$$U_k \in R^{m \times k}$$