Abhik Roychoudhury

### Dynamic Slicing



18

CS5219 2010-11 by Abhik

### Dynamic Slice

- ▶ Set slicing criterion
  - ▶ (Variable  $v$  at first instance of line 70)
  - ▶ The value of variable  $v$  at first instance of line 70 is unexpected.
- ▶ Dynamic slice
  - ▶ Closure of
    - ▶ Data dependencies &
    - ▶ Control dependencies
  - ▶ from the slicing criterion.

▶ 19 Copyright (c) 2009, Abhik Roychoudhury

### Dynamic data dependencies

$V := I;$   
...  
 $U := V$

An edge from a variable usage to the latest definition of the variable.

$A[i] := I;$   
...  
 $U := A[i]$

→ Do we consider this data dependence edge?  
→ Remember that the slicing is for an input, so the addresses are resolved  
→ We thus define data dependencies corresponding to memory locations rather than variable names.

▶ 20 Copyright (c) 2009, Abhik Roychoudhury

### Static Control dependencies

**Post-dominated:**  $I, J$  – nodes in Control Flow Graph  
 $I$  is post-dominated by  $J$  iff all paths from  $I$  to EXIT pass through  $J$

YES

NO

▶ 21 Copyright (c) 2009, Abhik Roychoudhury

### Static control dependencies

$I$  not post-dom by  $J$   
 $U, V$  post-dom by  $J$   
 Control dependence  $I \rightarrow J$

▶ 22 Copyright (c) 2009, Abhik Roychoudhury

### Dynamic control dependencies

- ▶  $X$  is dynamically control dependent on  $Y$  if
  - ▶  $Y$  occurs before  $X$  in the execution trace
  - ▶  $X$ 's stmt. is statically control dependent on  $Y$ 's stmt.
  - ▶ No statement  $Z$  between  $Y$  and  $X$  is such that  $X$ 's stmt. is statically control dependent on  $Z$ 's stmt.
- ▶ Captures the intuition:
  - ▶ What is the nearest conditional branch statement that allows  $X$  to be executed, in the execution trace under consideration.

▶ 23 Copyright (c) 2009, Abhik Roychoudhury

### Dynamic Slice

```

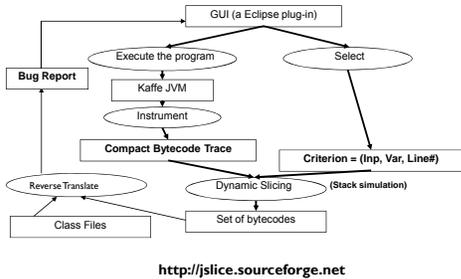
1. void setRunningVersion(boolean runningVersion)
2.   if( runningVersion ) {
3.     savedValue = value;
4.   } else{
5.     savedValue = "";
6.   }
7.   this.runningVersion = runningVersion;
8.   System.out.println(savedValue);

```

Slicing Criterion

▶ 24 Copyright (c) 2009, Abhik Roychoudhury

### Jslice: a dynamic slicing tool



<http://jslice.sourceforge.net>

25

Copyright (c) 2009, Abhik Roychoudhury

### Issues for such a slicing tool

- ▶ Online trace compression – beyond conventional string compression.
- ▶ Full trace is never stored.
- ▶ Program dependence analysis on compressed trace – no decompression.
- ▶ Analysis at low-level (byte-code) to support third-party software.
- ▶ Managing stack architecture.

26

Copyright (c) 2009, Abhik Roychoudhury

### Organization

- ▶ Dynamic checking of programs
  - ▶ Dynamic slicing
  - ▶ Hierarchical slicing
  - ▶ Fault Localization
  - ▶ Directed testing
- ▶ Static checking of programs
  - ▶ Predicate abstraction
  - ▶ Abstraction refinement

27

Copyright (c) 2009, Abhik Roychoudhury

### Problem with dynamic slicing

- ▶ Huge overheads
  - ▶ Backwards slicing requires trace storage.
  - ▶ Jslice tool for Java
    - ▶ Online trace compression & traversal
    - ▶ <http://jslice.sourceforge.net>
- ▶ Dynamic Slice is still too large ...
  - ▶ ... for human comprehension
  - ▶ Now

