# Programming Language Concepts, CS2104 <br> Lecture 2 

Oz Syntax, Data structures

## Reminder of last lecture

- Oz, Mozart
- Concepts of
- Variable, Type, Cell
- Function, Recursion, Induction
- Correctness, Complexity
- Lazy Evaluation
- Higher-Order Programming
- Concurrency, Dataflow
- Object, Classes
- Nondeterminism, Interleaving, Atomicity


## Overview

- Programming language definition: syntax, semantics
- CFG, EBNF
- Data structures
- simple: integers, floats, literals
- compound: records, tuples, lists
- Kernel language
- linguistic abstraction
- data types
- variables and partial values
- statements and expressions (next lecture)


## Language Syntax

- Language = Syntax + Semantics
- The syntax of a language is concerned with the form of a program: how expressions, commands, declarations etc. are put together to result in the final program.
- The semantics of a language is concerned with the meaning of a program: how the programs behave when executed on computers.


## Programming Language Definition

- Syntax: grammatical structure
- Lexical: how words are formed
- Phrasal: how sentences are formed from words
- Semantics: meaning of programs
- Informal: English documents (e.g. reference manuals, language tutorials and FAQs etc.)
- Formal:
- Operational Semantics (execution on an abstract machine)
- Denotational Semantics (each construct defines a function)
- Axiomatic Semantics (each construct is defined by pre and post conditions)

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## Parse Trees $=$ Abstract Syntax Trees

```
fun {Fact N}
    if N == 0
    then
            1
    else
        N*{Fact N-1}
    end
end
```

- words are called tokens
- grammar rules describe both tokens and statements


## Language Syntax

- Token is sequence of characters
- Statement is sequence of tokens
- Lexical analyzer is a program
- recognizes character sequence
- produces token sequence
- Parser is a program
- recognizes a token sequence
- produces statement representation
- Statements are represented as parse trees

Lexical analyzer
tokens

## Parser

parse tree

## Language Syntax

## - Defines legal programs

- programs that can be executed by machine
- Defined by grammar rules
- define how to make 'sentences' out of 'words'
- For programming languages
- sentences are called statements (commands, expressions)


## Context-Free Grammars

- A context-free grammar (CFG) is:
- A set of terminal symbols T (tokens or constants)
- A set of non-terminal symbols N
- One (non-terminal) start symbol $\sigma$
- A set of grammar (rewriting) rules $\Omega$ of the form
<nonterminal> ::= <sequence of terminals and nonterminals〉
- Grammar rules (productions) can be used to
- verify that a statement is legal
- generate all possible statements
- The set of all possible statements generated by a grammar from the start symbol is called a (formal) language


## Context-Free Grammars (Example)

$$
\text { Let } \begin{aligned}
\mathrm{N} & =\{\langle\mathrm{a}\rangle\}, \quad \mathrm{T}=\{0,1\}, \quad \sigma=\langle\mathrm{a}\rangle \\
\Omega & =\{\langle\mathrm{a}\rangle::=11\langle\mathrm{a}\rangle 0,\langle\mathrm{a}\rangle::=110\}
\end{aligned}
$$



But $011 \notin \mathrm{~L}(\mathrm{G})$


011

These trees are called parse trees or syntax trees or derivation trees.

## Extended Backus－Naur Form

－EBNF is a more compact notation to define the syntax of programming languages．
－EBNF has the same power as CFG．
－Terminal symbol is a token．
－Nonterminal symbol is a sequence of tokens，and is represented by a grammar rule：

〈nonterminal ：：＝〈rule body〉
－As EBNF，（positive）integers may be defined as：
〈integer〉 ：：＝〈digit＞$\{$ 〈digitit $\}$
－〈integer〉 is defined as the sequence of a 〈digit〉 followed by zero or more 〈digit〉＇s

