# Verification of Real Time Systems - CS5270 lecture 10

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## Outline



- Assignment 3
- The road map...

# Model checking CTL example (smv/nusmv LTL model checker - spin

- 3 Timed CTL model checking
  - Regional transition systems...
  - Timed CTL-
  - The modelling relation  $\models_{ au}$  for timed CTL-



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## Outline



- Assignment 3
- The road map...

## 2 Model checking

- CTL example (smv/nusmv)
- LTL model checker spin

## Timed CTL model checking

- Regional transition systems...
- Timed CTL-
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Image: A matrix

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Assignment 3 The road map...

# Outline



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# Assignment 3

Assignment 3 The road map...

## A reminder... Assignment number 3:

- On the web site
- Due 9th April! ...



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Assignment 3 The road map...

# Outline



- Assignment 3
- The road map...
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Assignment 3 The road map...

# The immediate road map

### The topics:

- Preliminaries for Model Checking
  - Temporal logic..., Kripke semantics
- CTL Model Checking
  - The CTL model checking relation
  - The CTL model checking algorithm, with optimizations
  - Example smv/spin CTL/LTL model checkers

## • TCTL Model Checking

- The TCTL model checking relation
- The TCTL model checking algorithm, with optimizations
- Example Uupaal TCTL model checker



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CTL example (smv/nusmv) LTL model checker - spin

## Outline

Administration

 Assignment 3
 The road map...

 Model checking

 CTL example (smv/nusmv)
 LTL model checker - spin

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CTL example (smv/nusmv) LTL model checker - spin

## The smv model checker

#### CTL model checker:

- McMillan (1992) wrote smv a CTL model checker, making sources public
- More recently, NuSMV is being developed further, and now includes LTL, and other extensions including SAT solvers, BMC...
- Now has an extensive history



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CTL example (smv/nusmv) LTL model checker - spin

## The smv model checker

## 10<sup>2</sup>00 states and beyond!

- The tool smv has been particularly useful for hardware design checking, although it is similar to all the other style systems we have seen
- specifying a model in an automata style
- useful for any responsive software system (protocols)
- For a change give a hardware verification example
  - electronic circuit to detect the START condition for I2C signalling.

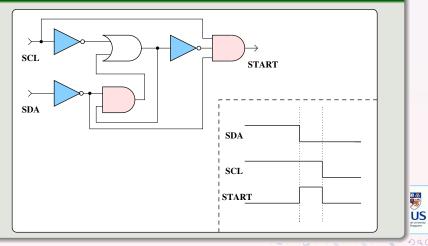
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CTL example (smv/nusmv) LTL model checker - spin

## Example: smv model checker

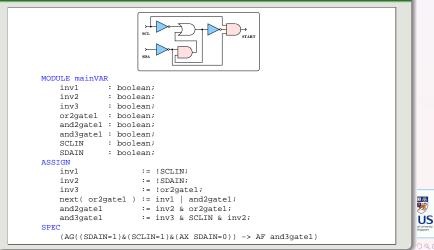
## If SDA goes low while SCL is high...



CTL example (smv/nusmv) LTL model checker - spin

## Example: smv model checker

## SMV code for the circuit:



CTL example (smv/nusmv) LTL model checker - spin

## Example: smv model checker

#### When we try it out:

```
[hugh@pp176-44 FormalVerification]$ NUSWV 12C
*** Fins is NUSMV 2.3.1 (compiled on Mon Apr 3 10:11:22 UTC 2006)
*** For more information on NUSMV see <http://nusmv.irst.itc.it>
*** or email to <nusmv-users@irst.itc.it>.
*** Please report bugs to <nusmv@irst.itc.it>.
- specification
    (AG ((SDAIN = 1 & SCLIN = 1) & AX SDAIN = 0) -> AF and3gatel)
    is true
lugn@pnp176-44 FormalVerification]$
```

 Verifies that it is always true that if SDA and SCL were both HIGH, and that if the next state had SDA LOW, then eventually and3gate=START will be HIGH?



