

Exercise 1. Circle the free variables in the following code fragments.

```

local X in
    Y=Y+X
End

local F in
X = {F {H 2} X*2}
End

fun {P X}
    if X=<0 then X
    else {P (X-2)} end
end

local L in
case L of
    nil then 0
    [] H|T then H
end
end

```

Exercise 2. Consider a generic binary tree data structure of the following form:

```
<BTREE A> ::= nil | node(A, <BTREE A>, <BTREE A>)
```

Note that A denotes the generic type for each element of the tree. Using pattern-matching constructs and recursion, write Oz programs to perform the following whereby informal types have already been given.

- i) A function that counts the number of elements in a given tree.
 $\text{// Count : } \langle \text{BTREE A} \rangle \rightarrow \text{Int}$
- ii) A function that returns a list of elements satisfying a given predicate.
 $\text{// FilterTree : } \{\langle \text{BTREE A} \rangle, (\text{A} \rightarrow \text{Bool})\} \rightarrow \langle \text{List A} \rangle$
- iii) A function that partitions the elements of a tree into two lists based on a given predicate. Those elements satisfying the predicate are returned in the first list, and the rest are returned in the second list.
 $\text{// Partition : } \{\langle \text{BTREE A} \rangle, (\text{A} \rightarrow \text{Bool})\} \rightarrow \langle \text{List A} \rangle \# \langle \text{List A} \rangle$

Question 3. Higher-Order Programs

Consider the following higher-order functions:

```

fun {FoldR F U L}
    case L of
        nil then U
        [] X|L2 then {F X {FoldR F U L2}}
    end
end

fun {Map F XS}
    case XS of
        nil then nil
        [] X|Xr then {F X}|{Map F Xr}
    end
end

```

Predict the output (data structure being returned) for the following code fragments. If there is a program error, please describe it.

- (i) {Map (fun {\$ x} x>3 end) [2 3 4 5]}
- (ii) {Map (fun {\$ x} x+3 end) [2 3 4 5]}
- (iii) {FoldR (fun {\$ x u} 1+u end) 0 [2 3 4 5]}
- (iv) {FoldR (fun {\$ x u} x end) 0 [2 3 4 5]}
- (v) {FoldR (fun {\$ x u} x end) 0 nil}
- (vi) {FoldR (fun {\$ x u} if x mod 2!=0 then x|u else u end end) nil [2 3 4 5]}
- (vii) {Map (fun {\$ x} [x] end) [2 3 4 5]}
- (viii) {Map (fun {\$ x} 1.3 end) [2 3 4 5]}
- (ix) {Map (fun {\$ x} (fun {\$ n} N+x end) end) [2 3 4 5]}
- (x) {FoldR (fun {\$ x u} u end) 0 [2 3 4 5]}