28

Copyright (c) 2009, Abhik Roychoudhury

### An example

```

1 public static void main(String[] args) {
    .....
2.  init( db );
3.  operate( db );
4.  output ( db );
5.  return;
}
    
```

*SPECJVM  
DB program*

```

init( .. db ) {
  db= ..
  ....
}
    
```

```

operate ( ... db ) {
  db =..
  ...
}
    
```

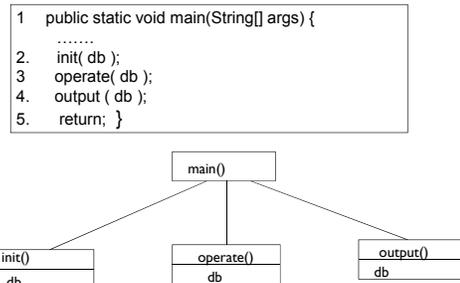
```

output( db ) {
  .....
  print(db...);
}
    
```

29

Copyright (c) 2009, Abhik Roychoudhury

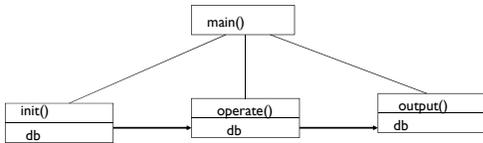
### Divide trace into phases



30

Copyright (c) 2009, Abhik Roychoudhury

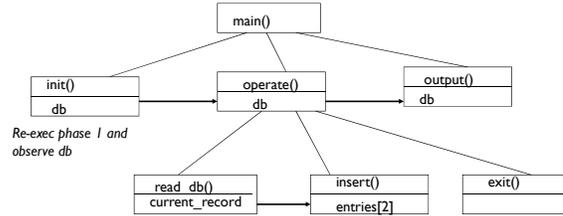
### Report inter-phase dependencies



Intra-phase control and data dependencies are suppressed.  
Inter-phase dep. form input-output relationships.

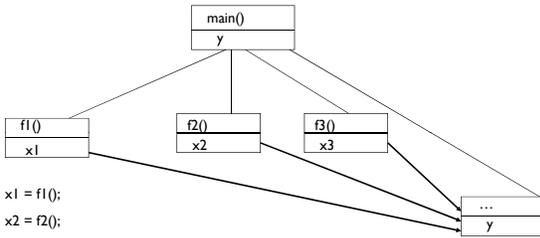
### Programmer zooms into ...

... one phase by inspecting the phase outputs  
-> (may/may not involve re-executing program)



Re-exec phase 1 and observe db

### Parallel Dependence Chains



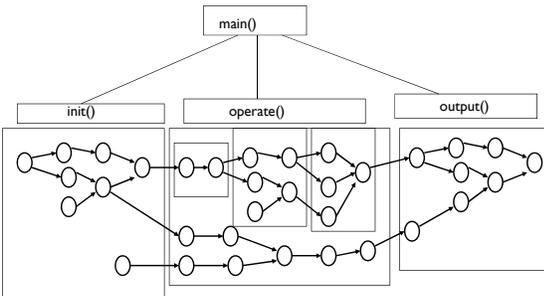
```

x1 = f1();
x2 = f2();
x3 = f3();
y = x1 + x2 + x3;
print y - Criterion
  
```

### Hierarchical dynamic slicing

- ▶ Compute "phases" of an exec. trace
  - ▶ Control structure boundaries
- ▶ Augment dynamic slicing algorithm
  - ▶ Mark inter-phase dependencies
  - ▶ Compute only reachable nodes from selected inter-phase dependency.
- ▶ Programmer intervention
  - ▶ Select the first suspicious inter-phase dep.
  - ▶ Comprehension guides computation.

### In action ...



### Beyond Dynamic Slices

- ▶ If dynamic slice computation and traversal becomes manageable
  - ▶ We can look beyond dynamic slices.
  - ▶ We can look at errors which are not captured in dynamic slices.

### Static vs Dynamic Slicing

- ▶ Static Slicing
  - ▶ source code
  - ▶ statement
  - ▶ static dependence
- ▶ Dynamic Slicing
  - ▶ a particular execution
  - ▶ statement instance
  - ▶ dynamic dependence

### Static vs Dynamic Slicing

```

1  b=1;
2  if (a>1)
3    x=1;
4  else
5    x=2;
6  printf ("%d", x);
    
```

Slicing Criterion

### Static vs Dynamic Slicing

```

1  p.f = 1;
2  x= q.f;
3  printf ("%d", x);
    
```

p and q point to the same object?

