Beyond Tests: Program Vulnerability Repair via Crash Constraint Extraction

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Automated program repair is an emerging technology which seeks to automatically rectify program errors and vulnerabilities. Repair techniques are driven by a correctness criterion which is often in the form of a test-suite. Such test-based repair may produce over-fitting patches, where the patches produced fail on tests outside the test-suite driving the repair. In this work, we present a repair method which fixes program vulnerabilities without the need for a voluminous test-suite. Given a vulnerability as evidenced by an exploit, the technique extracts a constraint representing the vulnerability with the help of sanitizers. The extracted constraint serves as a proof obligation which our synthesized patch should satisfy. The proof obligation is met by propagating the extracted constraint to locations which are deemed to be "suitable" fix locations. An implementation of our approach (ExtractFix) on top of the KLEE symbolic execution engine shows its efficacy in fixing a wide range of vulnerabilities taken from ManyBugs benchmark, real-world CVEs and Google's Open-source-systems OSS Fuzz framework. We believe that our work presents a way forward for the overfitting problem in program repair, by generalizing observable hazards/vulnerabilities (as constraint) from a single failing test or exploit.

CCS Concepts: • Software and its engineering → Automatic programming; Software testing and debugging; • Security and privacy → Software security engineering.

Additional Key Words and Phrases: Automated Program Repair, Overfitting, Constraint Extraction and Propagation

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1 INTRODUCTION

Automated program repair [28] is an emerging area for automated rectification of programming errors. In the most commonly studied problem formulation, the goal is to find a (minimal) change to
a given buggy program $P$ to make it pass a test-suite $T$—i.e., test-suite driven program repair. As the goal is to find change that merely passes the test-suite $T$, the automatically generated patch may overfit the test data, meaning that the patched program $P'$ may still fail on program inputs/tests outside of $T$ [24, 47]. The problem is particularly dangerous when fixing software vulnerabilities. If the correctness specification driving the repair of $P$ is incomplete (such as a test-suite $T$)—the automatically generated patch may not completely fix the vulnerability meaning that the patched program is still vulnerable. It has been shown in the past that even for manually generated fixes, 9% of the fixes are incomplete or incorrect [62]. For automatically generated fixes of program vulnerabilities, we need a stronger level of assurance about the quality of patches.

Automatically generating high-quality fixes is one of the key challenges in program repair research today. Low-quality fixes that over-fit the given test suite result from weak specifications driving the repair. The fundamental reason for the existence of over-fitting patches is that the patch space is under-constrained due to the incomplete specification given by test suites [47]. The over-fitted patches may change program behaviors in an unexpected way, e.g. change the original functionality. When fixing a crash or vulnerabilities, the patched program could fix the crash/vulnerabilities on the given tests, but it could still be vulnerable on the inputs outside the given test suite.

1.1 Overall Methodology

In this paper, we propose a general approach to combat the over-fitting problem in program repair via symbolic reasoning, specifically for fixing security vulnerabilities. Our key insight is that information about the underlying cause of vulnerability can be automatically extracted, and the extracted information can then be used to guide Automated Program Repair (APR). The information is extracted in the form of a constraint that all program inputs must satisfy at the location where the vulnerability is witnessed. In order to avoid repeating the vulnerability, then, the goal of repair is to ensure the constraint is always satisfied at the location of the vulnerability.

1.2 Challenges

Our constraint-driven program repair methodology involves several challenges that need to be overcome.

- **Constraint extraction**: The first challenge (Constraint extraction) is to extract a crash-free constraint or CFC from an observable crash/vulnerability. The observable program failure is a concrete property violation when executing a failing test or exploit. In contrast, CFC should capture the properties that all program inputs must satisfy at the crash location, in order to avoid the vulnerability.

- **Fix localization**: Our second challenge lies in fix localization (FL). Fix localization finds one (or more) suitable fix location(s). Typically, existing FL approaches, e.g. spectrum-based FL [43], rely on a given high-quality test suite, which is not always available. Often, there is only one test in the form of an exploit. So, it is a challenging task to infer fix locations with only one failing test.

- **Constraint propagation**: After we determine the crash-free constraint (CFC) and fix location, guiding patch generation using the constraint is not straightforward because the fix location could be different from the crash location. For instance, the following code shows a bug where the source and destination of memcpy overlap\(^1\). The bug is witnessed at line 4, but the correct patch was applied at line 1. We could extract constraint at the crash location (line 4) to ensure source and destination do not overlap, however, the constraint cannot be directly used to guide patch generation at fix location (line 1).

\(^1\)http://www.cplusplus.com/reference/cstring/memcpy
Beyond Tests: Program Vulnerability Repair via Crash Constraint Extraction

```plaintext
1 - for (i = 3; i < size / 2; i *= 2) // the correct fix location
+ for (i = 3; i <= size / 2; i *= 2)
2  memcpy (r + i, r, i);
3  if (i < size )
4  memcpy (r + i, r, size - i); // the crash location
```

Since fix location(s) could be different from the crash location, the extracted constraint must be propagated and transformed to guide patch generation at fix location(s).

- **Patch synthesis**: The final challenge is to use program synthesis to generate candidate patches that ensure that the constraint is satisfied for all possible inputs.

### 1.3 Tackling the challenges

To address the above challenges, our workflow begins with the detection of an exploitable vulnerability in the form of a crash, i.e., unexpected program termination due to control flow reaching an invalid state. With the help of sanitizers, such as AddressSanitizer (ASAN) [46] or UndefinedBehaviourSanitizer (UBSAN) [53], we could convert vulnerabilities into normal program crash; in the rest of this paper, we generally regard a exploit as a failing test. After witnessing a crash in an exploit, we extract the crash-free constraint or CFC (first challenge) using a template-based approach. According to pre-defined templates, a constraint representation of the violated condition—i.e., the crash-free constraint—can then be extracted from either the program itself (e.g. user assertion failure), API documentation, or safety properties enforced by dynamic analysis tools such as sanitizers. For example, a buffer overflow can be formalized as a violation of constraint:

```
access(buffer) < base(buffer) + size(buffer)
```

This constraint is extracted at run-time when the crash is witnessed and represents the precise condition that all patched programs must satisfy in order to avoid repeating the same crash.

We address the second challenge (**Fix localization**) by examining program dependencies, instead of purely relying on test suites. Specifically, we take as input one failing test, and use the crash location as a starting point and find candidate fix locations using control/data dependency analysis.