## Extended Backus－Naur Form Notations

| －$\left.{ }^{-1} \chi^{\prime}\right\rangle$ | nonterminal $x$ |
| :---: | :---: |
| －$\langle x\rangle$ ：$:=$ Body | $\langle x\rangle$ is defined by Body |
| －$\quad\langle x\rangle \mid\langle y\rangle$ | either $\langle x\rangle$ or $\langle y\rangle$（choice） |
| －$\langle x\rangle\langle y\rangle$ | the sequence $\langle x\rangle$ followed by $\langle y\rangle$ |
| －$\quad\{\langle x\rangle\}$ | sequence of zero or more |
|  | occurrences of $\langle x\rangle$ |
| －$\{\langle x\rangle\}^{+}$ | sequence of one or more |
|  | occurrences of $\langle x\rangle$ |
| －$[\langle x\rangle]$ | zero or one occurrence of $\langle x\rangle$ |

## Extended Backus－Naur Form Examples

－〈expression〉：：＝〈variable〉｜＜integer〉｜．．．

｜if 〈expression〉 then〈statement〉 \｛ elseif 〈expression〉 then 〈statement〉 \} ［ else 〈statement〉］end
｜．．．

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## Extended Backus－Naur Form Examples

－Description of（positive）real numbers：

"In '57, parsing expressions was not so easy"!


John Backus principal papers Backus-Naur form, Fortran

- Describing his early work on FORTRAN, Backus said:-
"We did not know what we wanted and how to do it. It just sort of grew. The first struggle was over what the language would look like. Then how to parse expressions - it was a big problem and what we did looks astonishingly clumsy now.... "
- Turing Award, 1977


## Data Structures (Values)

- Simple data structures
- integers

42, ~1, 0
~ means unary minus

- floating point
1.01, 3.14
- atoms atom, 'Atom', nil
- Compound data structures
- tuples: combining several values
- records: generalization of tuples
- lists: special cases of tuples

Tuples

```
X=state(1 a 2)
```



- Have a label
- e.g: state
- Combine several values (variables)
- e.g: 1, a, 2
- position is significant!

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Tuple Operations
$X=$ state (1 a 2)


- \{Label X\} returns label of tuple x
- here: state
- is an atom
- \{Width X$\}$ returns the width (number of fields)
- here:

3

- is a positive integer

Tuple Access (Dot)


- Fields are numbered from 1 to \{Width X$\}$
- x.n returns N -th field of tuple
- here, x. 1 returns 1
- here, x. 3 returns 2
- In x.n, N is called feature

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Tuples for Trees


- Trees can be constructed with tuples:

```
declare
    Y=s(1 2) Z=r(3 4)
    X=m(Y Z)
```


## Constructing Tuple Skeletons

- \{MakeTuple Label Width\}
- creates new tuple with label Label and width Width
- fields are initially unbound
- Access to fields then by "dot"


## Example Tuple Construction

- Created by execution of
declare

```
X = {MakeTuple a 3}
```



## Example Tuple Construction

- After execution of
$\mathrm{x} .2=\mathrm{b}$
$\mathrm{X} .3=\mathrm{c}$



## Records

- Records are generalizations of tuples
- features can be atoms
- features can be arbitrary integers
- not restricted to start with 1
- not restricted to be consecutive
- Records also have Label and width


## Records

- Position is insignificant
- Field access is as with tuples
X.a is 1

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## Tuples are Records

- Constructing
declare
X = state (1:a 2:b 3:c)
is equivalent to

```
X = state(a b c)
```


## A Way to Build Binary Trees

declare

```
Root=node(left:X1 right:X2 value:0)
X1=node(left:X3 right:X4 value:1)
X2=node(left:X5 right:X6 value:2)
X3=node(left:nil right:nil value:3)
X4=node(left:nil right:nil value:4)
X5=node(left:nil right:nil value:5)
X6=node(left:nil right:nil value:6)
{Browse Root}
proc {Preorder X}
    if X \= nil then {Browse X.value}
        if X.left \= nil then {Preorder X.left} end
        if X.right \= nil then {Preorder X.right} end
    end
end
{Preorder Root
```


## Lists

- A list contains a sequence of elements:
- is the empty list, or
- consists of a cons (or list pair) with head and tail
- head contains an element
- tail contains a list
- Lists are encoded with atoms and tuples
- empty list:
the atom nil
- cons:
tuple of width 2 with label '। '
- Special syntax for cons
$X=Y \mid Z$
instead of
$\mathrm{X}=$ '।' (Y Z)
Both are equivalent!

