

# Lab Week 7

CS4215: Programming Language Implementation

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- 1 Heap Memory
  - Memory Allocation for Programs
  - A Heap Memory Model
  - simPLvm with Heap
  - Implementing a Heap
- 2 Heap Management Techniques

## Resources of computing

- Time: accounted for by simPLvm, number of executed instructions
- Memory: not well represented yet, instructions freely construct “things”

## Questions

- Does a given data structure have to be stored forever?
- Will a given program run out of memory?
- Can we design a virtual machine that makes effective use of the available memory?

# Memory Allocation for Programs

- Static allocation
- Stack allocation
- Heap allocation

# Static Allocation

- Assign fixed memory location for every identifier
- Limitations
  - The size of each data structure must be known at compile-time. For example, arrays whose size depends on function parameters are not possible.
  - Recursive functions are not possible, because each recursive call needs its own copy of parameters and local variables.
  - Data structures such as closures cannot be created dynamically.

## Stack Allocation

- Keep track of information on function invocations on runtime stack
- Recursion possible
- Size of locals can depend on arguments
- Remaining shortcomings:
  - Difficult to manipulate recursive data structures
  - Only objects with known compile time size can be returned from functions

# Heap Allocation

- Data structures may be allocated and deallocated in any order
- Complex pointer structures will evolve at runtime
- Management of allocated memory becomes an issue

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# A Heap Memory Model

- Nodes: stack frames, operand stacks, environments etc
- Edges: references between nodes
- Labels on edges
- Nodes can point to primitive values

## Formal Model of Heap

A heap is a pair  $(V, E)$ , where

$$E \subseteq \{(v, f, w) \mid v \in V, f \in \mathbf{LS} + \mathbf{Int}, w \in V + \mathbf{PV}\}$$

Edge  $(v, f, w)$  has source  $v$ , label  $f$  and target  $w$ .

Edges are functional in the first two arguments.

## Operations on Heaps

$$\text{newnode}((V, E)) = (v, (V \cup \{v\}, E))$$

where  $v$  is chosen new;  $v \notin V$

$$\text{update}(v, f, w, (V, E)) = (V, (v, f, w) \cup (E - \{(v, f, w') \mid w' \in W\}))$$

## Operations on Heaps (continued)

$$\text{children}(v, (V, E)) = \{w \in W \mid (v, f, w) \in E \text{ for some } f \in L\}$$

$$\text{nodechildren}(v, (V, E)) = \{w \in V \mid (v, f, w) \in E \text{ for some } f \in L\}$$

$$\text{labels}(v, (V, E)) = \{f \in L \mid (v, f, w) \in E \text{ for some } w \in W\}$$

$$\text{deref}(v, f, (V, E)) = w, \text{ where } (v, f, w) \in E$$

## Operations on Heaps (continued)

$$\begin{aligned} \text{copy}(v, (V, E)) &= (v', (V \cup \{v'\}, E \cup \{(v', f_1, \text{deref}(v, f_1, (V, E))), \dots, \\ &\quad (v', f_n, \text{deref}(v, f_n, (V, E)))\})) \\ &\text{where } \{f_1, \dots, f_n\} = \text{labels}(v, (V, E)) \end{aligned}$$

## Operations on Heaps (continued)

$newstack(h) = (v, h'')$   
 where  $(v, h') = newnode(h)$ ,  
 and  $h'' = update(v, size, 0, h')$

$push(v, w, h) = h''$   
 where  $s = deref(v, size, h)$ ,  
 $h' = update(v, size, s + 1, h)$ ,  
 and  $h'' = update(v, s, w, h')$

$pop(v, h) = (w, h')$   
 where  $s = deref(v, size, h)$ ,  
 $h' = update(v, size, s - 1, h)$ ,  
 and  $w = deref(v, s - 1, h')$

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## Starting State of simPLvm with Heap

We start the machine with a state of the form  $(os_0, 0, e_0, rs_0, h_0)$ , where

$$(os_0, h') = newstack((\emptyset, \emptyset))$$

$$(e_0, h'') = newnode(h')$$

$$(rs_0, h_0) = newstack(h'')$$

## Rules of simPLvm with Heap

$$\frac{s(pc) = \text{LDCI } i}{(os, pc, e, rs, h) \Rightarrow_s (os, pc + 1, e, rs, h')} \quad h' = \text{push}(os, i, h)$$

