Programming Language Concepts, CS2104 Lecture 2

Oz Syntax, Data structures

Reminder of last lecture

- Oz, Mozart
- Concepts of
 - Variable, Type, Cell
 - Function, Recursion, Induction
 - Correctness, Complexity
 - Lazy Evaluation
 - Higher-Order Programming
 - Concurrency, Dataflow
 - Object, Classes
 - Nondeterminism, Interleaving, Atomicity

Overview

- Programming language definition: syntax, semantics
 CFG, EBNF
- Data structures
 - □ simple: integers, floats, literals
 - compound: records, tuples, lists
- Kernel language
 - linguistic abstraction
 - data types
 - variables and partial values
 - statements and expressions (next lecture)

Language Syntax

Language = Syntax + Semantics

- The syntax of a language is concerned with the form of a program: how expressions, commands, declarations etc. are put together to result in the final program.
- The semantics of a language is concerned with the meaning of a program: how the programs behave when executed on computers.

Programming Language Definition

Syntax: grammatical structure

- Lexical: how words are formed
- Phrasal: how sentences are formed from words
- Semantics: meaning of programs
 - Informal: English documents (e.g. reference manuals, language tutorials and FAQs etc.)
 - Formal:
 - Operational Semantics (execution on an abstract machine)
 - Denotational Semantics (each construct defines a function)
 - Axiomatic Semantics (each construct is defined by pre and post conditions)

Language Syntax

Defines *legal* programs

- programs that can be executed by machine
- Defined by grammar rules
 - define how to make 'sentences' out of 'words'

For programming languages

- sentences are called *statements* (commands, expressions)
- words are called *tokens*
- grammar rules describe both tokens and statements

Language Syntax

- *Token* is sequence of characters
- Statement is sequence of tokens
- *Lexical analyzer* is a program
 - recognizes character sequence
 - produces token sequence
- Parser is a program
 - recognizes a token sequence
 - produces statement representation
- Statements are represented as parse trees



Parse Trees = Abstract Syntax Trees

fun {Fact N} if N == 0 then 1 else $N*{Fact N-1}$ end Fact end

[fun'{''F'act''N''}''\n'''if'' 'N''=''='0''then''1'\n'''else ''N'*''{''F'act'''N''-'1'}'''en d'\n'end]

['fun' '{' 'Fact' 'N' '}' 'if' 'N' '==' '0' 'then' 'else' 'N' '*' '{' 'Fact' 'N' '-' '1' '}' 'end' 'end']



Context-Free Grammars

• A context-free grammar (CFG) is:

- A set of terminal symbols T (tokens or constants)
- A set of non-terminal symbols N
- $\hfill\square$ One (non-terminal) start symbol σ
- A set of grammar (rewriting) rules Ω of the form

 $\langle nonterminal \rangle ::= \langle sequence of terminals and nonterminals \rangle$

- Grammar rules (productions) can be used to
 - verify that a statement is legal
 - generate all possible statements
- The set of all possible statements generated by a grammar from the start symbol is called a (*formal*) *language*

Context-Free Grammars (Example)



These trees are called parse trees or syntax trees or derivation trees.

Why do we need CFGs for describing syntax of programming languages

- A programming language may have arbitrary number of nested statements, such as: if-then-else-end, local-in-end, and so on.
- $L_1 = \{(if-then)^n end^n (local-in)^m end^m \mid n, m > 0\}$

```
local ... in
    if ... then
        local ... in ... end
        else ...
        end
        end
```

Backus-Naur Form

- BNF is a common notation to define contextfree grammars for programming languages
- <digit> is defined to represent one of the ten tokens 0, 1, ..., 9

 $\langle digit \rangle ::= 0 | 1 | 2 | 3 | 5 | 6 | 7 | 8 | 9$

(Positive) Integers

 $\langle \text{integer} \rangle ::= \langle \text{digit} \rangle | \langle \text{digit} \rangle \langle \text{integer} \rangle$

 $\langle digit \rangle ::= 0 | 1 | 2 | 3 | 5 | 6 | 7 | 8 | 9$

(integer) is defined as the sequence of a (digit) followed by zero or more (digit)'s