Slicing Criterion

▶ Static points-to analysis is always conservative

### Relevant Slicing

```

1  b=10;
2  x=1;
3  if (a>1){
4    if (b>1){
5      x=2;
6    }
7  }
8  printf ("%d", x);
    
```

### Relevant Slicing

```

1  b=1;
2  x=1;
3  if (a>1){
4    if (b>1){
5      x=2;
6    }
7  }
8  printf ("%d", x);
    
```

### Relevant Slicing

input: a=2

```

1  b=1;
2  x=1;
3  if (a>1){
4    if (b>1){
5      x=2;
6    }
7  }
8  printf ("%d", x);
    
```

Source of Failure →

Dynamic Slice →

Execution is omitted →

### Potential Dependence

```

1  b=1;      input: a=2
2  x=1;
3  if (a>1){
4      if (b>1){
5          x=2;
6      }
7  }
8  printf ("%d", x);
    
```

### Relevant Slice

```

1  b=1;      input: a=2
2  x=1;
3  if (a>1){
4      if (b>1){
5          x=2;
6      }
7  }
8  printf ("%d", x);
    
```

### Program Slice

Static	Dynamic	Relevant	Code
1		1	1 b=1; input: a=2
2	2	2	2 x=1;
3			3 if (a>1){
4		4	4 if (b>1){
5		5	5 x=2;
			6 }
6	6	6	6 printf ("%d", x);

### Organization

- ▶ Dynamic checking of programs
  - ▶ Dynamic slicing
  - ▶ Hierarchical slicing
  - ▶ Fault Localization
  - ▶ Directed testing
- ▶ Static checking of programs
  - ▶ Predicate abstraction
  - ▶ Abstraction refinement

46 Copyright (c) 2009, Abhik Roychoudhury

### More on debugging

- ▶ Dynamic slicing analyzes the problematic execution trace.
  - ▶ Problematic: output is unexpected
  - ▶ OK: output is as expected.
- ▶ Alternatively:
  - ▶ We could compare a given problematic trace with an OK trace to localize the source of error.

47 Copyright (c) 2009, Abhik Roychoudhury

### Fault Localization: overview

```

graph TD
    FR([Failing Run]) --> CE[Compare Execution]
    SR([Successful Run]) --> CE
    CE --> D([Difference])
    D --> Dev[Developer]
    D --- BR[As bug report]
    
```

48 Copyright (c) 2009, Abhik Roychoudhury

### Comparing executions

```

1. m=...
2. if (m >= 0) {
3.   ...
4.   lastm = m;
5. }
6. ....
    
```

should be  
if ((m >= 0) && (lastm!=m))

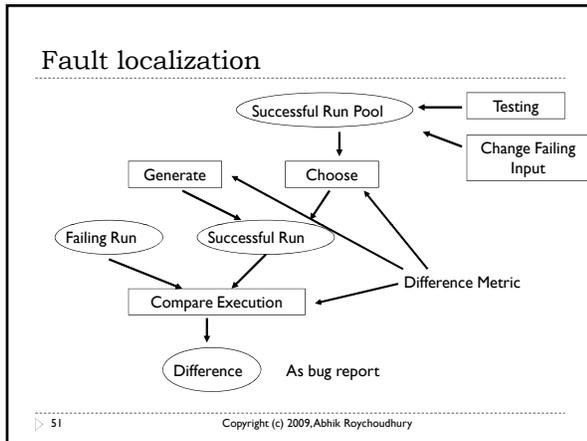
49 Copyright (c) 2009, Abhik Roychoudhury

### Comparing executions

1. m=...	1. m=...
2. if (m >= 0) {	2. if (m >= 0) {
3.   ...	3.   ...
4.   lastm = m;	4.   lastm = m;
5. }	5. }
6. ....	6. ....