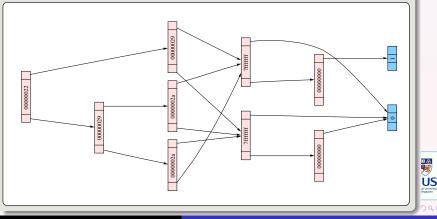
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CTL example (smv/nusmv) LTL model checker - spin

## Example: smv model checker

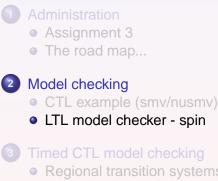
**ROBDD** representation of model:

• Generated automatically from within smv...



CTL example (smv/nusmv) LTL model checker - spin

## Outline



- Timed CTL-
- The modelling relation  $\models_{\tau}$  for timed CTL-



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CTL example (smv/nusmv) LTL model checker - spin

## The spin model checker

### LTL style:

- spin is the name of an LTL model checker
- xspin is a graphical interface for it
- PROMELA is the model checking language it uses.
- Developed by Gerard Holzmann at Bell Labs at

http://www.spinroot.com/

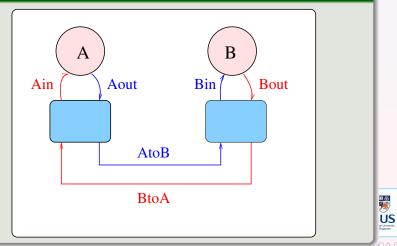


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CTL example (smv/nusmv) LTL model checker - spin

# Modelling protocols

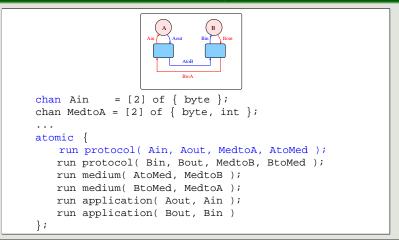
## Modelling the whole system:



CTL example (smv/nusmv) LTL model checker - spin

## Modelling protocols

#### PROMELA code to connect whole system:

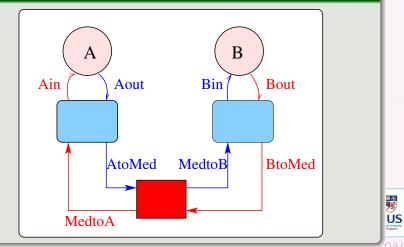


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CTL example (smv/nusmv) LTL model checker - spin

# Modelling protocols

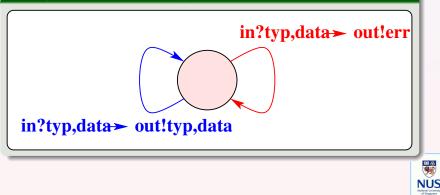
## System with a noisy channel:



CTL example (smv/nusmv) LTL model checker - spin

## Modelling protocols

#### A noisy channel transition system:

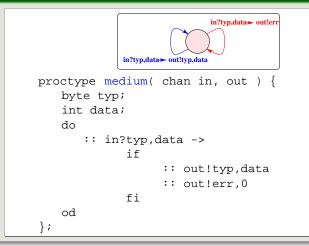


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CTL example (smv/nusmv) LTL model checker - spin

# Modelling protocols

## PROMELA code for noisy channel transition system:



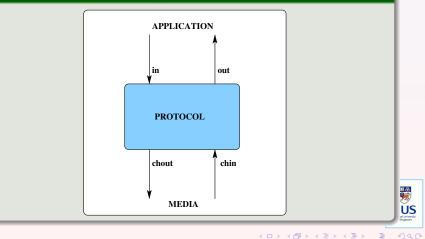
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CTL example (smv/nusmv) LTL model checker - spin

## Modelling protocols

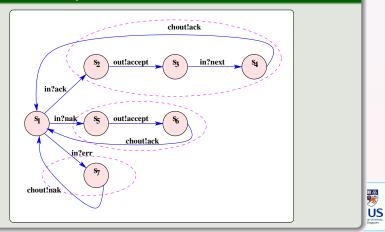
## Protocol lies between the application and the media:



CTL example (smv/nusmv) LTL model checker - spin

# Modelling protocols

#### Protocol transition system:



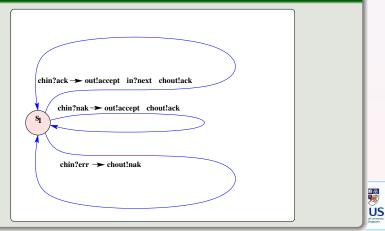
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CTL example (smv/nusmv) LTL model checker - spin