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## An Example List

- After execution of
declare
$\mathrm{X} 1=\mathrm{a}|\mathrm{X} 2 \quad \mathrm{X} 2=\mathrm{b}| \mathrm{X} 3 \quad \mathrm{X} 3=\mathrm{c} \mid$ nil



## Simple List Construction

- One can also write
$\mathrm{x} 1=\mathrm{a}|\mathrm{b}| \mathrm{c} \mid$ nil
which abbreviates
X1=a|(b|(c|nil)))
which abbreviates
X1= '|' (a '|' (b '|' (c nil)))
- Even shorter
$\mathrm{X} 1=[\mathrm{a}$ b c]

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## Computing With Lists

- Remember: a cons is a tuple!
- Access head of cons
X. 1
- Access tail of cons
X. 2
- Test whether list x is empty:

```
if X==nil then ... else ... end
```


## Head And Tail

- Define abstractions for lists

```
fun {Head Xs}
        Xs.1
    end
    fun {Tail Xs}
        Xs.2
end
- {Head [a b c]}
returns a
- {Tail [a b c]}
returns [b c]
■ {Head {Tail {Tail [a b c]}}}
returns c
```

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## How to Process Lists. General Method

- Lists are processed recursively
- base case: list is empty (nil)
- inductive case: list is cons
access head, access tail
- Powerful and convenient technique
- pattern matching
- matches patterns of values and provides access to fields of compound data structures

How to Process Lists. Example

- Input: list of integers
- Output: sum of its elements
- implement function Sum
- Inductive definition over list structure
- Sum of empty list is 0
- Sum of non-empty list L is

```
{Head L} + {Sum {Tail L}}
```

Sum of the Elements of a List using Conditional Construct

```
fun {Sum L}
    if L==nil
    then 0
    else {Head L} + {Sum {Tail L}}
    end
end
```

Sum of the Elements of a List using Pattern Matching

```
fun {Sum L}
    case L
    of nil then 0
    [] H|T then H +{Sum T}
    end
end
```

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Sum of the Elements of a List using Pattern Matching

```
fun {Sum L}
    case L
    of nil then 0
                                    Clause
    [] H|T then H +{Sum T}
    end
end
```

- nil is the pattern of the clause

Sum of the Elements of a List using Pattern Matching

```
fun {Sum L}
```

    case L
    of nil then 0
    [] H|T then H \(+\{\) Sum I \(\} \quad\) Clause
    end
    end

- HIT is the pattern of the clause


## Pattern Matching

- The first clause uses of, all other []
- Clauses are tried in textual order (left to right, top to bottom)
- A clause matches, if its pattern matches
- A pattern matches, if the width, label and features agree
- then, the variables in the pattern are assigned to the respective fields
- Case-statement executes with first matching clause


## Length of a List

- Inductive definition
- length of empty list is 0
- length of cons is $1+$ length of tail
fun \{Length Xs \}
case Xs
of nil then 0
[] X|Xr then $1+\{$ Length Xr\}
end
end


## General Pattern Matching

- Pattern matching can be used not only for lists!
- Any value, including numbers, atoms, tuples, records

```
fun {DigitToString X}
    case X
            of 0 then "Zero"
            [] 1 then "One"
            [] . . .
        end
    end
```


## Language Semantics

- Defines what a program does when executed
- Considerations:
- simplicity
- allow programmer to reason about program (correctness, execution time, and memory use)
- Practical language used to build complex systems (millions lines of code) must often be expressive.
- Solution : Kernel language approach for semantics