Once the fix locations are determined, to solve the third challenge (**Constraint propagation**), we propagate the extracted constraint backward from the crash location to one or more suitable fix locations by calculating the weakest precondition.

To address the last challenge (**Patch synthesis**), we integrated the second-order program synthesis with counterexample guided inductive synthesis. We synthesize a patch so that the weakest precondition, the extension of crash-free constraint, cannot be violated, thereby guaranteeing that the patched program cannot repeat the same crash, and thus resolving the vulnerability.

Our workflow allows the program repair system to decide between single-line and multi-line fixes as shown by experiments. We instantiate the proposed approach in a prototype named ExtractFix.

### 1.4 Contributions of the paper

The contributions of this paper can be summarized as follows.

- **Conceptual Contribution**: We propose a technique for completely fixing security vulnerabilities which alleviates the well-known overfitting problem in program repair [47]. This is important since today, many security vulnerabilities once detected and reported as CVE remains un-fixed for a significant period. The automated repair can thus reduce the exposure to these un-fixed vulnerabilities.

- **Technical Contribution**: Our main insight is to extract symbolic constraints from violations in an exploit trace witnessed by sanitizer. The constraint extraction from sanitizers is made possible by automatically symbolizing program variables relevant to the crash. Our constraint-based
program repair method has several technical novelties. First of all, we provide an effective constraint/dependency based fix localization instead of relying on the widely used statistical fault localization. Secondly, we are able to synthesize non-trivial patches at locations different from the crash location, owing to having scalable constraint propagation. Last, we extend existing second-order program synthesis methods to generate patches with minimal syntactic/semantic changes.

• **Utilitarian Contribution:** We implement our security vulnerability repair approach in a tool named EXTRACTFIX. We evaluate EXTRACTFIX on a wide range of vulnerabilities from ManyBugs benchmark and real-world CVEs. Evaluation results show that EXTRACTFIX can generate more correct patches than state-of-the-art automated program repair tools. The generated patches can be found in https://extractfix.github.io.

2 OVERVIEW

For our purposes, a crash is broadly defined to be any program termination due to control flow reaching certain illegal states where conditions/properties are violated. A crash can be caused by the violation of an explicit user assertion (e.g., assert(C)), an implicit assertion enforced by the operating-system (e.g., illegal memory access), or instrumented check inserted by sanitizers to enforce some safety properties. Typical sanitizers, such as AddressSanitizer (ASAN) [46] and UndefinedBehaviorSanitizer (UBSAN) [53], instrument the program with implicit assertions that enforce additional properties, such as memory safety, type safety, integer overflows protection, etc. If a sanitizer assertion is violated, the program will abort (i.e., “crash”), usually with an error message indicating the problem. The underlying cause of a “crash” can be automatically extracted in the form of a crash-free-constraint (CFC). The CFC represents the condition that should be satisfied at the crashing location in order to avoid repeating the crash. For example, for a user assertion violation (assert(C)), the CFC is C itself, for a NULL-pointer de-reference on p the CFC is (p!=0), and for an array bounds overflow error on a[i] the CFC is (i<SIZE) where SIZE is the size of array a. If the crashing program is patched so that the CFC is always satisfied at the crash location, then the same crash cannot be repeated for any program input.

2.1 Workflow

Our basic workflow consists of several components/steps, including:

1. **Constraint Extraction.** Given a program and a single input that exercises the crash, the first step is to extract the “crash-free constraint” (CFC). The observable program crash is a concrete property violation when executing a failing test or exploit, while CFC should capture the properties for all possible inputs. The CFC is the symbolization or abstraction of the concrete violations. We extract CFC according to predefined templates which formulate the underlying cause of the defect.

2. **Fix Localization.** Once the CFC is generated, one (or more) candidate fix location(s) will be generated using a dependency-based fix localization algorithm. Unlike the widely used spectrum-based fault localization (SBFL) [43], we take one failing test as input, and use the crash location as a starting point and find candidate fix locations using control/data dependency analysis.

3. **Constraint Propagation.** The CFC is a constraint over the program state at the crash location. The CFC at the crash location is propagated to a CFC′ at a given fix location satisfying the following Hoare triple:

\[ \{CFC\} P \{CFC'\} \quad \text{(CFC-Propagation)} \]

Here, P represents the program between fix location and crash location. CFC′ is the least restrictive (weakest) precondition that will guarantee the postcondition CFC [4]. Finding CFC′
void fillp (char *r, size_t size) {
    ...
    r[2] = bits & 255;
    for (i = 3; i < size / 2; i *= 2)
    memcpyp(r + i, r, i);
    if (i < size) 
    memcpyp(r + i, r, size - i);
    ...
}
(a) Buggy code snippet.

Fig. 1. Workflow example from Coreutils

involves solving CFC-PROPAGATION. For multi-line repair, the approach is generalized and propagation is applied to multiple fix locations.

(4) **Patch Synthesis.** Once the fix location and propagated CFC’ have been decided, the next step is to generate patch candidates. Patch synthesis involves rewriting the fix location statement \( \rho \) into an alternative \( f \) such that the following Hoare triple holds:

\[
\{ \text{true} \} [ \rho \mapsto f ] \{ \text{CFC'} \} P \{ \text{CFC} \}
\]

\( \text{(CFC-Repair)} \)

The generated patch is guaranteed to ensure that CFC’ is satisfied, meaning that the CFC condition at the crash location cannot be violated in the patched program.

**Workflow Example.** To illustrate our workflow, we consider an example bug from Coreutils. The buggy code snippet is shown in Figure 1a. Here, the snippet attempts to fill a buffer \( r \) with a pattern determined by variable \( \text{bits} \) using repeated calls to memcpy. The length of each memcpy operation is doubled inside the for-loop, and the final memcpy handles any remaining unfilled space in the buffer. Unfortunately, the code snippet contains a bug \(^2\) For certain inputs (e.g., size=13), the source and destination regions for the final memcpy will overlap— an undefined behaviour under the memcpy specification. This bug may cause a program crash on some platforms. Specifically, when size=13, the for-loop will terminate in the second iteration with \( i=6 \) and size/2=6 (integer division). Then, at line 7, the source and destination of memcpy overlap because \( r+(13-6)\rangle r+6 \). Using an appropriate sanitizer (UBSAN), this program will crash on the final memcpy call.