## Rules of simPLvm with Heap (continued)

$$s(pc) = \text{PLUS}$$

---


$$(os, pc, e, rs, h) \Rightarrow_s (os, pc + 1, e, rs, h''')$$

where

$$(i_2, h') = \text{pop}(os, h)$$

$$(i_1, h'') = \text{pop}(os, h')$$

$$h''' = \text{push}(os, i_1 + i_2, h'')$$

## Rules of simPLvm with Heap (continued)

$$s(pc) = \text{GOTOR } i$$

---


$$(os, pc, e, rs, h) \Rightarrow_s (os, pc + i, e, rs, h)$$

$$s(pc) = \text{JOFR } i$$

---


$$(os, pc, e, rs, h) \Rightarrow_s (os, pc + 1, e, rs, h')$$

if  $(t, h') = \text{pop}(os, h)$

## Rules of simPLvm with Heap (continued)

$$s(pc) = \text{LDS } x$$

---

$$(os, pc, e, rs, h) \Rightarrow_s (os, pc + 1, e, rs, h')$$

$$h' = \text{push}(os, \text{deref}(e, x, h), h)$$

## Rules of simPLvm with Heap (continued)

$$s(pc) = \text{LDFS } x_1 \cdots x_n$$

---


$$(os, pc, e, rs, h) \Rightarrow_s (os, pc + 1, e, rs, h')$$

where

$$(c, h^{(1)}) = \text{newnode}(h)$$

$$(f, h^{(2)}) = \text{newnode}(h^{(1)})$$

$$h^{(3)} = \text{update}(c, \text{address}, pc + 2, h^{(2)})$$

$$h^{(4)} = \text{update}(c, \text{formals}, f, h^{(3)})$$

$$h^{(5)} = \text{update}(c, \text{environment}, e, h^{(4)})$$

$$h^{(6)} = \text{push}(os, c, h^{(5)})$$

$$h^{(6+i)} = \text{update}(f, i, x_i, h^{(6+i-1)}), \text{ where } 1 \leq i \leq n$$

$$h' = h^{(6+n)}$$

## Rules (continued)

$$s(pc) = \text{CALL } n$$

---


$$(os, pc, e, rs, h) \Rightarrow_s (os', a, e', rs, h')$$

$$(v_{n-i+1}, h^{(i)}) = \text{pop}(os, h^{(i-1)}), \text{ where } 1 \leq i \leq n$$

$$h^{(n+i)} = \text{update}(e', \text{deref}(f, i, h^{(n+i-1)}), v_i, h^{(n+i-1)}),$$

$$\text{where } 1 \leq i \leq n$$

$$(c, h^{(2n+1)}) = \text{pop}(os, h^{(2n)})$$

$$a = \text{deref}(c, \text{address}, h^{(2n+1)})$$

$$f = \text{deref}(c, \text{formals}, h^{(2n+1)})$$

$$(e', h^{(2n+2)}) = \text{copy}(\text{deref}(c, \text{environment}, h^{(2n+1)}), h^{(2n+1)})$$

$$(sf, h^{(2n+3)}) = \text{newnode}(h^{(2n+2)})$$

## Rules (continued)

$$s(pc) = \text{CALL } n$$

---


$$(os, pc, e, rs, h) \Rightarrow_s (os', a, e', rs, h')$$

$$\begin{aligned} (v_{n-i+1}, h^{(i)}) &= \text{pop}(os, h^{(i-1)}), \text{ where } 1 \leq i \leq n \\ h^{(n+i)} &= \text{update}(e', \text{deref}(f, i, h^{(n+i-1)}), v_i, h^{(n+i-1)}), \\ &\text{where} \end{aligned}$$

...

$$\begin{aligned} (e', h^{(2n+2)}) &= \text{copy}(\text{deref}(c, \text{environment}, h^{(2n+1)}), h^{(2n+1)}) \\ (sf, h^{(2n+3)}) &= \text{newnode}(h^{(2n+2)}) \\ h^{(2n+4)} &= \text{update}(sf, pc, pc + 1, h^{(2n+3)}) \\ h^{(2n+5)} &= \text{update}(sf, os, os, h^{(2n+4)}) \\ h^{(2n+6)} &= \text{update}(sf, e, e, h^{(2n+5)}) \end{aligned}$$

## Memory Consumption of Instructions

We count the number of nodes and edges created by each instruction.

