

Example

$$Q = \{q_1, q_2\}$$

start state q_1

$$F = \{q_2\}.$$

$$\delta(q_1, 0) = q_1$$

$$\delta(q_1, 1) = q_2$$

$$\delta(q_2, 0) = q_2$$

$$\delta(q_2, 1) = q_2$$

$$R_{11}^0 = \epsilon + 0$$

$$R_{12}^0 = 1$$

$$R_{21}^0 = \emptyset$$

$$R_{22}^0 = \epsilon + 0 + 1$$

$$R_{11}^1 = R_{11}^0 + R_{11}^0(R_{11}^0)^*R_{11}^0 = (\epsilon + 0) + (\epsilon + 0)(\epsilon + 0)^*(\epsilon + 0) = (\epsilon + 0)^+ = 0^*$$

$$R_{12}^1 = R_{12}^0 + R_{11}^0(R_{11}^0)^*R_{12}^0 = 1 + (\epsilon + 0)(\epsilon + 0)^*1 = 0^*1$$

$$R_{21}^1 = R_{21}^0 + R_{21}^0(R_{11}^0)^*R_{11}^0 = \emptyset + \emptyset(\epsilon + 0)^*(\epsilon + 0) = \emptyset$$

$$R_{22}^1 = R_{22}^0 + R_{21}^0(R_{11}^0)^*R_{12}^0 = (\epsilon + 0 + 1) + \emptyset(\epsilon + 0)^*1 = \epsilon + 0 + 1.$$

$$R_{11}^2 = R_{11}^1 + R_{12}^1(R_{22}^1)^*R_{21}^1 = 0^* + 0^*1(\epsilon + 0 + 1)^*\emptyset = 0^*$$

$$R_{12}^2 = R_{12}^1 + R_{12}^1(R_{22}^1)^*R_{22}^1 = 0^*1 + 0^*1(\epsilon + 0 + 1)^*(\epsilon + 0 + 1) = 0^*1 + 0^*1(0 + 1)^* = 0^*1(0 + 1)^*.$$

$$R_{21}^2 = R_{21}^1 + R_{22}^1(R_{22}^1)^*R_{21}^1 = \emptyset + (\epsilon + 0 + 1)(\epsilon + 0 + 1)^*\emptyset = \emptyset$$

$$R_{22}^2 = R_{22}^1 + R_{22}^1(R_{22}^1)^*R_{22}^1 = (\epsilon + 0 + 1) + (\epsilon + 0 + 1)(\epsilon + 0 + 1)^*(\epsilon + 0 + 1) = (0 + 1)^*.$$