Extended Backus-Naur Form

- EBNF is a more compact notation to define the syntax of programming languages.
- EBNF has the same power as CFG.
- *Terminal symbol* is a token.
- Nonterminal symbol is a sequence of tokens, and is represented by a grammar rule:

 $\langle nonterminal \rangle ::= \langle rule body \rangle$

As EBNF, (positive) integers may be defined as:

 $\langle \text{integer} \rangle ::= \langle \text{digit} \rangle \{ \langle \text{digit} \rangle \}$

 (integer) is defined as the sequence of a (digit) followed by zero or more (digit)'s

Extended Backus-Naur Form Notations

- $\langle x \rangle \\ \langle x \rangle ::= Body \\ \langle x \rangle | \langle y \rangle$
- $\land \langle x \rangle \langle y \rangle$
- $= \{ \langle X \rangle \}$

• $\{\langle X \rangle\}^+$

 $\bullet [\langle X \rangle]$

nonterminal x $\langle x \rangle$ is defined by *Body* either $\langle x \rangle$ or $\langle y \rangle$ (choice) the sequence $\langle x \rangle$ followed by $\langle y \rangle$ sequence of zero or more occurrences of $\langle x \rangle$ sequence of one or more occurrences of $\langle x \rangle$ zero or one occurrence of $\langle x \rangle$

Extended Backus-Naur Form Examples

- $\langle expression \rangle ::= \langle variable \rangle | \langle integer \rangle | ... \rangle$
- <statement> ::= skip | <expression> '=' <expression> | ...
 if <expression> then <statement>
 { elseif <expression> then <statement> }
 [else <statement>] end
 ...

Extended Backus-Naur Form Examples

Description of (positive) real numbers:

- <real-#> ::= <int-part>. <fraction>
 <int-part> ::= <digit> | <int-part> <digit>
 <fraction> ::= <digit> | <digit> <fraction>
 <digit> ::= 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9
- **Token:** 13.79



"In '57, parsing expressions was not so easy"!



John Backus principal papers Backus-Naur form, Fortran

 Describing his early work on FORTRAN, <u>Backus</u> said:-

"We did not know what we wanted and how to do it. It just sort of grew. The first struggle was over what the language would look like. Then how to parse expressions - it was a big problem and what we did looks astonishingly clumsy now...."

Turing Award, 1977

Data Structures (Values)

Simple data structures

integers 42, ~1, 0
 means unary minus
 floating point 1.01, 3.14
 atoms atom, 'Atom', nil

- Compound data structures
 - tuples: combining several values
 - records: generalization of tuples
 - lists: special cases of tuples



Have a label

• e.g: state

Combine several values (variables)

- **e.g:** 1, a, 2
- position is significant!



- {Label X} returns label of tuple X
 - **here:** state
 - is an atom
- Width X} returns the width (number of fields)
 - **here:** 3
 - is a positive integer



- Fields are numbered from 1 to {Width X}
- x.N returns N-th field of tuple
 - □ here, X.1 returns 1
 - **here**, X.3 returns 2
- In X.N, N is called feature

Tuples for Trees



Trees can be constructed with tuples:

declare Y=s(1 2) Z=r(3 4) X=m(Y Z)

Constructing Tuple Skeletons

{MakeTuple Label Width}

- creates new tuple with label Label and width Width
- fields are initially unbound
- Access to fields then by "dot"

Example Tuple Construction

Created by execution of

declare

$$X = \{MakeTuple a 3\}$$



Example Tuple Construction

After execution of

$$X.2 = b$$

 $X.3 = c$



Records

Records are generalizations of tuples

- features can be atoms
- □ features can be arbitrary integers
 - not restricted to start with 1
 - not restricted to be consecutive
- Records also have Label and Width



- Position is insignificant
- Field access is as with tuples
 X.a is 1

Tuples are Records

Constructing

- declare
- X = state(1:a 2:b 3:c)

is equivalent to

X = state(a b c)