Figure 1b shows the overall workflow of our approach. We start with the single crashing input (size=13) that triggers the crash on line 7 (highlighted). Step (1) generates the CFC corresponding to the crash according to a predefined template. The CFC template (shown in Section 4.1) of memcpy(p, q, s) is defined as \( p+s \leq q \lor q+s \leq p \). In this case, CFC is

\[
(r+i+size-i\leq r \lor r+size-i\leq r+i) \equiv (size \leq 0 \lor size\leq2*i)
\]

Since size is an unsigned integer (size_t) value, we only focus on the second clause \( size\leq2*i \) in this example. Step (2) determines candidate fix locations. One promising fix location is the for-condition on line 4 (highlighted) since there exists a control dependency with an assignment \( i \ *= \ 2 \), line 4) that has a data dependency with the crash location. Step (3) propagates the CFC to the fix location along all feasible paths. In this case, the CFC is propagated along one path with path constraint \( i<size \), and CFC remains unmodified. Step (4) synthesizes a patch \( f \) to replace the for-condition. To completely fix the bug, we should ensure size\leq2*i is always satisfied after applying \( f \). In this case, the synthesizer gives \( i \ <= \ size/2 \). Thus, the program can be patched as follows:

\(^2\)https://debbugs.gnu.org/cgi/bugreport.cgi?bug=26545
for (i = 3; i < size / 2; i *= 2)
+ for (i = 3; i <= size / 2; i *= 2)
The resulting patch is equivalent to the developer patch. In contrast, test-driven program repair approaches may produce overfitting patches. For example, the following patch generated by Fix2Fit [11] fixes the bug for size=13, but does not generalize to other crashing inputs, e.g. size=7.

+ for (i = 3; i < size / 2 || i == 6; i *= 2)

3 BACKGROUND ON SYNTHESIS

Given a set of specifications, program synthesis generates a program satisfying the specifications. Program synthesis is formalized to be a second-order constraint solving problem in the recent work on SE-ESOC [35]. We build our program synthesizer on top of the approach proposed by SE-ESOC. Given a set of components $C$, this approach first constructs a set of terms and then represents them as a tree. Specifically, each leaf of the tree corresponds to components without input, and an intermediate node has as many subnodes as the maximal number of inputs of a component.

Figure 2 shows a tree with three nodes, and each node is constructed using four components ("x", "y", "+", "-").

For a node, $\varphi_{node}$ describes the semantic relations of each node between its output and inputs, where the inputs are the outputs of its sub-nodes. $\varphi_{choice}$ restricts that only exactly one component is selected inside each node. Using the above encoding, the output of the root node represents a function $f$ that connects inputs and outputs of components. Finally, given $n$ input-output pairs...
Table 1. Basic crash classes, crash expressions/statements, and the corresponding Crash-Free Constraint CFC-template. We consider seven types of crash: explicit developer assertion violation, sanitizer-induced crash such as buffer overflows/underflows, integer overflows, API constraint violation.

<table>
<thead>
<tr>
<th>Class</th>
<th>Template ID</th>
<th>Expression</th>
<th>CFC Template</th>
</tr>
</thead>
<tbody>
<tr>
<td>developer</td>
<td>$T_1$</td>
<td>assert($C$)</td>
<td>$C$</td>
</tr>
<tr>
<td>sanitizer</td>
<td>$T_2$</td>
<td>*$p$</td>
<td>$p + \text{sizeof}(p) \leq \text{base}(p) + \text{size}(p)$</td>
</tr>
<tr>
<td></td>
<td>$T_3$</td>
<td>$a \text{ op } b$</td>
<td>$\text{MIN} \leq a \text{ op } b \leq \text{MAX}$ (over $\mathbb{Z}$)</td>
</tr>
<tr>
<td></td>
<td>$T_4$</td>
<td>memcpy($p$, $q$, $s$)</td>
<td>$p + s \leq q \lor q + s \leq p$</td>
</tr>
<tr>
<td></td>
<td>$T_5$</td>
<td>*$p$ (for $p=0$)</td>
<td>$p \neq 0$</td>
</tr>
<tr>
<td></td>
<td>$T_6$</td>
<td>$a / b$ (for $b=0$)</td>
<td>$b \neq 0$</td>
</tr>
</tbody>
</table>

$\{(\alpha_k, \beta_k) \mid 1 \leq k \leq n\}$, the synthesis goal is to generate function $f$ by traversing the abstract tree and satisfying $\varphi_{\text{correct}}$, where

$$\varphi_{\text{correct}} := \bigwedge_{k=1}^{n} \beta_k = f(\alpha_k) \quad (3)$$

4 METHODOLOGY

Our workflow for program repair involves constraint extraction, propagation, and patch synthesis. In this section, we discuss each step in more details.

4.1 Crash-Free Constraint Extraction

Our workflow begins with a vulnerable program and a single crashing input. The first step is to extract both (1) the crashing location (e.g., filename/lineno), and (2) the crash-free constraint (CFC) representing the condition that was violated and the underlying cause of the crash. For (1), the crash location is extracted according to debugging information when the crash is triggered, meaning that the program must be compiled with debugging enabled ($\text{-g}$). For (2), the CFC extraction is template-based, and is instantiated from the crashing expression/statement. Our repair technique currently considers crashes due to:

(1) Developer-induced crashes, i.e., assert($C$) failure;
(2) Sanitizer-induced crashes caused by the program violating a sanitizer-enforced safety property (e.g., memory safety, type safety, etc.);

A summary of the different kinds of crashes and the corresponding CFC-templates are shown in Table 1. Here, the crash expression is matched against the corresponding crashing expression/statement from the buggy program, and the CFC-template is instantiated accordingly. We choose those templates because they cover the common errors and vulnerabilities in C/C++ programs, e.g. null pointer dereference, integer/buffer overflow. In this paper, we restrict to fix the bugs supported by these templates. Our tool can also fix other kinds of bugs by extending the templates.