*Failing run*                      *Successful run*

50 Copyright (c) 2009, Abhik Roychoudhury



### Example program

*Program*

```

1. if (a)
2.   i = i + 1;
3. if (b)
4.   j = j + 1;
5. if (c)
6.   if (d)
7.     k = k + 1;
8.   else
9.     k = k + 2;
10. printf("%d", k);
    
```

52 Copyright (c) 2009, Abhik Roychoudhury

### Comparing executions

1. <b>if (a)</b>	1. <b>if (a)</b>
2. i = i + 1;	2. i = i + 1;
3. <b>if (b)</b>	3. <b>if (b)</b>
4. j = j + 1;	4. j = j + 1;
5. <b>if (c)</b>	5. <b>if (c)</b>
6. <b>if (d)</b>	6. <b>if (d)</b>
7. k = k + 1;	7. k = k + 1;
8. else	8. else
9. k = k + 2;	9. k = k + 2;
10. printf("%d", k);	10. printf("%d", k);

**Execution run  $\pi$**                       **Execution run  $\pi I$**

53 Copyright (c) 2009, Abhik Roychoudhury

### Set of statements

- ▶ S = Set of statements executed in  $\pi$ 
  - ▶ {1,3,5,6,7,10}
- ▶ S<sub>I</sub> = Set of statements executed in  $\pi I$ 
  - ▶ {1,3,4,5,6,9,10}
- ▶ If  $\pi$  is faulty and  $\pi I$  is OK
  - ▶ Bug report = S - S<sub>I</sub> = {4,7}
- ▶ Choice of the execution run to compare with is very important.

54 Copyright (c) 2009, Abhik Roychoudhury

### Another difference metric

Failing Run      Successful Runs

- Number of Branches
- Location of Branches

55 Copyright (c) 2009, Abhik Roychoudhury

### Difference b/w traces shown

<ol style="list-style-type: none"> <li>1. if (a)</li> <li>2.    i = i + 1;</li> <li>3. if (b)</li> <li>4.    j = j + 1;</li> <li>5. if (c)</li> <li>6.    if (d)</li> <li>7.        k = k + 1;</li> <li>8.        else</li> <li>9.        k = k + 2;</li> <li>10. printf("%d", k);</li> </ol>	<ol style="list-style-type: none"> <li>1. if (a)</li> <li>2.    i = i + 1;</li> <li>3. if (b)</li> <li>4.    j = j + 1;</li> <li>5. if (c)</li> <li>6.    if (d)</li> <li>7.        k = k + 1;</li> <li>8.        else</li> <li>9.        k = k + 2;</li> <li>10. printf("%d", k);</li> </ol>
---	---

56 Copyright (c) 2009, Abhik Roychoudhury

### Trace alignment and differences

Execution Run			Alignment		Difference	
$\pi$	$\pi'$	$\pi''$	$\pi$	$\pi'$	$diff(\pi, \pi')$	$diff(\pi', \pi'')$
1 <sup>1</sup>	1 <sup>1</sup>	1 <sup>1</sup>				
2 <sup>2</sup>	2 <sup>2</sup>	2 <sup>2</sup>				
3 <sup>3</sup>	3 <sup>3</sup>	3 <sup>3</sup>				
4 <sup>4</sup>	3 <sup>3</sup>	4 <sup>4</sup>			•	
5 <sup>5</sup>	4 <sup>4</sup>	5 <sup>5</sup>				
7 <sup>6</sup>	7 <sup>4</sup>	7 <sup>6</sup>				•
8 <sup>7</sup>	8 <sup>5</sup>					
9 <sup>8</sup>	9 <sup>6</sup>					
		12 <sup>7</sup>				
1 <sup>9</sup>	1 <sup>7</sup>	1 <sup>8</sup>				
2 <sup>10</sup>	2 <sup>8</sup>	2 <sup>9</sup>				
3 <sup>11</sup>	3 <sup>9</sup>	3 <sup>10</sup>				
4 <sup>12</sup>	4 <sup>10</sup>	4 <sup>11</sup>				
5 <sup>13</sup>	5 <sup>11</sup>	5 <sup>12</sup>			•	•
7 <sup>14</sup>	7 <sup>12</sup>	7 <sup>13</sup>				
8 <sup>15</sup>						
9 <sup>16</sup>						
		12 <sup>13</sup>				
		14 <sup>14</sup>				
		14 <sup>15</sup>				