## Kernel Language Approach

- Define simple language (kernel language)
- Define its computation model
- how language constructs (statements) manipulate (create and transform) data structures
- Define mapping scheme (translation) of full programming language into kernel language
- Two kinds of translations
- linguistic abstractions
- syntactic sugar


## Kernel Language Approach



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## Linguistic Abstractions $\Leftrightarrow$ Syntactic Sugar

- Linguistic abstractions provide higher level concepts
- programmer uses to model and reason about programs (systems)
- examples: functions (fun), iterations (for), classes and objects (class)
- Functions (calls) are translated to procedures (calls). This eliminates a redundant construct from the semantics viewpoint.

Linguistic Abstractions $\Leftrightarrow$ Syntactic Sugar

- Linguistic abstractions: provide higher level concepts
- Syntactic sugar: short cuts and conveniences to improve readability
if $\mathrm{N}=1$ then [1]
else
local Lin
..
end
if $\mathrm{N}=1$ then [1]
else Lin
end


## Approaches to Semantics



## Sequential Declarative Computation Model

- Single assignment store
- declarative (dataflow) variables and values (together called entities)
- values and their types
- Kernel language syntax
- Environment
- maps textual variable names (variable identifiers) into entities in the store
- Execution of kernel language statements
- execution stack of statements (defines control)
- store
- transforms store by sequence of steps

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## Single Assignment Store

- Single assignment store is store (set) of variables
- Initially variables are unbound
- Example: store with three variables, $x_{1}, x_{2}$, and $x_{3}$

Store
$x_{1}$
unbound
$x_{2}$
unbound
$x_{3}$
unbound

## Single Assignment Store

- Variables in store may be bound to values
- Example:
- $x_{1}$ is bound to integer 314
- $x_{2}$ is bound to list [12 3]
- $x_{3}$ is still unbound



## Value Expressions in the Kernel Language

```
<v\rangle ::= <number\rangle | <record\rangle| <procedure\rangle
\langlenumber\rangle ::= <int> | \langlefloat\rangle
\langlerecord\rangle, \langlepattern\rangle ::= <literal>|
            <literal\rangle (\langlefeature }\mp@subsup{}{1}{}\rangle:\langle\mp@subsup{x}{1}{}\rangle...\langle\mp@subsup{\mathrm{ feature }}{n}{}\rangle:\langle\mp@subsup{x}{n}{}\rangle
<literal\rangle ::=\langleatom\rangle \ <bool\rangle
\langlefeature\rangle ::=\langleint\rangle|\langleatom\rangle|\langlebool\rangle
\langlebool> ::= true | false
<procedure\rangle::= proc {$\langle\mp@subsup{y}{1}{}\rangle\ldots\langle\mp@subsup{y}{n}{\prime}\rangle}\langles\rangle\mathrm{ end}
```


## Statements and Expressions

- Expressions describe computations that return a value
- Statements just describe computations
- Transforms the state of a store (single assignment)
- Kernel language
- Expressions allowed: value construction for primitive data types
- Otherwise statements


## Variable Identifiers

- $\langle x\rangle,\langle y\rangle,\langle z\rangle$ stand for variables identifiers
- Concrete kernel language variables identifiers
- begin with an upper-case letter
- followed by (possibly empty) sequence of alphanumeric characters or underscore
- Any sequence of characters within backquotes
- Examples:
- X, Y1
- Hello_World
- 'hello this is a $\$ 5$ bill' (backquote)


## Values and Types

- Data type
- set of values
- set of associated operations
- Example: Int is data type "Integer"
- set of all integer values
- 1 is of type Int
- has set of operations including +, -, *, div, etc
- Model comes with a set of basic types
- Programs can define other types
- for example: abstract data types - ADT (<Stack T> is an ADT with elements of type T and 4 operations. Type T can be anything, and the operations must satisfy certain laws, but they can have any particular implementation - Section 3.7)