For Example 2.1, the crashing statement memcpy($r+i$, $r$, $\text{size}−i$) is matched against the template from Table 1 using the substitution $p=r+i$, $q=r$, and $s=\text{size}−i$. This yields the following CFC after substitution and simplification:

$$(r+i+\text{size}−i \leq r \lor r+\text{size}−i \leq r+i) \equiv (\text{size} \leq 0 \lor \text{size} \leq 2*i)$$

We now discuss the CFC generation step in more details.
4.1.1 User-Assertion. The CFC for user assertions is relatively straightforward to generate. Assuming the crash is caused by a user assertion failure \( \text{assert}(C) \), the CFC can be read directly from the assertion statement itself, i.e., \( \text{CFC}=C \).

4.1.2 Sanitizer Constraint Extraction. For our purposes, a sanitizer is any dynamic analysis tool that instruments/modifies the program with additional runtime checks enforcing certain safety properties, such as memory safety, preventing integer overflows or other undefined behavior avoidance. Typically, sanitizers insert instrumented checks/ assertions before relevant operations. For example, as shown in the following figure, the instrumentation (left part) of most spatial memory safety sanitizers (a.k.a., bounds-check sanitizers) track object bounds information (i.e., the size and base address of each allocated object) using a disjoint metadata store or related method. At run-time (right part of the following figure), this metadata is used to look up the object bounds corresponding to the dereferenced pointer, and this pointer (access) is checked against these bounds (base+size). If the instrumented check fails, the program is terminated, i.e., “crashes”. Crashes can be caused by hardware failure such as NULL-pointer dereference and divide-by-zero are detected using an appropriate sanitizer or signal handler, e.g., SIGSEGV with si_addr=0 and SIGFPE with si_code=FPE_INTDIV respectively. The corresponding CFC ensures that the crashing symbolic pointer/divisor is not zero.

Sanitizers can only detect “crashes” on concrete program state, e.g. specific values of size and base on a certain test. We then symbolize the safety condition that sanitizer enforces by mapping the concrete state back to variables/memory relevant to the crash. For the example in Figure 1a, a sanitizer detects source/destination memory regions overlap when size=13. We then generate CFC by mapping the concrete value of source/destination back to program variables \( r \) and \( r+i \), respectively. To map a concrete crashing state back to symbolized variables, we extend the metadata by also restoring the corresponding program variable information (e.g. variable name, type) representing size and base. When the crash is detected, we can simply construct the crash-free constraints using the symbolized program states (program variables). However, in some cases, we may fail to symbolize constraints because some variables used to construct CFC are not accessible at the crashing points, i.e. the variables stored in metadata have already been killed at the crashing points. In the general case, we could symbolize the CFC using an extended program state.

Sanitizer Constraint Language. Some sanitizer-inserted instrumented checks enforce conditions over an extended state that is managed by a runtime library or additional instrumentation. This extended state is not part of the original program itself. As such, the sanitizer assertion is over an extended program state that includes the sanitizer runtime. To handle sanitizer-extended state, we allow the generated CFC to include functions/types/variables that do not necessarily appear in the original program. For example, in the case of bounds-check sanitizers, we introduce two new abstract functions:

- base(p): the base address of the object referenced by p; and
- size(p): the size (in bytes) of the object referenced by p.

The generated CFC will be over these extended functions (see Table 1). Another example is integer-overflow sanitizers, where the generated CFC (e.g., \( a+b \leq \text{MAX} \)) is over arbitrary precision integers...
ALGORITHM 1: Fix localization algorithm

Input: A crash location (crashLoc) and an Inter-procedure Control Flow Graph (ICFG)
Output: A set of candidate fix locations (fixLocs)

fixLocs := \{crashLoc\};

repeat
    fixLocsPrev := fixLocs;
    foreach fixLoc ∈ fixLocsPrev, loc ∈ ICFG − FixLocsPrev do
        if depends(loc, fixLoc) ∧ dominates(CFG, loc, crashLoc) then
            fixLocs := fixLocs ∪ \{loc\};
        end
    end
until fixLocsPrev = fixLocs;
rFixLocs := rank(fixLocs);
return rFixLocs;

(\(\mathbb{Z}\)) rather than the original 32bit integer type. For the purpose of CFC-generation, we extract the extended-language constraints "as-is", and defer further simplification/handling to the latter stages of our workflow.

4.2 Dependency-based Fix Localization

Once the crash location and CFC have been determined, the next step is to decide one (or more) fix location(s) where the patch(es) are to be applied. Typically, existing FL approaches, e.g. spectrum-based FL [43], find candidate fix locations by analyzing the execution trace of passing and failing tests. The FL results depend on the quality of the tests, but high-quality tests are not always available. Unlike traditional FL approaches, we make a minimal assumption that only one failing test (exploit) is available, which is a very common scenario when security vulnerabilities are found.

The main intuition of our dependency-based fix localization is that the fix location(s) ought to exhibit a control or data-dependency with the crash location, such that, the statement at fix location can influence the truth value of the CFC. We are also looking for fix location(s) which appear on the execution path of the crashing test. As a practical realization of these intuitions, our repair technique uses the crash location as the starting point and performs backward control and data-dependency analysis along with crashing path. Algorithm 1 summarizes the fix localization algorithm to decide candidate fix locations. Here, the algorithm takes as input an Inter-procedure Control Flow Graph (ICFG) and a crash location (crashLoc). Since the ICFG may be large in practice, partial ICFG is constructed by considering locations visited by the failing test (exploit) and dependency analysis is performed with the crashing statement as the slicing criterion. The algorithm iteratively builds a set of potential fix locations (fixLocs) by adding nodes that (1) have a (transitive) dependency with the crash location, and (2) dominate the crash location. Finally, the algorithm generates a sequence of fix location candidates, which are ranked according to the distance to the crash location.

Dependency Closure. Our algorithm also considers the transitive closure of static data and control dependencies [48] of the crashing statement to compute potential fix locations. Data dependencies are determined using the standard def-use-chain traversal algorithm over a Single Static Assignment (SSA) representation of the program. We detect control dependencies using the standard Control Dependence Graph (CDG) [5] program analysis as part of the LLVM compiler infrastructure. Considering Figure 1a once more, the for-condition (line 4) is a control dependency on the assignment.
statement \((1 \ast= 2, \text{ also line 4})\), and the crash location (line 7) is data dependent on this assignment. Thus, the \textit{for}-condition is a potential fix location.