57 Copyright (c) 2009, Abhik Roychoudhury

### Compare Corresponding Statement Instances

<ol style="list-style-type: none"> <li>1. while (a){</li> <li>2.    if (b)</li> <li>3.    i++;</li> <li>4. }</li> <li>1. while (a){</li> <li>2.    if (b)</li> <li>3.    i++;</li> <li>4. }</li> <li>1. while (a){</li> <li>5.    .....</li> </ol>	<ol style="list-style-type: none"> <li>1. while (a){</li> <li>2.    if (b)</li> <li>3.    i++;</li> <li>4. }</li> <li>1. while (a){</li> <li>2.    if (b)</li> <li>3.    i++;</li> <li>4. }</li> <li>1. while (a){</li> <li>2.    if (b)</li> </ol>	<p>1<sup>st</sup> Loop Iteration</p> <p>2<sup>nd</sup> Loop Iteration</p> <p>3<sup>rd</sup> Loop Iteration</p>
--	---	--

Use control dependencies!

58

### Formal notion of Alignment

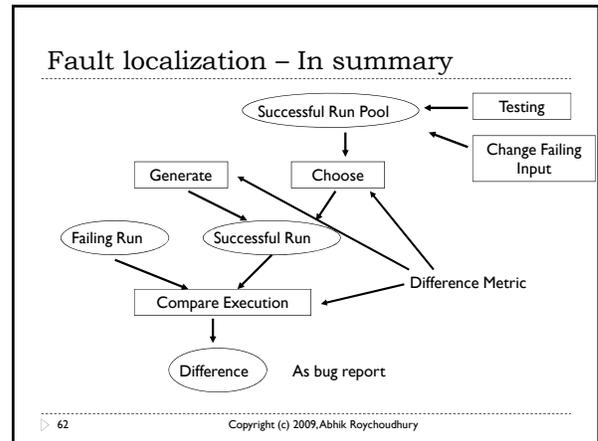
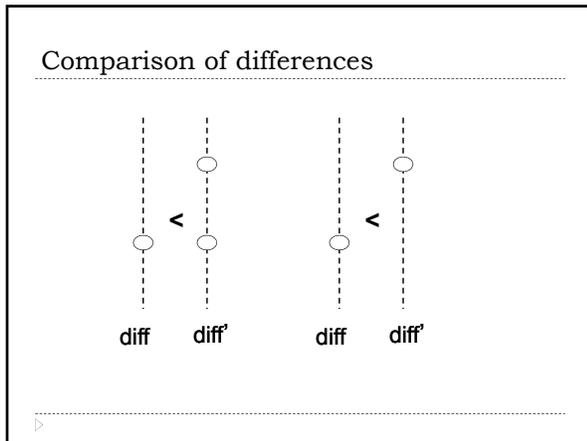
For any pair of event  $e$  in run  $x$  and event  $e0$  in run  $y$ , we define  $align(e, e0) = true$  ( $e$  and  $e0$  are aligned) iff.

- ▶  $stmt(e) = stmt(e0)$ , and
- ▶ either
  - ▶  $e, e0$  are the first events appearing in runs  $x, y$  or
  - ▶  $align(dep(e, x), dep(e0, y)) = true$ .
    - ▶  $dep(e, x) ==$  the event on which  $e$  is dynamically control dependent in run  $x$ .