# Modelling protocols

#### Simplified protocol transition system:



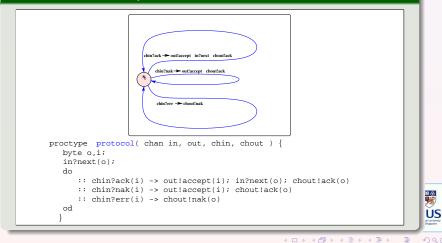
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CTL example (smv/nusmv) LTL model checker - spin

## Modelling protocols

#### PROMELA code for protocol:



CTL example (smv/nusmv) LTL model checker - spin

# Specifying properties?

#### For reachability and temporal claims:

 Add assertions in the PROMELA code for reachability claims:

assert(maxbuffered=3);

 Convert LTL formula into Buchi automata for (negative) temporal claims?

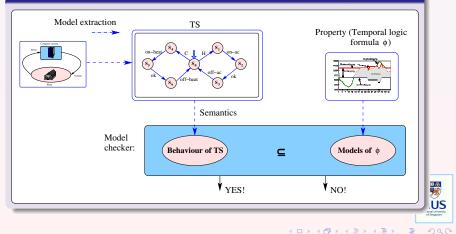


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CTL example (smv/nusmv) LTL model checker - spin

# The big picture again.....

## Models, properties, LANGUAGE of a model, property:



CTL example (smv/nusmv) LTL model checker - spin

# The big picture

#### Model theoretic view:

- To assert an LTL temporal formula/claim on a model, we have to show that the language of the model (all executions) is included in the language of the claim.
- It is easier to claim the negative ...
  - It is easier to prove that the intersection of the language of the model and the claim is empty.
  - Hence NEVER claims in PROMELA.

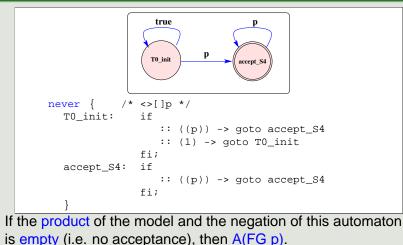


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CTL example (smv/nusmv) LTL model checker - spin

# Modelling claims: A(FG p) ... spin -f "<>[]p"

## PROMELA code for NEVER claim:



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Regional transition systems... Timed CTL-The modelling relation  $\models_{\tau}$  for timed CTL-

# Outline

- Administration
  Assignment 3
  The road map.
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   CTL example (smv/nusmv)
   LTL model checker spin
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Regional transition systems... Timed CTL-The modelling relation  $\models_{\tau}$  for timed CTL-

# Regional transition system

#### Timed CTL versus traditional CTL:

- Major difference is that we have clocks:
  - in the automaton (X, a finite set of clock variables), and
  - in the TCTL formula (Z, a different finite set of clock variables).

We have to take these clocks into account both in the definition of TCTL, and also the model checking relation for TCTL:  $\models_{\tau}$ . The Kripke structure is different, as it corresponds to an RTS (regional transition system) instead of a standard transition system.

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## Regional transition system

## The Kripke structure for RTS:

The (composite) states of the RTS are a pair r
 = (s, [v]<sub>≈</sub>), termed a region, where s corresponds to the original state of the transition system, and [v]<sub>≈</sub> is the regional equivalence class for v as defined in Chapter 4.

We begin by formally defining an RTS, and its corresponding model, in terms of the time abstract transition system  $TA_{TTS}$ . Recall that the (possibly infinite) states in  $TA_{TTS}$  are of the *composite* form (*s*, *v*), where *s* corresponds to the states of the original timed transition system, and *v* is a valuation of the clocks of that syste.

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## Regional transition system

#### Formal definition of RTS:

Given  $TA_{TTS} = (S, S_0, Act, \rightsquigarrow)$ , then the RTS is a quotiented transition system  $RTS = (\overline{R}, \overline{R}_0, Act, \rightarrow)$  where

$$\overline{R} = \{ (s, [v]_{\approx}) \mid (s, v) \in S \land v \in [v]_{\approx} \}, \text{ and} \overline{R}_0 = \{ (s, [v]_{\approx}) \mid (s, v) \in S_0 \land v \in [v]_{\approx} \},$$

and  $(s, [v]_{\approx}) \xrightarrow{a} (s', [v']_{\approx})$  if and only if there is a transition  $(s, v) \xrightarrow{a} (s', v')$  in TA<sub>TTS</sub>.



