

CS5230 Tutorial 4

1. Show that $DTIME(2^{n^2})$ is a proper superset of $DSPACE(n)$.
2. Show that $DTIME(2^n)$ is a proper subset of $DTIME(2^n * \lceil (n)^{2/3} \rceil)$.
3. Show Gap theorem for deterministic space and non-deterministic time/space. Please try to do it as a corollary of theorems done in class, rather than re-proving it using the technique for gap theorem for time.
4. Suppose \mathbf{M} is a deterministic one-tape TM which accepts $\{wcw^R : w \in \{a, b\}^*\}$. Then show that \mathbf{M} is $\Omega(n^2)$ time bounded (Note that for time-bounded TMs, one-tape TM means that the only tape is the input tape, which is readable/writable). Here w^R denotes the reverse of string w .

Hint: Consider the behaviour of \mathbf{M} on inputs of the form $wa^mca^mw^R$, where w is of length m . Consider the crossing sequences of the machine in the portion a^mc . [Here, ignore the content of the tape, and just consider the states of the TM in the crossing sequence]. Divide in two appropriate cases based on whether for some w of length m the crossing sequence are all “large”.