\textbf{Crashing Path and Dominance.} The set of all (transitive) data and control dependencies of the crash location can be quite large, leading to many potential fix locations. To reduce the number of potential fix locations, we restrict the fix location(s) should exist somewhere along the concrete path belonging to the original crashing test case. Furthermore, in order to guarantee that the patched program satisfies the \textit{CFC}, our fix localization algorithm only considers statements that \textit{dominate} the crash location—i.e, all paths from the entry point to the crash location must also pass through the fix location, as illustrated in Figure 3. Considering Example 2.1, the \textit{for}-condition (line 4) \textit{dominates} the crash location, since all paths from the entry will visit the \textit{for}-condition at least once. There are usually multiple nodes that dominate the crash location in real-world programs, meaning there are multiple potential fix locations. Note that, there are always at least two nodes that dominate the crash location: the entry point, and the crash location itself.

\subsection{4.3 Crash-Free Constraint Propagation}

The weakest precondition of a formula \(\varphi\) is the least restrictive precondition that will guarantee \(\varphi\) \cite{4}. We consider the problem of backward propagation as finding the weakest precondition \(CFC'\) at fix location \(l\) that necessarily drives the program to the crash location and satisfies \(CFC\) at the crash location. As shown in \cite{16} (Theorem 9), for all deterministic programs \(P\) and any desired post-condition \(Q\): \(wp(P, Q) = fwd(P, Q)\), where \(wp\) represents the weakest precondition that drives program \(P\) to satisfy \(Q\), while \(fwd\) is the result generated by forward symbolically executing \(P\) from the first statement to the last and substituting the used variables in \(Q\) with symbolic state of variables.

\textbf{Example 4.1.} Consider the following program \(P\): \((x = x + x; x = x + x; x = x + x)\) and post-condition \(Q: x < 8\), the weakest precondition to guarantee \(Q\) is \(wp(P, Q) = \{x < 1\}\). Similarly, if we set \(x\) to be a symbolic variable and symbolically execute \(P\) from the beginning, we would get \(8x < 8\). That is, \(fwd(P, Q) = \{x < 1\}\).

In this paper, we use forward symbolic execution to calculate the weakest precondition. Given a fix location \(l\), crash location \(c\), and \(CFC\), we perform symbolic execution between \(l\) and \(c\), and calculate the weakest precondition \(CFC'\) at \(l\). Our symbolic execution starts concrete execution with a concrete input \(t\) until the fix location \(l\). The concrete input \(t\) can be the exploit of the vulnerability, or any test that can drive the program to \(l\). From the fix location, we insert symbolic variables and start symbolic execution to explore all the paths \(\Pi\) from fix location \(l\) to crash location \(c\).

\textbf{Symbolic Variable Insertion.} At fix location, existing semantics-based repair techniques, e.g. Semfix \cite{41}, Angelix \cite{38} and \cite{35}, represent the to-be-repaired expression as (either a first-order or a second-order) symbolic variable. Symbolic execution captures the constraint of passing a given test suite \(T\) by exploring alternate paths from the fix location along which the execution of \(T\) could be driven in the fixed program. In contrast, in our approach, symbolic execution computes the weakest pre-condition of the crash-free constraint \(CFC\), by exploring all paths between fix location and crash location. We apply the following transformation schemes to introduce second-order symbolic variable \(\rho\):

- changing the right-hand side of an assignment:

\[ x := E_1 \mapsto x := \rho(v_1, \ldots, v_n); \]
Fig. 3. Illustration of the fix localization algorithm. The algorithm attempts to find a node (fix location) that (1) is a dependency of, and (2) dominates the (crash location). All paths from the entry point to the crash location must pass through the fix location. There can be more than one path ($P_l$) between the fix and crash locations. It is allowable that some paths, including loops, from the fix location do not pass through the crash location ($P_{other}$).

- changing a condition:

$$\text{if}(E) \Rightarrow \text{if}(\rho(v_1, \ldots, v_n))$$

- adding an if-guard:

$$S; \Rightarrow i f(\rho(v_1, \ldots, v_n))\{S;\}$$

- adding an if-return:

$$\text{insert} : i f(\rho(v_1, \ldots, v_n))\{\text{return } C;\}$$

where $S$ is statement, $E$ is expression, $C$ is constant and $v_1, \ldots, v_n$ are the live variables at the fix location. We use if-return transformation only if the others fail to generate a correct patch, and the error handling code $C$ is generated using Talos [14]. Apart from generating a (second-order) symbolic variable $\rho$ at the fix location (to capture the to-be-synthesized expression) we also set the live variables $V$ (on which $CFC$ is dependent) as symbolic variables. We might introduce multiple symbolic variables. If a variable $v$ at the fix location may affect the truth value of $CFC$ at the crash location, we will set $v$ as a symbolic variable. This strategy introduces a minimal number of symbolic variables while ensuring that all relevant paths between fix and crash location are explored. With these symbolic variables, we can explore and navigate the paths between fix and crash location.

**Symbolic execution scope.** To avoid exploring irrelevant paths, all the paths that never reach crash location, e.g. $P_{other}$ in Figure 3, are terminated early (whether a path can reach $c$ is determined by analyzing control flow graph). With the help of symbolic variable injection and early termination, the explosion of paths is reduced. Furthermore, since fix locations are usually close to the crash location, we can further alleviate the path explosion problem which is common in symbolic execution.

**Constraint collection.** After symbolic exploration, we collect the path constraints $pc_j$ for each path $\pi_j \in \Pi$ (all feasible path from $l$ to $c$). Besides, following each $\pi_j$, all the variables used in $CFC$ can be represented using the symbolic variables ($V$ and $\rho$). By replacing the elements in $CFC$ with the symbolic representations of $V$ and $\rho$, we rewrite $CFC$ as $CFC'$. Then, $pc_j \Rightarrow CFC'$ will be exactly the same as the constraint by backward propagating $CFC$ from crash location to fix location along path $\pi_j$. Consider the following program

```
input x, i; if(i>0) y=x+1; else y=x-1; output y;
```

Suppose the $CFC$ is $(y > 5)$, along the if-then branch, we will get the constraint $(i>0 \Rightarrow x + 1 > 5)$. 

Constraint Simplification (Optional). The propagated constraints may still contain extended sanitizer-supplied functions (e.g., base(p)/size(p)) or types (e.g., \( \mathbb{Z} \) for integer overflow). There are two basic approaches to handling the extended constraint language: (1) Synthesize the patch “as-is”. If necessary, extra functionality can be supplied using a suitable runtime library; or (2) translate the extended constraints into the native language if possible.