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## Regional transition system

### Notations when discussing RTS:

There are three levels:

- The elements of the set  $\overline{R}$  are called the *regions* of the RTS.
- 2 The notation for identifying a particular region will be  $\overline{r} \in \overline{R}$ , and
- 3 a (transitory) state with a particular clock valuation within that region will be denoted by r = (s, v).

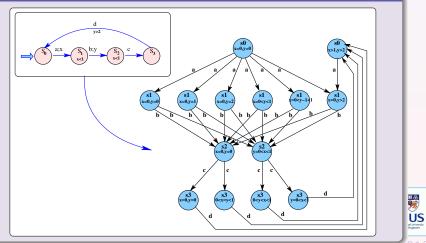


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# Regional transition system

#### From TTS to RTS:



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## Regional transition system

#### RTS is finite (reminder):

- Note that since ≡<sub>REG</sub> is a stable equivalence relation of finite index, the RTS is a finite structure.
- We do not need to differentiate between the RTS and the zone based transition system here, instead considering that the zone based transition system is just a more efficient version of the RTS.

The semantics for TCTL is again defined in terms of a Kripke structure or TCTL-model. This model is derived from the RTS.

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## Regional transition system

#### Definition for the model:

A TCTL model  $\overline{M}$  over a set AP of atomic propositions is a 4-tuple ( $\overline{R}, \Delta, AP, \mathcal{L}$ ), where

- $\overline{R}$  is the finite set of **regions** derived from the RTS.
- $\Delta \subseteq \overline{R} \times \overline{R}$  is a **transition relation** derived from  $\rightarrow$  in RTS. It must be *total.*
- AP is a finite set of atomic propositions.
- $\mathcal{L}: \overline{R} \to 2^{AP}$  is a function which **labels** each region with the set of atomic propositions true in that region.



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Regional transition systems... Timed CTL-The modelling relation  $\models_{\tau}$  for timed CTL-

# Timed CTL-

#### Definition:

Given a proposition  $p \in AP$  (atomic propositions),  $x \in X$  (clock variables),  $z \in Z$  (clock variables in the property formula) and  $\phi \in \Phi(X \cup Z)$  (clock constraints), then p and  $\phi$  are both TCTL-formulæ, and if  $\psi_1$  and  $\psi_2$  are TCTL- formulæ, then

- $\neg \psi_1$  is a TCTL- formula
- $\psi_1 \wedge \psi_2$  is a TCTL- formula
- $\psi_1 \lor \psi_2$  is a TCTL- formula
- $z in \psi_1$  is a TCTL- formula
- $A(\psi_1 U \psi_2)$  is a TCTL- formula
- $E(\psi_1 U \psi_2)$  is a TCTL- formula

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Regional transition systems... Timed CTL-The modelling relation  $\models_{\tau}$  for timed CTL-

# Timed CTL-

### How time is handled in timed CTL-:

- The FREEZE definition in line 4. The meaning of "z in ψ" is that ψ holds when the property formula clock z is reset to 0. Corresponds to the clock reset.
- Temporal operators are subscripted with time constraints:

## $\mathrm{A}(\psi_{\mathsf{1}}\,\mathrm{U}_{\leq\mathsf{5}}\,\psi_{\mathsf{2}})$

expresses the idea that  $\psi_1$  holds until within 5 time units,  $\psi_2$  becomes true. This may be defined in TCTL- using the FREEZE operator:

### z in A(( $\psi_1 \wedge z \leq 5$ ) U $\psi_2$ )

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# Timed CTL-

#### How time is handled in timed CTL-:

• Example 1:

### A(alarm $U_{<7}$ boileroff)

expresses the idea that the alarm is on until (within 7 time units) the boileroff is signaled.

• Example 2:

### $EF_{<7}(alarm)$

expresses the idea that the alarm will be on within 7 time units.

