# Midterm Examination 1 MA 3205: Set Theory 

15.09.2009, 12.00-12.45h

Matriculation Number:

## Rules

Each question contains as many marks as it has subquestion. Each correct subquestion gives 1 mark. The maximum score is 15 marks.

Question 1. Determine the following sets where $A=\{1,2,4,8,16\}$ and $B=$ $\{3,4,5,6,7,8\}$ :
(a) $A \cup B=\{$ $\qquad$
(b) $A \cap B=\{$ $\qquad$
(c) $A \Delta B=\{$


Here $\cup$ is the union, $\cap$ the intersection and $\Delta$ the symmetric difference.
Question 2. Let $A$ be the powerset of $\mathbb{N}$, that is, let $A$ be the set of all subsets of $\mathbb{N}$. Check the correct box for each set.
(a) The set $\{B \in A: \mathbb{N} \subseteq B\}$ isempty $\square$ finite and not emptycountableuncountable.
(b) The set $\{C \in A: C$ has 5 elements $\}$ is $\square$ empty $\square$ finite and not emptycountableuncountable.
(c) The set $\{D \in A: D$ is infinite $\}$ isempty finite and not emptycountableuncountable.

Question 3. (a) Is there a set $A$ such that $A$ has more elements then $\cup A$ ?No.
(b) Write a few lines to justify your answer (no complete proof needed, but it should make sense; only counted if (a) is correct).

Question 4. (a) Is there a set $B$ such that $B \neq \mathbb{N}, B$ is transitive and $B$ is inductive? $\square$ Yes; $\square$ No.
(b) Write a few lines to justify your answer (no complete proof needed, but it should make sense; only counted if (a) is correct).

Question 5. (a) Is there a set $C$ such that the power set $\mathcal{P}(C)$ of $C$ is countable? Yes; $\square$ No.
Here recall that the statement " $\mathcal{P}(C)$ is countable" implies that " $\mathcal{P}(C)$ is infinite". (b) Write a few lines to justify your answer (no complete proof needed, but it should make sense; only counted if (a) is correct).

Question 6. (a) Determine all sets $A$ which satisfy $\mathcal{P}(A) \subseteq\{\emptyset,\{\emptyset\},\{\{\emptyset\}\}\}$ :
(b) Determine all sets $B$ which satisfy $B \subseteq \mathbb{N}$ and $\forall n[n \in B \Leftrightarrow n+2 \in B]$ :
(c) How many sets $C \in \mathbb{N}$ have at most 5 elements?

$\square 2$
$\square 7$
$\square 3$
$\square 4$ infinitely many.

## Working Space

You can use this page to do calculations, but you should write the answers into the space provided. Answers found here are not evaluated.