59 CSS219 2010-11 by Abhik

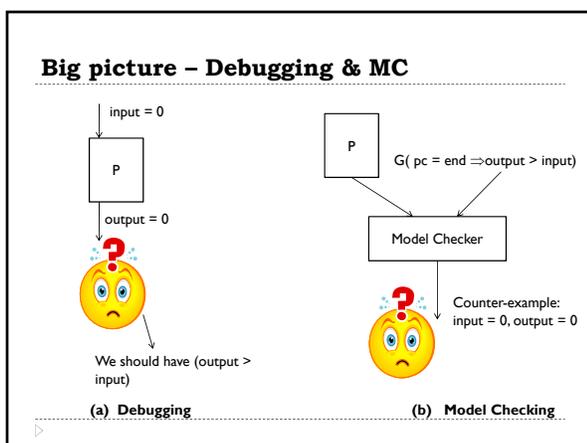
### Comparison of differences

60

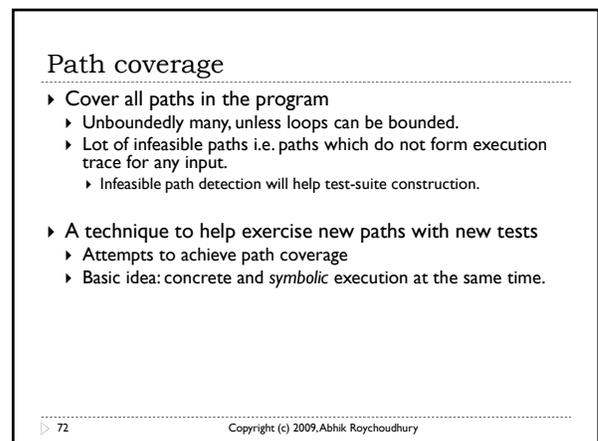
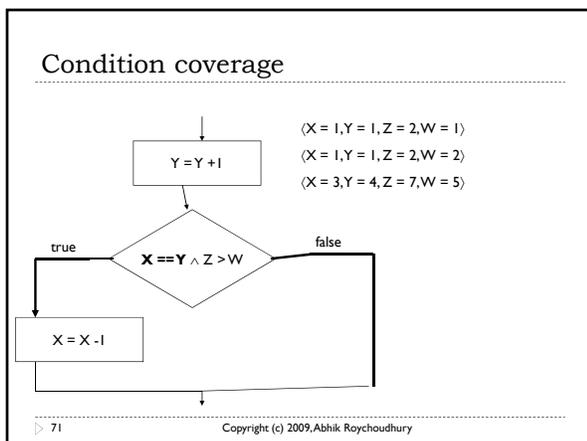
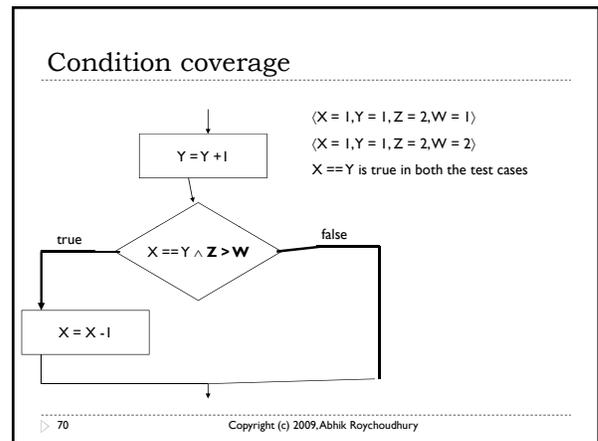
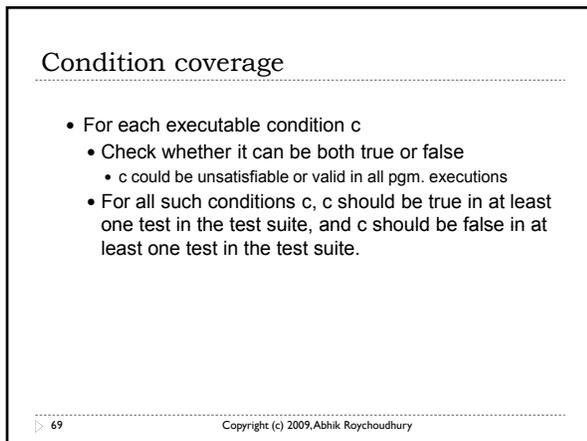
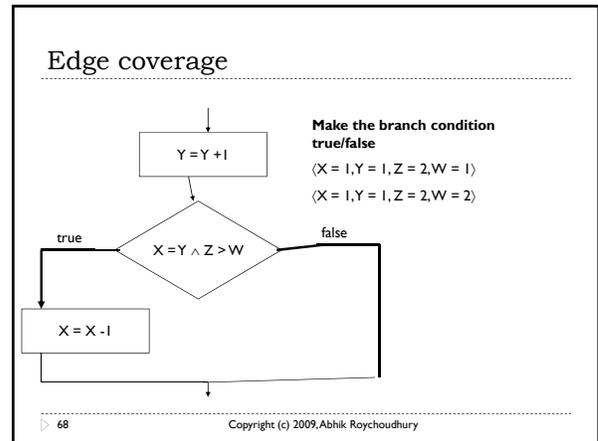
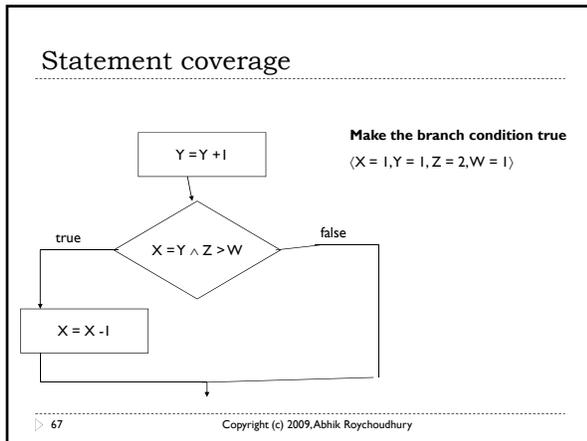