A Way to Build Binary Trees

```
declare
Root=node(left:X1 right:X2 value:0)
                                                 ()
X1=node(left:X3 right:X4 value:1)
X2=node(left:X5 right:X6 value:2)
X3=node(left:nil right:nil value:3)
X4=node(left:nil right:nil value:4)
X5=node(left:nil right:nil value:5)
X6=node(left:nil right:nil value:6)
                                             3
                                                   5
                                                4
{Browse Root}
proc {Preorder X}
 if X = nil then \{Browse X.value\}
   if X.left \geq nil then {Preorder X.left} end
   if X.right \= nil then {Preorder X.right} end
 end
end
{Preorder Root}
```

A Way to Build Binary Trees

Oz Browser	×
Browser Selection Options	
<pre>node(left:node(left:node(left:nil right:nil value:3) right:node(left:nil right:nil value:4) value:1) right:node(left:node(left:nil right:nil value:5) right:node(left:nil right:nil value:6) value:2)</pre>	
value:0) 0 1 3 4 2 5 6	

Lists

- A list contains a sequence of elements:
 - □ is the empty list, or
 - consists of a *cons* (or *list pair*) with *head* and *tail*
 - head contains an element
 - tail contains a list
- Lists are encoded with atoms and tuples
 - o empty list: the atom nil
 - □ cons: tuple of width 2 with label ` | '
- Special syntax for cons

X = Y | Z

instead of

X = (Y Z)

Both are equivalent!

An Example List

After execution of



X1=a|X2 X2=b|X3 X3=c|nil



Simple List Construction

 One can also write X1=a|b|c|nil
 which abbreviates
 X1=a|(b|(c|nil)))
 which abbreviates
 X1=`|'(a`|'(b`\|'(c nil)))

 Even shorter

X1=[a b c]

Computing With Lists

- Remember: a cons is a tuple!
- Access head of cons

Χ.1

Access tail of cons

Х.2

Test whether list x is empty:

if X==nil then ... else ... end

Head And Tail

Define abstractions for lists

```
fun {Head Xs}
   Xs.1
```

end

fun {Tail Xs}

Xs.2

end

- {Head [a b c]}
 returns a
- {Tail [a b c]}

returns [b c]

{Head {Tail {Tail [a b c]}}

returns c

How to Process Lists. General Method

- Lists are processed recursively
 - base case: list is empty (nil)
 - inductive case: list is cons

access head, access tail

- Powerful and convenient technique
 - pattern matching
 - matches patterns of values and provides access to fields of compound data structures
How to Process Lists. Example

- Input: list of integers
- Output: sum of its elements
 implement function Sum
- Inductive definition over list structure
 - Sum of empty list is 0
 - $\hfill\square$ Sum of non-empty list $\hfill \bot$ is

```
\{\text{Head L}\} + \{\text{Sum }\{\text{Tail L}\}\}
```

Sum of the Elements of a List using Conditional Construct

```
fun {Sum L}
    if L==nil
    then 0
    else {Head L} + {Sum {Tail L}}
    end
end
```

Sum of the Elements of a List using Pattern Matching

```
fun {Sum L}
case L
of nil then 0
[] H|T then H +{Sum T}
end
end
```

Sum of the Elements of a List using Pattern Matching



nil is the pattern of the clause

Sum of the Elements of a List using Pattern Matching



H|T is the pattern of the clause

Pattern Matching

- The first clause uses of, all other []
- Clauses are tried in textual order (left to right, top to bottom)
- A clause matches, if its pattern matches
- A pattern matches, if the width, label and features agree
 - then, the variables in the pattern are assigned to the respective fields
- Case-statement executes with first matching clause

Length of a List

- Inductive definition
 - □ length of empty list is 0
 - $\hfill\square$ length of cons is 1 + length of tail

```
fun {Length Xs}
    case Xs
    of nil then 0
    [] X|Xr then 1+{Length Xr}
    end
end
```

General Pattern Matching

- Pattern matching can be used not only for lists!
- Any value, including numbers, atoms, tuples, records

```
fun {DigitToString X}
    case X
    of 0 then "Zero"
    [] 1 then "One"
    [] . . .
    end
end
```

Language Semantics

- Defines what a program does when executed
- Considerations:
 - simplicity
 - allow programmer to reason about program (correctness, execution time, and memory use)
- Practical language used to build complex systems (millions lines of code) must often be expressive.
- Solution : Kernel language approach for semantics