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Regional transition systems... Timed CTL-The modelling relation  $\models_{\tau}$  for timed CTL-

# Timed CTL- $\models_{\tau}$ relation

#### Definition:

 $\overline{M}, (r, f) \models_{\tau} p \qquad \Leftrightarrow$  $\overline{M}, (r, f) \models_{\tau} \phi \qquad \Leftrightarrow$  $\overline{M}, (r, f) \models_{\tau} \neg \psi_1 \qquad \Leftrightarrow$  $\overline{M}, (r, f) \models_{\tau} \psi_1 \land \psi_2 \qquad \Leftrightarrow$  $\overline{M}, (r, f) \models_{\tau} \psi_1 \lor \psi_2 \qquad \Leftrightarrow$  $\overline{M}, (r, f) \models_{\tau} z in \psi_1 \qquad \Leftrightarrow$  $\overline{M}, (r, f) \models_{\tau} A(\psi_1 U \psi_2) \qquad \Leftrightarrow$ 

 $\overline{M}, (r, f) \models_{\tau} E(\psi_1 U \psi_2) \quad \Leftrightarrow \quad$ 

- $p \in L(\overline{r})$   $v \cup f \models \phi$ iff it is not the case that  $\overline{M}, (r, f) \models_{\tau} \psi_1$ iff  $\overline{M}, (r, f) \models_{\tau} \psi_1$  and  $\overline{M}, (r, f) \models_{\tau} \psi_2$ iff  $\overline{M}, (r, f) \models_{\tau} \psi_1$  or  $\overline{M}, (r, f) \models_{\tau} \psi_2$
- $\inf \overline{M}, (r, z \inf f) \models_{\tau} \psi_1$
- iff for every path  $\overline{\pi} = s_0 \ s_1 \ \dots$  from *r*, where for some  $j, \overline{M}, \overline{\pi}(j) \models_{\tau} \psi_2$ , and  $\forall i < j, \overline{M}, \overline{\pi}(i) \models_{\tau} \psi_1 \lor \psi_2$
- iff there is a path  $\overline{\pi} = s_0 \ s_1 \ \dots$  from *r*, where for some *j*,  $\overline{M}, \overline{\pi}(j) \models_{\tau} \psi_2$ , and  $\forall i < j, \overline{M}, \overline{\pi}(i) \models_{\tau} \psi_1 \lor \psi_2$

Regional transition systems... Timed CTL-The modelling relation  $\models_{\tau}$  for timed CTL-

# The modelling relation $\models_{\tau}$

#### Comments on the relation:

- In this definition, the progression of time is defined in reference to the states of the original TS<sub>TTS</sub>. In particular, a path from one state *r* is an infinite sequence of states *π* = s<sub>0</sub> s<sub>1</sub> ... such that s<sub>0</sub> = *r* and s<sub>i</sub> → s<sub>i+1</sub>. A particular *i*-th element of *π* is *π*(*i*).
- The notation found in the definition for the FREEZE operator
   (*M*, (*r*, *z* in *f*) ⊨<sub>τ</sub> ψ<sub>1</sub>) indicates that *M*, (*r*, *f*) ⊨<sub>τ</sub> ψ<sub>1</sub> if all
   occurences of *z* in *f* are reset to 0.



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# The modelling relation $\models_{\tau}$

#### Comments on the relation:

- An interesting element of the definition is found in the definitions for E(ψ<sub>1</sub> U ψ<sub>2</sub>) and A(ψ<sub>1</sub> U ψ<sub>2</sub>), where at some *j*, *M*, π(*j*) ⊨<sub>τ</sub> ψ<sub>2</sub>, but for all *i* < *j*, *M*, π(*i*) ⊨<sub>τ</sub> ψ<sub>1</sub> ∨ ψ<sub>2</sub>.
- If you compare this with the similar definition from CTL, you find in that case the condition "for all *i* < *j*, *M*, π(*i*) ⊨ ψ<sub>1</sub>" (i.e. ψ<sub>1</sub> instead of ψ<sub>1</sub> ∨ ψ<sub>2</sub>).

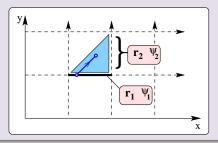


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# The modelling relation $\models_{\tau}$

#### Explanation:

We can see the need for the expression  $\psi_1 \vee \psi_2$  instead of just  $\psi_1$  by considering the *big* step from a particular valuation in  $\overline{r}_1$  to another in  $\overline{r}_2$  seen below. For all points in the two regions we want  $A(\psi_1 U \psi_2)$ , but for the two points connected by the line,  $\psi_1$  is not true just before the new point



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