Approach (1) is the most general. For example, runtime implementations of the base(p)/size(p) are available using a suitable library, meaning these functions can be used in a patch. The downside is that this introduces an additional dependency on the patched program, which may be undesirable for some applications. The alternative (2) approach is to rewrite the extended constraints back into the native language if possible. For example, using a simple static analysis, our tool searches for a dominating CFG node where the object associated to \( p \) is first allocated, e.g., \( \text{ptr} = \text{malloc}(\text{len}) \). If such a node is found, then our tool can substitute base(p)=ptr and size(p)=len. This approach is less general than (1) since it depends on a suitable substitution to be found.

Note that the weakest precondition calculation inherits the limitation(s) of how symbolic execution is performed. For instance, we may generate incomplete weakest preconditions if there are loops between fixing location and crash location. In our setting, we also inherit the solution from symbolic execution by adding a bound to the number of loop iterations, which may result in incorrect patches as shown in Section 5.

4.4 Patch Synthesis

After backward propagation of crash-free constraints, patch synthesis is used to rewrite the statement at fix location and guarantee:

\[
\{true\} \begin{array}{l}
\rho \mapsto f \\
\end{array} \{\text{CFC}'\}
\]

Although our reasoning is performed on a partial program (from fix to crash location), the synthesized patch will be also effective for the whole program, because the precondition (true) is applied. Once \( \{true\} \begin{array}{l}
\rho \mapsto f \\
\end{array} \{\text{CFC}'\} \) is satisfied, \( \text{CFC}' \) is guaranteed to hold under any context.

Instead of satisfying input-output relations as shown in Equation 3, the synthesizer is used to produce a patch satisfying a certain constraint. Suppose \( \Pi \) is the set of feasible paths between fix and crash location, for each path \( \pi_j \in \Pi \), the generated patch \( f \) should imply \( \text{CFC}'_j \) under all input space. Then, we change the definition of \( \phi_{\text{correct}} \) defined in Section 3 to:

\[
\phi_{\text{correct}} := \bigwedge_{j=1}^{||\Pi||} \left( (\rho = f(V) \wedge pc_j) \Rightarrow \text{CFC}'_j \right) \tag{4}
\]

where \( f \) represents the to-be-synthesized function and \( V \) is the set of variables used by \( f \). For the example 2.1, \( \phi_{\text{correct}} \) will be:

\[
\phi_{\text{correct}} = (\rho = f(\text{size}, i) \wedge \neg \rho \wedge i < \text{size}) \Rightarrow \text{size} \leq i \ast 2
\]

Since \( f \) is a function and the implication should hold for all inputs, \( \phi_{\text{correct}} \) is actually a second-order formula. To solve this formula, ExtractFix uses the idea of second-order solver [35] to convert \( \phi_{\text{correct}} \) to a first-order formula, and then uses counter-example guided inductive synthesis (CEGIS) [17] to find proper patches. By synthesizing \( f \) satisfying \( \phi_{\text{correct}} \), we can handle all bug-triggering inputs that violate \( \text{CFC}' \), hence \( \text{CFC} \).

Though the generated patch makes \( \text{CFC} \) hold, we may still have a wide choice of candidate patches. For fixing the bug in example 2.1, several patches satisfying the \( \phi_{\text{correct}} \) (equation 4) could be generated, such as \( \{1, i \leq \text{size}/2\} \). Obviously, the second one is more likely to be correct. To further improve the quality of patches, the intuition is that the correct patch should be similar, both syntactically and semantically, with the original program. To generate “similar” patches,
ALGORITHM 2: Extension of second-order synthesizer

Input: The original buggy expression $e$, the constraint $\varphi_{\text{correct}}$
Output: A patch $f$ which satisfies $\varphi_{\text{correct}}$

1. $\text{hard} := \varphi_{\text{wfp}}$;
2. $\text{soft} := \varphi_{\text{syn}}$;
3. $\text{patches} := \emptyset$;
4. while $|\text{patches}| \leq N$ and (timeout not reached) do
   5. $f_c := \text{pMaxSMT}(\text{hard}, \text{soft})$;
   6. $I := \text{SMT}(\neg \varphi_{\text{correct}}[f \mapsto f_c])$;
   7. if $I \neq \text{None}$ then
      8. $\text{hard} := \text{hard} \land \varphi_{\text{correct}}[V \mapsto I]$;
   else
      10. $\text{patches} := \text{patches} \cup \{f_c\}$;
   end
7. end
11. return $\text{semSelect}(\text{patches})$

ExtractFix extends the second-order solver proposed by Mechtaev et al. by further considering the distance between the patched and original program.

The overall workflow of our synthesizer is shown in Algorithm 2, which takes as input the suspicious expression $e$ and $\varphi_{\text{correct}}$, and generates a patch $f$. ExtractFix first generates a patch candidate by solving combined hard and soft constraints using MaxSMT[9] (line 5 of Algorithm 2). The hard constraint is initialized as $\varphi_{\text{wfp}}$ (refer section 3), which ensures the candidate is well-formed. The soft constraint $\varphi_{\text{syn}}$ formulates the syntax distance between buggy expression $e$ and candidate patch. More formally, we build abstract tree $T_e$ for $e$, and $T_c$ for the patch candidate, and define

$$\varphi_{\text{syn}} := \bigcup_{k=1}^{\mid T_e \mid} \{T_e^k \models T_c^k\}$$

where $T_e^k$ ($T_c^k$) denotes the $k$-th node of tree $T_e$ ($T_c$). MaxSMT constructs a patch candidate $f_c$ which strictly satisfies the hard constraint, and satisfies the maximum number of soft constraints (shortest distance). The candidate $f$ is then validated by Satisfiability Modulo Theories (SMT) solver [6] to check whether an input that violates $\varphi_{\text{correct}}$ exists (line 6). If such a counter-example $I$ exists (line 7-8), the counter-example $I$ is first encoded into first-order logic and then added into the hard constraint. Consider the example shown in Figure 1a, in the first iteration, assume $f_c = \lambda i. \lambda size. i < size/2$ , then

$$\varphi_{\text{correct}} = (\rho = (\lambda i. \lambda size. i < size/2) \land \neg \rho(i, size) \land i < size) \Rightarrow size \leq i \ast 2$$