Kernel Language Approach

- Define simple language (kernel language)
- Define its computation model
 - how language constructs (statements) manipulate (create and transform) data structures
- Define mapping scheme (translation) of full programming language into kernel language
- Two kinds of translations
 - linguistic abstractions
 - syntactic sugar

Kernel Language Approach



Linguistic Abstractions \Leftrightarrow Syntactic Sugar

- Linguistic abstractions provide higher level concepts
 - programmer uses to model and reason about programs (systems)
 - examples: functions (fun), iterations (for), classes and objects (class)
- Functions (calls) are translated to procedures (calls). This eliminates a redundant construct from the semantics viewpoint.

Linguistic Abstractions \Leftrightarrow Syntactic Sugar

 Linguistic abstractions: provide higher level concepts
 Syntactic sugar: short cuts and conveniences to improve readability





Approaches to Semantics



Aid programmer in reasoning and understanding

Mathematical study of programming (languages) λ -calculus, predicate calculus, π -calculus Aid implementer in efficient execution on a real machine

Sequential Declarative Computation Model

Single assignment store

- declarative (dataflow) variables and values (together called *entities*)
- values and their types
- Kernel language syntax
- Environment
 - maps textual variable names (variable identifiers) into entities in the store
- *Execution* of kernel language statements
 - execution stack of statements (defines control)
 - store
 - transforms store by sequence of steps

Single Assignment Store

- Single assignment store is store (set) of variables
- Initially variables are unbound
- Example: store with three variables, x₁, x₂, and x₃

Store		
	<i>X</i> ₁	unbound
	<i>X</i> ₂	unbound
	<i>X</i> ₃	unbound

Single Assignment Store

- Variables in store may be bound to values
- Example:
 - x₁ is bound to integer
 314
 - x_2 is bound to list [1 2 3]
 - \square x_3 is still unbound



Reminder : Variables and Partial Values

- Declarative variable
 - resides in single-assignment store
 - is initially unbound
 - can be bound to exactly one (partial) value
 - can be bound to several (partial) values as long as they are compatible with each other
- Partial value
 - data-structure that may contain unbound variables
 - when one of the variables is bound, it is replaced by the (partial) value it is bound to
 - a complete value, or value for short is a data-structure that does not contain any unbound variable

Value Expressions in the Kernel Language

 $\langle v \rangle$::= $\langle number \rangle | \langle record \rangle | \langle procedure \rangle$

```
\begin{array}{ll} \langle number \rangle & ::= \langle int \rangle \mid \langle float \rangle \\ \langle record \rangle, \langle pattern \rangle ::= \langle literal \rangle \mid \\ & \langle literal \rangle \left( \langle feature_1 \rangle : \langle x_1 \rangle \dots \langle feature_n \rangle : \langle x_n \rangle \right) \\ \langle literal \rangle & ::= \langle atom \rangle \mid \langle bool \rangle \\ \langle feature \rangle & ::= \langle int \rangle \mid \langle atom \rangle \mid \langle bool \rangle \\ \langle bool \rangle & ::= true \mid false \end{array}
```

 $\langle \text{procedure} \rangle ::= \text{proc} \{ \{ \langle y_1 \rangle \dots \langle y_n \rangle \} \langle s \rangle \text{ end} \}$

Statements and Expressions

- Expressions describe computations that return a value
- Statements just describe computations
 - Transforms the state of a store (single assignment)
- Kernel language
 - Expressions allowed: value construction for primitive data types
 - Otherwise statements

Variable Identifiers

• $\langle x \rangle$, $\langle y \rangle$, $\langle z \rangle$ stand for variables identifiers

Concrete kernel language variables identifiers

- □ begin with an upper-case letter
- followed by (possibly empty) sequence of alphanumeric characters or underscore
- Any sequence of characters within backquotes
 Examples:
 - X, Y1
 - Hello_World
 - 'hello this is a \$5 bill' (backquote)

