

Axiom of Propositional Logic, as Data Structure

Tactic used for same idea, in “native mode”

Axiom Top_I :

holds propTop.

“trivial”, “apply I”

Axiom Conj_I : forall f1 f2,

“split”

holds f1 ->

holds f2 ->

holds (propConj f1 f2).

Axiom Conj_E1 : forall f1 f2,

“destruct H”, where “H : P \wedge Q”

holds (propConj f1 f2) ->

holds f1.

Axiom Conj_E2 : forall f1 f2,

“destruct H”, where “H : P \wedge Q”

holds (propConj f1 f2) ->

holds f2.

Axiom NegNeg_E : forall f,

“apply NNPP” (for LEM, use
“generalize (classic F)” or
“LEM F”)

holds (propNeg (propNeg f)) ->

holds f.

Axiom Impl_I : forall f1 f2,

“intro”, “intros”

(holds f1 -> holds f2) ->

holds (propImpl f1 f2).

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```
Axiom Impl_E : forall f1 f2,  
  holds (propImpl f1 f2) ->  
  holds f1 ->  
  holds f2.
```

“apply”, “apply ... in ...”, “generalize”, “spec”

```
Axiom Disj_I1 : forall f1 f2,  
  holds f1 ->  
  holds (propDisj f1 f2).
```

“left”

```
Axiom Disj_I2 : forall f1 f2,  
  holds f2 ->  
  holds (propDisj f1 f2).
```

“right”

```
Axiom Disj_E : forall f1 f2 f3,  
  holds (propDisj f1 f2) ->  
  (holds f1 -> holds f3) ->  
  (holds f2 -> holds f3) ->  
  holds f3.
```

“destruct”

```
Axiom Bot_E : forall f,  
  holds propBot ->  
  holds f.
```

“elimtype False”

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Axiom Neg_E : forall f,

“contradiction”, “destruct”

 holds f ->

 holds (propNeg f) ->

 holds propBot.

Axiom Neg_I : forall f,

“intro” (or “unfold not. intro.”)

 (holds f -> holds propBot) ->

 holds (propNeg f).