Data Types


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## Kernel's Primitive Data Types



## Numbers

- Number: either Integer or Float
- Integers:
- Decimal base:
- 314, 0, ~10 (minus 10)
- Hexadecimal base:
- 0xA4 (164 in decimal base)
- 0X1Ad (429 in decimal base)
- Binary base:
- 0b1101 (13 in decimal base)
- 0B11 (3 in decimal base)
- Floats:
- $1.0,3.4,2.34 \mathrm{e} 2, \sim 3.52 \mathrm{E} \sim 3\left(\sim 3.52 \times 10^{-3}\right)$


## Literals: Atoms and Booleans

- Literal: atom or boolean
- Atom (symbolic constant):
- A sequence starting with a lower-case character followed by characters or digits: person, peter
- Any sequence of printable characters enclosed in single quotes:' I am an atom','Me too'
- Note: backquotes are used for variable identifier ( 'John Doe ')
- Booleans:

[^1]
## Records

- Compound data-structures
$\left\langle\lambda\left(\left\langle f_{1}\right\rangle:\left\langle x_{1}\right\rangle \ldots\left\langle f_{n}\right\rangle:\left\langle x_{n}\right\rangle\right)\right.$
- the label: $\rangle$ is a literal
the features: $\left\langle f_{1}\right\rangle, \ldots,\left\langle f_{n}\right\rangle$ can be atoms, integers, or booleans
the variable identifiers: $\left\langle x_{1}\right\rangle, \ldots,\left\langle x_{n}\right\rangle$
- Examples:
person (age:X1 name:X2)
person(1:X1 2:X2)
'।' (1:H 2:T) \% no space after '|'
nil
person
An atom is a record without features!

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## Syntactic Sugar

- Tuples
$\left.\langle\lambda\rangle\left\langle x_{1}\right\rangle \ldots\left\langle x_{n}\right\rangle\right) \quad$ (tuple)
equivalent to record
$\left\langle\lambda\left(1:\left\langle x_{1}\right\rangle \ldots n:\left\langle x_{n}\right\rangle\right)\right.$
- Lists 'l' ( $\langle h d\rangle\langle t\rangle)$
- A string:
- a list of character codes:
$\left[\begin{array}{llllllllll}87 & 101 & 32 & 108 & 105 & 107 & 101 & 32 & 79 & 122\end{array} 46\right]$
- can be written with double quotes: "We like oz."


## Operations on Basic Types

- Numbers
- floats: +, -, *, /
a integers: +, -, *, div, mod
- Records
- Arity, Label, Width, and "."
- $\mathrm{X}=$ person (name:"George" age:25)
- $\{$ Arity $X\}$ returns [age name]
- \{Label X\} returns person
- X. age returns 25
- Comparisons (integers, floats, and atoms)
- equality:
$==, \quad \backslash=$
a order: $\quad=<, \quad<, \quad>=$

Variable-Variable Equality (Unification)

- It is a special case of unification
- Example: constructing graphs
declare
Y Z
$X=a\left(\begin{array}{ll}Y & Z\end{array}\right)$



## Variable-Variable Equality (Unification)

- Now bind z to x

Z $=\mathrm{X}$

- Possible due to deferred assignment


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## Variable-Variable Equality (Unification)

- Consider $\mathrm{x}=\mathrm{Y}$ when both x and Y are bound
- Case one: no variables involved
- If the graphs starting from the nodes of $X$ and $Y$ have the same structure, then do nothing (also called structure equality).
- If the two terms cannot be made equal, then an exception is raised.
- Case two: x or y refer to partial values
- the respective variables are bound to make $X$ and $Y$ the "same"


## Case One: no Variables Involved

- This is not unification, because there will no binding.
- declare
$X=r\left(\begin{array}{ll}a & b\end{array}\right) \quad Y=r(a b)$
$X=Y$ \% passes silently
- declare
$X=r\left(\begin{array}{ll}a & b\end{array}\right) \quad Y=r\left(\begin{array}{ll}a & c\end{array}\right)$
$X=Y$ \% raises an failure error
- Failure errors are exceptions which should be caught.