Values and Types

- Data type
 - set of values
 - set of associated operations
- Example: Int is data type "Integer"
 - set of all integer values
 - □ 1 is of type Int
 - □ has set of operations including +, -, *, div, etc
- Model comes with a set of basic types
- Programs can define other types
 - for example: abstract data types ADT (<Stack T> is an ADT with elements of type T and 4 operations. Type T can be anything, and the operations must satisfy certain laws, but they can have any particular implementation Section 3.7)

Data Types



Kernel's Primitive Data Types



Numbers

- Number: either Integer or Float
- Integers:
 - Decimal base:
 - 314, 0, ~10 (minus 10)
 - Hexadecimal base:
 - 0xA4 (164 in decimal base)
 - OX1Ad (429 in decimal base)
 - Binary base:
 - Ob1101 (13 in decimal base)
 - OB11 (3 in decimal base)

Floats:

□ 1.0, 3.4, 2.34e2, ~3.52E~3 (~3.52×10⁻³)

Literals: Atoms and Booleans

- Literal: atom or boolean
- Atom (symbolic constant):
 - A sequence starting with a lower-case character followed by characters or digits: person, peter
 - Any sequence of printable characters enclosed in single quotes: 'I am an atom', 'Me too'
 - Note: backquotes are used for variable identifier (`John Doe`)

Booleans:

- 🛛 true
- false

Records

Compound data-structures

- $\Box \langle l \rangle (\langle f_1 \rangle : \langle x_1 \rangle \dots \langle f_n \rangle : \langle x_n \rangle)$
- the label: $\langle I \rangle$ is a literal
- the features: $\langle f_1 \rangle$, ..., $\langle f_n \rangle$ can be atoms, integers, or booleans
- the variable identifiers: $\langle x_1 \rangle$, ..., $\langle x_n \rangle$
- Examples:
 - person(age:X1 name:X2)
 - □ person(1:X1 2:X2)
 - □ ' | ' (1:H 2:T) % no space after ' | '
 - 🛛 nil
 - 🛛 person
 - An atom is a record without features!

Syntactic Sugar

Tuples

 $\langle h \rangle (\langle x_1 \rangle \dots \langle x_n \rangle)$ (tuple) equivalent to record $\langle h \rangle (1: \langle x_1 \rangle \dots n: \langle x_n \rangle)$ Lists '|' ($\langle hd \rangle \langle th \rangle$) A string: a list of character codes:

[87 101 32 108 105 107 101 32 79 122 46]

can be written with double quotes: "We like Oz."

Operations on Basic Types

- Numbers
 - □ floats: +, -, *, /
 - □ integers: +, -, *, div, mod

Records

- Arity, Label, Width, and "."
- \u00ed X = person(name:"George" age:25)
- {Arity X} returns [age name]
- 4 {Label X} returns person
- X.age returns 25
- Comparisons (integers, floats, and atoms)
 - equality: ==, \setminus =
 - □ order: =<, <, >=

Variable-Variable Equality (Unification)

- It is a special case of unification
- Example: constructing graphs
 - declare
 - ΥZ
 - X=a(YZ)



Variable-Variable Equality (Unification)

- Now bind z to x
 - Z = X
- Possible due to deferred assignment



Variable-Variable Equality (Unification)

- Consider X=Y when both X and Y are bound
- Case one: no variables involved
 - If the graphs starting from the nodes of X and Y have the same structure, then do nothing (also called *structure equality*).
 - If the two terms cannot be made equal, then an exception is raised.
- Case two: x or y refer to partial values
 - the respective variables are bound to make X and Y the "same"

Case One: no Variables Involved

This is not unification, because there will no binding.

declare

- X=r(a b) Y=r(a b)
- X=Y % passes silently

declare

- X=r(a b) Y=r(a c)
- X=Y % raises an failure error

Failure errors are exceptions which should be caught.