- ### Organization
- ▶ Dynamic checking of programs
    - ▶ Dynamic slicing
    - ▶ Hierarchical slicing
    - ▶ Fault Localization
    - ▶ Directed testing
- 63 Copyright (c) 2009, Abhik Roychoudhury

- ### Big picture – Testing and Debugging
- ▶ Why test?
    - ▶ Feel good about the program you have written.
  - ▶ How does it relate to fault localization?
    - ▶ Testing identifies which inputs we run the program against.
      - ▶ What is a good set of inputs to test?
    - ▶ Once you run the selected inputs, for some of them the output is unexpected.
      - ▶ These are the failing tests.
      - ▶ These are subjected to fault localization.
- 64



- ### Common terminology
- ▶ Test case
    - ▶ A test input (or its execution trace)
  - ▶ Test suite
    - ▶ Set of test cases
  - ▶ Test purpose
    - ▶ A formal specification to guide testing
      - ▶ e.g. a regular expression which the test case should satisfy
  - ▶ Coverage criterion
    - ▶ A guide to exhaustively cover program structure.
      - ▶ e.g. Statement coverage, Cond. coverage, Path coverage.
- 66 Copyright (c) 2009, Abhik Roychoudhury



## Directed testing

- ▶ Start with a random input  $I$ .
- ▶ Execute program  $P$  with  $I$ 
  - ▶ Suppose  $I$  executes path  $p$  in program  $P$ .
  - ▶ While executing  $p$ , collect a symbolic formula  $f$  which captures the set of all inputs which execute path  $p$  in program  $P$ .
  - ▶  $f$  is the **path condition of path  $p$  traced by input  $i$** .
- ▶ Minimally change  $f$ , to produce a formula  $f_1$ 
  - ▶ Solve  $f_1$  to get a new input  $I_1$  which executes a path  $p_1$  different from path  $p$ .

▶ 73

Copyright (c) 2009, Abhik Roychoudhury

## Example program

- ▶ if (Climb)
  - ▶ separation =  $U_p$ ;
- ▶ else
  - ▶ separation =  $U_p + 100$ ;      Start with random input
- ▶ if (separation > 150)      (Climb == 0,  $U_p$  == 457)
  - ▶ upward = 1;
- ▶ else
  - ▶ upward = 0;
- ▶ if (upward > 0)
  - ▶ printf("Upward");
- ▶ else
  - ▶ printf("Downward");

▶ 74

Copyright (c) 2009, Abhik Roychoudhury

## Example program

- ▶ if (Climb)
  - ▶ separation =  $U_p$ ;
- ▶ else
  - ▶ separation =  $U_p + 100$ ;      Climb == 0  $\wedge$
- ▶ if (separation > 150)      ( $U_p + 100 > 150$ )  $\wedge$ 
  - ▶ upward = 1;
- ▶ else
  - ▶ upward = 0;
- ▶ if (upward > 0)      upward > 0
  - ▶ printf("Upward");
- ▶ else
  - ▶ printf("Downward");

▶ 75

Copyright (c) 2009, Abhik Roychoudhury

## Generating new tests

- ▶ The path condition calculated
  - ▶ Climb == 0  $\wedge$   $U_p + 100 > 150 \wedge$  upward > 0
- ▶ Minimally modify the condition
  - ▶ Climb == 0  $\wedge$   $U_p + 100 > 150 \wedge \neg(\text{upward} > 0)$
- ▶ Corresponding to the path ...