is violated when $i = 6$ and $size = 13$. Therefore, we add

$$(\rho = f \land \neg \rho(6, 13) \land 6 < 13) \Rightarrow 13 \leq 12$$

i.e. $f(6, 13) = \text{true}$, into the hard constraints. With the refined hard constraints, the candidate $f_c$ generated in the next iteration will ensure $\varphi_{\text{correct}}$ must be satisfied under $I$, i.e. $f_c(6, 13) = \text{true}$. Eventually, a plausible patch $f_c$ is thereby generated, which will be added into the $\text{patches}$ list (line 10). The process continues until $\text{timeout}$ is reached or we find $N$ plausible patches, where $\text{timeout}$ and $N$ are defined by users.
The patch synthesis of ExtractFix is built on top of SE-ESOC [35]. The difference with SE-ESOC is two-fold. First, we introduce a set of soft constraints (Equation 5) to formulate the distance between original expression and patch candidates. Such that, we can generate patches that are syntactically similar to the original program. Second, SE-ESOC is designed to solve a problem with existential quantifiers, i.e., generate patches to pass existing tests. In contrast, the synthesis in ExtractFix generates patches that fix the bug for all the valid inputs. Thus, we integrate counterexample guided inductive synthesis into SE-ESOC to make it support solving problems with universal quantifiers, i.e., generate patches to fix the bug under all input space.

Among \( N \) plausible patches, the most likely to be the correct one is selected according to its semantic distance to the origin buggy expression \( e \) (semSelect line 13). Specifically, we (1) generate a set of inputs \( \mathcal{I} \) that can distinguish plausible patches in terms of their semantics (2) for each \( i \in \mathcal{I} \), calculate the values of each plausible patch and expression \( e \) (3) calculate the value distance between each patch with \( e \) (4) select the patch with the shortest distance.

4.5 Multiple-line Fix

The proposed work-flow can be easily extended to support bug-fixing in multiple locations. Fix localization can be generalized as a set of nodes that collectively dominate the crash location, i.e., all paths must go through one of the nodes from the set. Suppose we are introducing patches at location \( \{l_1, \ldots, l_n\} \), when propagating CFC, multiple second-order variables \( \{\rho_1, \ldots, \rho_n\} \) are introduced to represent the to-be-synthesized expressions at \( \{l_1, \ldots, l_n\} \), respectively. Correspondingly, the generated \( CFC' \) will involve multiple second-order variables \( \{\rho_1, \ldots, \rho_n\} \). Then, the goal of synthesizer is to generate a set of function \( \{f_1, \ldots, f_n\} \) to satisfy:

\[
\varphi_{\text{correct}} := \bigwedge_{j=1}^{||\Pi||} \left( \bigwedge_{i=1}^{n} (\rho_i = f_i(V_i)) \land pc_j \Rightarrow CFC'_j \right)
\] (6)

5 EVALUATION

We evaluate the effectiveness and efficiency of ExtractFix and answer the following research questions.

**RQ1** What is the overall effectiveness of ExtractFix in fixing vulnerabilities?

**RQ2** Compared with state-of-the-art techniques, can ExtractFix alleviate the overfitting problem in automated program repair?

**RQ3** What is the efficiency of ExtractFix in generating patches?

5.1 Implementation

We have implemented our approach in a tool named ExtractFix, whose architecture is shown in Figure 4. ExtractFix takes as input the vulnerable program, exploit (test case) and produces patches. ExtractFix is composed of four main components: constraint extractor, fix locator, propagation engine and patch synthesizer.

**Constraint extractor** takes as inputs the vulnerable program and exploit, generates a crashing location, and a crash-free constraint CFC. The constraint extractor is mainly implemented on top of sanitizers: Lowfat [7, 8] for buffer overflow/underflow and UBSAN [53] for integer overflow, null pointer dereference and etc. Although our prototype supports a specific set of defects, other bugs can be supported by integrating new sanitizers and corresponding templates. Once a crash is detected, the concrete crash condition is symbolized into crash-free constraint CFC by mapping the concrete value back to program variables. To enable the mapping, the programs should be compiled using clang with the debug option.
**Fix locator** takes as inputs the buggy program and crash information, and produces a set of ranked fix location candidates. The fix locator is a static analysis tool and is implemented as an LLVM pass \(^3\). We implement it on top of LLVM because LLVM provides a set of interfaces to generate control flow graphs and data dependency graphs.

**Propagation engine** is built on top of KLEE [2]. For the purpose of generating the weakest precondition, we modify the path exploration of KLEE in the following two aspects. First, we change the constraint collection by only considering the path constraints between fix and crash location. Second, we early terminate the paths that cannot reach a crash location. The execution scope is controlled by Controller.

**Patch synthesizer** is a second-order synthesizer which is implemented according to the approach proposed in [35]. Besides, ExtractFix implements three new features: (1) taking the CFC as correctness criterion (2) combining with counter-example guided synthesis and (3) taking into account the distance between patches and original buggy expression. In our implementation of the synthesizer, we use Z3 [6] as a backend SMT solver.

### 5.2 Experimental Setup

<table>
<thead>
<tr>
<th>Program</th>
<th>#Vul</th>
<th>Loc</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>Libtiff</td>
<td>11</td>
<td>81K</td>
<td>library for processing TIFF files</td>
</tr>
<tr>
<td>Binutils</td>
<td>2</td>
<td>98K</td>
<td>a set of programming tools for creating and managing binary programs</td>
</tr>
<tr>
<td>Libxml2</td>
<td>5</td>
<td>299K</td>
<td>XML C parser and toolkit</td>
</tr>
<tr>
<td>Libjpeg</td>
<td>4</td>
<td>58K</td>
<td>C library for manipulating JPEG files</td>
</tr>
<tr>
<td>FFmpeg</td>
<td>2</td>
<td>617K</td>
<td>library for processing audio &amp; video</td>
</tr>
<tr>
<td>Jasper</td>
<td>2</td>
<td>29K</td>
<td>library for coding &amp; manipulating image</td>
</tr>
<tr>
<td>Coreutil</td>
<td>4</td>
<td>78K</td>
<td>GNU core utilities</td>
</tr>
</tbody>
</table>

We evaluate our approach on two sets of benchmarks: ManyBugs [26] and our own constructed benchmark. ManyBugs is a C program benchmark suite that is widely used to evaluate automated program repair techniques, such as GenProg [27], Prophet [33] and Angelix [38]. Since we are

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\(^3\)LLVM Pass: http://llvm.org/docs/WritingAnLLVMPass.html
focusing on vulnerabilities in this paper, we only select bugs that relate to vulnerabilities as our subjects. We therefore select our subjects based on the following criteria:

1. we only consider bugs related to vulnerabilities, including segmentation fault, buffer overflow/underflow, integer overflow;
2. the target application can be compiled into LLVM [22] bitcode and executed by KLEE [2];
3. the target vulnerability can be reproduced in our environment.