Case two: x or y refers to partial values

- Unification is used because of partial values.
- declare
$r\left(\begin{array}{ll}X & Y\end{array}\right)=r\left(\begin{array}{ll}1 & 2\end{array}\right)$
-X is bound to 1 , Y is bound to 2
- declare U Z

$$
\begin{aligned}
& X=\text { name }\left(\begin{array}{ll}
a & U
\end{array}\right) \\
& Y=\text { name }\left(\begin{array}{ll}
Z & b
\end{array}\right) \\
& X=Y
\end{aligned}
$$

- U is bound to $\mathrm{b}, \mathrm{z}$ is bound to a

Case two: x or y refers to partial values

- declare

X=r(name:full(Given Family) age:22)
$\mathrm{Y}=\mathrm{r}$ (name: full(claudia Johnson) age:A)
$X=Y$ \% Given=claudia, $A=22$, Johnson=Family

- declare
$X=r(a \quad X) \quad Y=r(a r(a Y))$
$X=Y$ \% this is fine
- Both $X, Y$ are $r(\operatorname{ar}(\operatorname{ar}(a \ldots))) \% a d$ infinitum

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## Unification

- unify $(x, y)$ is the operation that unifies two partial values $x$ and $y$ in the store
- Store is a set $\{x 1, \ldots, x k\}$ partitioned as follows:
- Sets of unbound variables that are equal (also called equivalence sets of variables).
- Variables bound to a number, record, or procedure (also called determined variables).
- Example: $\{x 1=$ name (a: $x 2$ ) , $x 2=x 9=73$,

$$
x 3=x 4=x 5, \quad x 6, \quad x 7=x 8\}
$$

## Unification. The primitive bind

## operation

- bind $(E S,\langle v\rangle)$ binds all variables in the equivalence set $E S$ to <v>.
- Example: bind (\{x7, $x 8\}$, name (a: $x 2$ ))
$-\operatorname{bind}\left(E S_{1}, E S_{2}\right)$ merges the equivalence set $E S_{1}$ with the equivalence set $E S_{2}$.
- Example: bind( $\{x 3, x 4, x 5\},\{x 6\})$


## The Unification Algorithm: unify ( $\mathrm{x}, \mathrm{y}$ )

1. If $x$ is in $E S_{x}$ and $y$ is in $E S_{y}$, then do bind $\left(E S_{x}, E S_{y}\right)$.
2. If $x$ is in $E S_{x}$ and $y$ is determined, then do $\operatorname{bind}\left(E S_{x}, y\right)$.
3. If $y$ is in $E S_{y}$ and $x$ is determined, then do bind $\left(E S_{y}, x\right)$.
4. If
5. $x$ is bound to $\left(l_{1}: x_{1}, \ldots, l_{n}: x_{n}\right)$ and $y$ is bound to $l^{\prime}\left(l_{1}^{\prime}: y_{1}, \ldots, l_{m}^{\prime}: y_{m}\right)$ with $I \neq l$ ' or
6. $\left\{l_{1}, \ldots, l_{n}\right\} \neq\left\{l_{1}^{\prime}, \ldots, l_{m}^{\prime}\right\}$,
then raise a failure exception.
7. If $x$ is bound to $l\left(l_{1}: x_{1}, \ldots, I_{n}: x_{n}\right)$ and $y$ is bound to $l\left(I_{1}: y_{1}, \ldots, I_{n}: y_{n}\right)$, then for $i$ from 1 to $n$ do unify $\left(x_{i}, y_{i}\right)$.

## Handling Cycles

- The above algorithm does not handle unification of partial values with cycles.
- Example:
- The store contains $x=\mathrm{f}(\mathrm{a}: x)$ and $y=\mathrm{f}(\mathrm{a}: y)$.
- Calling unify $(x, y)$ results in the recursive call unify $(x, y), \ldots$
- The algorithm loops forever!
- However $x$ and $y$ have exactly the same structure!