▶ 76

Copyright (c) 2009, Abhik Roychoudhury

## Infeasible path!!

- ▶ if (Climb)
  - ▶ separation =  $U_p$ ;
- ▶ else
  - ▶ separation =  $U_p + 100$ ;      Climb == 0  $\wedge$
- ▶ if (separation > 150)      ( $U_p + 100 > 150$ )  $\wedge$ 
  - ▶ upward = 1;
- ▶ else
  - ▶ upward = 0;
- ▶ if (upward > 0)
  - ▶ printf("Upward");
- ▶ else
  - ▶ printf("Downward");       $\neg$  upward > 0

▶ 77

Copyright (c) 2009, Abhik Roychoudhury

## Generating new tests

- ▶ The path condition calculated
  - ▶ Climb == 0  $\wedge$   $U_p + 100 > 150 \wedge$  upward > 0
- ▶ Minimally modify the condition
  - ▶ Climb == 0  $\wedge$   $U_p + 100 > 150 \wedge \neg(\text{upward} > 0)$
  - ▶ Corresponding to infeasible path!
- ▶ Modify a bit more
  - ▶ Climb == 0  $\wedge \neg$  ( $U_p + 100 > 150$ )
  - ▶ Corresponding to the path ...

▶ 78

Copyright (c) 2009, Abhik Roychoudhury

## Feasible path

- ▶ if (Climb)
  - ▶ separation = Up;
- ▶ else Climb == 0  $\wedge$
- ▶ separation = Up + 100;
- ▶ if (separation > 150)  $\neg$ (Up + 100 > 150)
- ▶ upward = 1;
- ▶ else
- ▶ upward = 0;
- ▶ if (upward > 0)
  - ▶ printf("Upward");
- ▶ else
- ▶ printf("Downward");

▶ 79

Copyright (c) 2009, Abhik Roychoudhury

## Generating new tests

- ▶ The path condition calculated
  - ▶  $\text{Climb} == 0 \wedge \text{Up} + 100 > 150 \wedge \text{upward} > 0$
- ▶ Minimally modify the condition
  - ▶  $\text{Climb} == 0 \wedge \text{Up} + 100 > 150 \wedge \neg(\text{upward} > 0)$
  - ▶ Corresponding to infeasible path!
- ▶ Modify a bit more
  - ▶  $\text{Climb} == 0 \wedge \neg(\text{Up} + 100 > 150)$
  - ▶ Solve to get another test input
    - ▶  $\text{Climb} == 0, \text{Up} == 0$
- ▶ Continue in this fashion.

▶ 80

Copyright (c) 2009, Abhik Roychoudhury

## Path condition computation

```

1 input x, y, z;
2 if (y > 0){
3   z = y * 2;
4   x = y - 2;
5   x = x - 2;}
6 if (z == x){
7   output("How did I get here");
}

```

▶

## Path condition computation

Line#	Assignment store	Path cond.
1	{}	true
2	{}	$y > 0$
3	{}	$y > 0$
4	{ $(z, 2^*y)$ }	$y > 0$
5	{ $(z, 2^*y)$ }	$y > 0$
6	{ $(z, 2^*y), (x, y-2)$ }	$y > 0$
7	{ $(z, 2^*y), (x, y-4)$ }	$y > 0$
	{ $(z, 2^*y), (x, y-4)$ }	$y > 0 \wedge 2^*y == y - 4$
	{ $(z, 2^*y), (x, y-4)$ }	false

▶

## Path condition computation

- ▶ We traverse forward along the sequence of statements in the given path, starting with a null formula and gradually building it up. At any point during the traversal of the trace, we maintain a set of symbolic expressions for the program variables and the path condition.
  - ▶ for every assignment encountered, we update the symbolic assignment store.
  - ▶ for every branch statement encountered, we conjoin the branch condition with the path condition. While doing so, we use the symbolic assignment store for every variable appearing in the branch condition.
- ▶ At the end of the trace, we get the path condition.

▶

## Topics Covered

- ▶ Dynamic checking of programs
  - ▶ Dynamic slicing - what was important & executed
  - ▶ Hierarchical slicing – managing dynamic slices
  - ▶ Fault Localization – Trace comparison
  - ▶ Directed testing – Symbolic execution along traces
- ▶ Static checking of programs – Not covered in this module

▶ 84

Copyright (c) 2009, Abhik Roychoudhury