Example: LDFS  $x$   $y$   $z$  creates

- 2 nodes:  $c$ ,  $f$ ,
- 7 edges: 3 leaving  $c$ , 1 leaving  $os$ , and 3 leaving  $f$ .

## Questions

- How realistic is this graph view of a heap?
- Once a node is created, will it have to be stored until the end of the program execution?

# Memory Management

- $V = V_{useful} \cup V_{useless}$
- Is there an algorithm to compute  $V_{useful}$  and  $V_{useless}$ ?
- No, undecidable! :-)
- Idea: Approximate  $V_{useful}$  and  $V_{useless}$  by
$$V_{live} \supseteq V_{useful}$$
$$V_{dead} \subseteq V_{useless}$$

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## Implementing the Heap

```
static int HEAPBOTTOM = 0;          // smallest heap address
static int HEAPSIZe = 1000000;     // size of heap is fixed
static int[] HEAP = new int[HEAPSIZe];
```

## Example of Node

Stack frame (*os*, 400, *e*)

```
HEAP[120] = .... // write book keeping information
...
HEAP[124] = .... // write book keeping information
HEAP[125] = 100; // save address of operand stack
HEAP[126] = 400; // save pc
HEAP[127] = 110; // save address of environment
```

## Mutator Operations

```
int newnode(int size);  
void update(int v, int f, int w);
```

## 1 Heap Memory

## 2 Heap Management Techniques

- Reference Counting
- Mark-Sweep Garbage Collection
- Copying Garbage Collection
- Background

## Reference Counting

$$V_{dead} = \{w \in V \mid \text{there is no } f \in L, v \in V, \text{ s.t. } (v, f, w) \in E\}$$

Every update operation identifies all new elements of  $V_{dead}$  and makes them available for future *newnode* operations.

## Freelist for Keeping Track of Free Memory

```
static int NEXT = 1; // field 1 keeps the next pointer
static int RC = 1;   // field 1 keeps the reference count
static int Freelist = HEAPBOTTOM;
int current = HEAPBOTTOM;
while (current+NODESIZE < heapsize) {
    heap[current+NEXT] = current+NODESIZE;
    current = current + NODESIZE;
}
heap[current+NEXT] = NIL;
```

## Allocating a New Node

```
int allocate() {
    int newnode = freelist;
    freelist = heap[freelist+next];
    return newnode;
}

int newnode() {
    if (freelist == NIL) abort("Memory exhausted");
    int newnode = allocate();
    heap[newnode+RC] = 1;
    return newnode;
}
```

## Updating an Edge

```
void free(int n) {
    heap[n+NEXT] = freelist;
    freelist = n;
}

void delete(int n) {
    heap[n+RC] = heap[n+RC] - 1;
    if (heap[n+RC] == 0) {
        for c in children(n) do delete(heap[n+c]);
        free(n);
    }
}

void update(int v,int f,int w) {
    delete(heap[v+f]);
    heap[w+RC] = heap[w+RC] + 1;
    heap[v+f] = w;
}
```

# Advantages of Reference Counting

- Incrementality
- Locality
- Immediate reuse

## Disadvantages of Reference Counting

- Runtime overhead
- Cannot reclaim cyclic data structures

# Garbage Collectors

When `newnode()` runs out of memory, a garbage collector computes a set  $V_{dead}$  and reclaims the memory its elements were occupying.

`update()` not affected by GC:

```
void update(int v,int f,int w) {  
    heap[v+f] = w;  
}
```

# Mark-Sweep

```
int newnode() {  
    if (freelist == NIL) mark_sweep();  
    int newnode = allocate();  
    return newnode;  
}
```

# Liveness

$$\exists f.(v_1, f, v_2) \in E$$

---


$$v_1 \longrightarrow v_2$$

---


$$v \longrightarrow^* v$$

$$v_1 \longrightarrow v_2$$

---


$$v_1 \longrightarrow^* v_2$$

$$v_1 \longrightarrow^* v_2$$

$$v_2 \longrightarrow^* v_3$$

---


$$v_1 \longrightarrow^* v_3$$

## Liveness (continued)

The set  $V_{live}$  of a machine in state  $(os, pc, e, rs, (V, E))$  is now defined as follows:

$$V_{live} = \{v \in V \mid r \longrightarrow^* v, \text{ where } r \in \{os, e, rs\}\}$$

$\{os, e, rs\}$  are called roots.