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## The New Unification Algorithm: unify'( $\mathrm{x}, \mathrm{y}$ )

- Let $M$ be an empty table (initially) to be used for memoization.
- Call unify ${ }^{\prime}(x, y)$.
- Where unify ${ }^{\prime}(x, y)$ is:
- If $(x, y) \in M$, then we are done.
- Otherwise, insert ( $x, y$ ) in $M$ and then do the original algorithm for unify $(x, y)$, in which the recursive calls to unify are replaced by calls to unify'.


## Displaying cyclic structures

```
declare X
X = '|'(a '|'(b X)) % or X = a | b | X
{Browse X}
```

| Oz Browser |
| :--- | :--- |
| Browser Selection Options |
| $\mathrm{a}\|\mathrm{b}\| \mathrm{a}\|\mathrm{b}\| \mathrm{a}\|\mathrm{b}\| \mathrm{a}\|\mathrm{b}\| \mathrm{a}\|\mathrm{b}\| \mathrm{a}\|\mathrm{b}\| \mathrm{a}\|\mathrm{b}\| \mathrm{a}\|\mathrm{b}\| \mathrm{a}\|\mathrm{b}\| \mathrm{a}\|\mathrm{b}\| \mathrm{a}\|\mathrm{b}\| \mathrm{a}\|\mathrm{b}\| \mathrm{a}\|\mathrm{b}\| \mathrm{a}\|\mathrm{b}\| \mathrm{a} \mid$ |
| $\mathrm{b}\|\mathrm{a}\| \mathrm{b}\|\mathrm{a}\| \mathrm{b}\|\mathrm{a}\| \mathrm{b}\|\mathrm{a}\| \mathrm{b}\|\mathrm{a}\| \mathrm{b}\|\mathrm{a}\| \mathrm{b}\|\mathrm{a}\| \mathrm{b}\|\mathrm{a}\| \mathrm{b}\|\mathrm{a}\| \mathrm{b}\|\mathrm{a}\| \mathrm{b} \mid, \ldots$ |

- Example: rational trees (section 12.3.1) The graph $\mathrm{x}=\mathrm{foo}$ ( X ) represents the tree $\mathrm{X}=\mathrm{foo}(\mathrm{foo}(\mathrm{foo}(. .)$.$) ).$


## Entailment (the $==$ operation)

- It returns the value true if the graphs starting from the nodes of $X$ and $Y$ have the same structure (it is called also structure equality).
- It returns the value false if the graphs have different structure, or some pairwise corresponding nodes have different values.
- It blocks when it arrives at pairwise corresponding nodes that are different, but at least one of them is unbound.


## Entailment (example)

- Entailment check/test never do any binding.
- declare

L1=[11 2 ]
L2 =' |' (1 ' |' (2 nil) )
L3=[ll 3 ]
\{Browse L1==L2\}

```
{Browse L1==L3}
```

- declare

L1 = [1]
L2 $=$ [ X$]$
\{Browse L1==L2\}

- \% blocks as X is unbound


## Summary

- Programming language definition: syntax, semantics - CFG, EBNF, ambiguity
- Data structures
- simple: integers, floats, literals
- compound: records, tuples, lists
- Kernel language
- linguistic abstraction
- data types
- variables and partial values
- statements and expressions (next lecture)

Lab Session 0

- Wed $24^{\text {th }}$ August 2007
- Time : 3-6pm (choose 1-hr slot)
- Venue : -
- Deadline : 28 ${ }^{\text {th }}$ August 2007 5pm

Reading suggestions

- From [van Roy,Haridi; 2004]
- Chapter 2, Sections 2.1.1-2.3.5
- Appendices B, C
- Exercises 2.9.1-2.9.3


[^0]:    24 Aug 2007
    CS2104, Lecture 2

[^1]:    - true
    - false