Case two: x or y refers to partial values

- Unification is used because of partial values.
- declare

r(X Y)=r(1 2)

- X is bound to 1, Y is bound to 2
- declare U Z

```
X=name(a U)
```

```
Y=name(Z b)
```

Х=Х

U is bound to b, Z is bound to a

Case two: x or y refers to partial values

declare

- X=r(name:full(Given Family)
 age:22)
- Y=r(name:full(claudia Johnson)
 age:A)
- X=Y % Given=claudia,A=22,Johnson=Family

declare

- X=r(a X) Y=r(a r(a Y))
- X=Y % this is fine
- Both X, Y are r(a r(a r(a ...))) % ad infinitum

Unification

- unify(x, y) is the operation that unifies two partial values x and y in the store
- Store is a set {x1, ..., xk} partitioned as follows:
 - Sets of unbound variables that are equal (also called *equivalence sets of variables*).
 - Variables bound to a number, record, or procedure (also called *determined variables*).
- Example: {x1=name(a:x2), x2=x9=73,
Unification. The primitive bind operation

bind(ES, <v>) binds all variables in the equivalence set ES to <v>.

Example: bind({x7, x8}, name(a:x2))

• bind(ES_1, ES_2) merges the equivalence set ES_1 with the equivalence set ES_2 .

Example: bind({x3, x4, x5}, {x6})

The Unification Algorithm: unify(x,y)

- 1. If x is in ES_x and y is in ES_y , then do bind(ES_x , ES_y).
- 2. If x is in ES_x and y is determined, then do bind(ES_x , y).
- 3. If y is in ES_y and x is determined, then do bind(ES_y , x).

4. If

- *x* is bound to $I(I_1:x_1,...,I_n:x_n)$ and *y* is bound to $I'(I'_1:y_1,...,I'_m:y_m)$ with $l \neq l'$ or
- 2. $\{l_1, \ldots, l_n\} \neq \{l'_1, \ldots, l'_m\},\$

then raise a failure exception.

5. If x is bound to $l(l_1:x_1,...,l_n:x_n)$ and y is bound to $l(l_1:y_1,...,l_n:y_n)$, then for *i* from 1 to *n* do unify (x_i, y_i) .

Handling Cycles

The above algorithm does not handle unification of partial values with cycles.

Example:

- The store contains x = f(a:x) and y = f(a:y).
- Calling unify(x, y) results in the recursive call unify(x, y), ...
- □ The algorithm loops forever!
- However x and y have exactly the same structure!

The New Unification Algorithm: unify'(x,y)

- Let *M* be an empty table (initially) to be used for memoization.
- Call unify '(x, y).
- Where unify '(x, y) is:
 - □ If $(x, y) \in M$, then we are done.
 - Otherwise, insert (x, y) in M and then do the original algorithm for unify(x, y), in which the recursive calls to unify are replaced by calls to unify'.

Displaying cyclic structures

declare X
X = ' | ' (a ' | ' (b X)) % or X = a | b | X
{Browse X}

Oz Browser	
Browser Selection Op	otions
a b a b a b a b a b a b a b a b a b a b	

Example: rational trees (section 12.3.1) The graph X=foo(X) represents the tree X=foo(foo(foo(...))).

Entailment (the == operation)

- It returns the value true if the graphs starting from the nodes of X and Y have the same structure (it is called also structure equality).
- It returns the value false if the graphs have different structure, or some pairwise corresponding nodes have different values.
- It blocks when it arrives at pairwise corresponding nodes that are different, but at least one of them is unbound.

Entailment (example)

- Entailment check/test never do any binding.
- declare
 - L1=[1 2]
 - L2=' | ' (1 ' | ' (2 nil))
 - L3=[1 3]
 - {Browse L1==L2}
 - {Browse L1==L3}
- declare
 - L1=[1] L2=[X] {Browse L1==L2}
- % blocks as X is unbound

Summary

- Programming language definition: syntax, semantics
 CFG, EBNF, ambiguity
- Data structures
 - □ simple: integers, floats, literals
 - compound: records, tuples, lists
- Kernel language
 - linguistic abstraction
 - data types
 - variables and partial values
 - statements and expressions (next lecture)

Lab Session 0

- Wed 24th August 2007
- Time : 3-6pm (choose 1-hr slot)
- Venue : -
- Deadline : 28th August 2007 5pm

Reading suggestions

From [van Roy,Haridi; 2004]

- □ Chapter 2, Sections 2.1.1-2.3.5
- □ Appendices B, C
- Exercises 2.9.1-2.9.3