## Idea

Visit all nodes in  $V_{live}$  and MARK them.

Visit every node in the heap and free every UNMARKED node.

# Mark-Sweep

```
void mark_sweep() {
    for r in Roots
        mark(r);
    sweep();
    if (Freelist == NIL) abort("memory exhausted");
}

void mark(v) {
    if (HEAP[v+MARKBIT] == UNMARKED) {
        HEAP[v+MARKBIT] = MARKED;
        for (int c = FIRSTCHILD, c <= LASTCHILD, c++) {
            mark(HEAP[v+c]);
        }
    }
}
```

## Mark-Sweep (continued)

```
void sweep() {
    int v = HEAPBOTTOM;
    while (v < HEAPTOP) {
        if (HEAP[v+MARKBIT] == UNMARKED) free(v);
        else HEAP[v+MARKBIT] = UNMARKED;
        v = v + NODESIZE;
    }
}
```

## Performance

$$e_{MS} = \frac{m_{MS}}{t_{MS}}$$

$m_{MS}$ : amount of reclaimed memory

$t_{MS}$ : time taken

$M = |V| = \text{HEAPSIZE}/\text{NODESIZE}$ .

$R$ : the number of live nodes.

$r = R/M$ : residency

## Performance (continued)

$$m_{MS} = M - R$$

$$t_{MS} = a \cdot R + b \cdot M$$

$$e_{MS} = \frac{m_{MS}}{t_{MS}} = \frac{M - R}{aR + bM} = \frac{1 - r}{ar + b}$$

## Idea

- Use only half of the available memory for allocating nodes
- Once this half is filled up, copy the live memory contained in the first half to the second half
- Reverse the roles of the halves and continue.

## Initialization

```
void init() {  
    Tospace = HEAPBOTTOM;  
    SPACESIZE = HEAPSIZ / 2;  
    Topospace = Tospace + SPACESIZE - 1;  
    Fromspace = Topospace + 1;  
    Free = Tospace;  
}
```

## Allocating New Nodes

```
int newnode() {
    if (Free + NODESIZE > Topofspace)
        flip();
    if (Free + NODESIZE > Topofspace)
        abort("memory exhausted");
    int newnode = Free;
    Free = Free + NODESIZE;
    return newnode;
}
```

# Cheney's Algorithm

```
void flip() {
    int temp = Fromspace;
    Fromspace = Tospace; Tospace = temp;
    Topofspace = Tospace + SPACESIZE - 1;
    int scan = Tospace; Free = Tospace;
    for r in Roots
        r = copy(r);
    while (scan < Free) {
        for (int c = FIRSTCHILD, c <= LASTCHILD, c++) {
            HEAP[scan+c] = copy(HEAP[scan+c]);
            scan = scan + NODESIZE;
        }
    }
}
```

# Cheney's Algorithm (continued)

```
int copy(v) {
    if (moved_already(v))
        return HEAP[v+FORWARDINGADDRESS];
    else {
        int addr = free
        move(v,free);
        free = free + NODESIZE;
        HEAP[v+FORWARDINGADDRESS] = addr;
        return addr;
    }
}
```

# Performance

$$m_{Copy} = \frac{M}{2} - R$$

$$t_{Copy} = c \cdot R$$

$$e_{Copy} = \frac{m_{Copy}}{t_{Copy}} = \frac{\frac{M}{2} - R}{cR} = \frac{1}{2cr} - \frac{1}{c}$$

## Historical Background

- Pioneered by LISP implementations
- Reference counting: Gelernter et al 1960, Collins 1960, used in Smalltalk, and Modula-2+
- Mark-sweep: McCarthy 1960, widely used, e.g. JVM
- Minsky 1963, Cheney 1970, widely used in functional and logic programming

## Explicit Heap Deallocation

```
var p : ^t
```

```
p := nil
```

```
new(p)
```

```
dispose(p)
```

# Space Leak

```
new(p);  
p := nil
```

# Dangling Reference

```
a.s := p;  
dispose(p)
```

# Memory Management in Software Systems

Space leaks can occur even in systems with automatic memory management.

Large systems implement their own memory management (Unix, Adobe Photoshop).

## Next Lecture

- The language rePL—Adding data structures to simPL
- Denotational semantics
- Pass-by-name and pass-by-need