We omit two applications of the benchmark (python and fbc) because we could not run these subjects on KLEE. In total, we select 26 defects from three applications: Libtiff, Lighttd, and Php.

Besides ManyBugs, we also constructed an additional vulnerability benchmark suite from a set of popular applications by searching the online databases [50–52]. Those databases provide a list of entries, and each of them contains an identification number, a short description of the bug and optional reproducer (i.e. exploit). We obtain our candidate bugs by searching for the bug types (including buffer-overflow/underflow, integer-overflow, divide-by-zero, null pointer, and developer assertion) that our prototype supports. We just consider the bugs reported after 2010 because the earlier bugs are harder to reproduce. Then, we randomly select and manually filter the subjects based on the following four criteria:

1. exploit(s) to trigger the vulnerability is available or exploit(s) can be constructed from the available information;
2. the target vulnerability has already been fixed by developers so that we have the ground truth on how to fix it;
3. the target application can be compiled into LLVM [22] bitcode and executed by KLEE [2];
4. the target vulnerability can be reproduced in our environment.

Finally, 30 unique vulnerabilities across seven applications are selected as our benchmark, which includes 16 buffer-overflow/underflow, 4 integer-overflow, 5 divide-by-zero, 3 API assertion, and 2 null pointer dereference. The exploits, as well as the instructions to reproduce the bugs, are obtained from blogs of researchers, bug reports, exploit databases or the attachments along with patch commit. The selected subjects are across seven applications, and their brief descriptions are given in table 2. Column Loc represents their lines of source code, while column #Vul shows the number of selected vulnerabilities for each application. The main difference between ManyBugs and our own constructed benchmark is that the subjects from ManyBugs include a huge number of test cases, while the subjects in our benchmark only have an exploit and few developer test cases. Note that ExtractFix is designed for working with a few cases.

The experiment is directly conducted on these vulnerable applications on a device with Intel Xeon CPU E5-2660 2.00GHz process (56 cores) 64G memory and 16.04 Ubuntu. We set timeout for the symbolic execution and program synthesis as 30 minutes each. Note that, we do not support parallelism yet. All the results are generated using sequential algorithms.

5.3 Experimental Results

5.3.1 How effective is ExtractFix in fixing vulnerabilities?

To answer RQ1, we evaluate the effectiveness of ExtractFix in the following three aspects: 1) extracting CFC 2) finding fix locations and 3) generating patches to fix vulnerabilities. Recall that the vulnerabilities are formalized as violations of constraints, we first evaluate whether ExtractFix can successfully extract such constraints for the given vulnerabilities. For the generated constraint, we generate the ground truth of correctness by manually analyzing the source code and root cause of the vulnerability. For instance, we manually analyze the condition that a buffer overflow can be triggered, and check the correctness of CFC. Given CFC, we then evaluate whether ExtractFix can find the correct fix locations by referring to the developer patches. As our dependency-based
Table 3. Evaluation results of ExtractFix. The first part (the first three rows) show the results on ManyBugs benchmark, and the second part present the results on our benchmark.

<table>
<thead>
<tr>
<th>Application</th>
<th>Defects</th>
<th>CFC</th>
<th>FL (T1/T3)</th>
<th>Patches</th>
<th>Correct Patches</th>
<th>Avg. Time (m)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Libtiff*</td>
<td>5</td>
<td>3</td>
<td>2 / 3</td>
<td>3</td>
<td>2</td>
<td>4.32</td>
</tr>
<tr>
<td>Lighttd</td>
<td>3</td>
<td>2</td>
<td>1 / 2</td>
<td>2</td>
<td>1</td>
<td>7.50</td>
</tr>
<tr>
<td>Php</td>
<td>18</td>
<td>14</td>
<td>6 / 10</td>
<td>14</td>
<td>9</td>
<td>11.11</td>
</tr>
<tr>
<td>Libtiff*</td>
<td>11</td>
<td>9</td>
<td>7 / 8</td>
<td>9</td>
<td>6</td>
<td>5.64</td>
</tr>
<tr>
<td>Binutils</td>
<td>2</td>
<td>2</td>
<td>1 / 1</td>
<td>2</td>
<td>1</td>
<td>26.28</td>
</tr>
<tr>
<td>Libxml</td>
<td>5</td>
<td>4</td>
<td>3 / 3</td>
<td>4</td>
<td>2</td>
<td>13.80</td>
</tr>
<tr>
<td>Libjpeg</td>
<td>4</td>
<td>3</td>
<td>1 / 2</td>
<td>3</td>
<td>2</td>
<td>12.01</td>
</tr>
<tr>
<td>FFmpeg</td>
<td>2</td>
<td>2</td>
<td>1 / 1</td>
<td>2</td>
<td>2</td>
<td>8.23</td>
</tr>
<tr>
<td>Jasper</td>
<td>2</td>
<td>2</td>
<td>1 / 1</td>
<td>2</td>
<td>1</td>
<td>1.07</td>
</tr>
<tr>
<td>Coreutil</td>
<td>4</td>
<td>2</td>
<td>1 / 2</td>
<td>2</td>
<td>2</td>
<td>5.17</td>
</tr>
<tr>
<td>Total</td>
<td>56</td>
<td>43</td>
<td>24 / 33</td>
<td>43</td>
<td>28</td>
<td>9.46</td>
</tr>
</tbody>
</table>

*Both Manybugs and our benchmark include the Libtiff program, but the defects in different benchmarks do not overlap.

Table 3 shows our evaluation results. The first part (first three rows) of Table 3 shows the results on ManyBugs benchmark and the second part gives the results on our own constructed subject. The effectiveness of ExtractFix is shown in columns 3-5, where CFC shows the number of correctly generated crash-free constraints in each application. FL represents fix localization results in a form of (T1/T3), where T1 is the number of bugs whose correct fix location is ranked first, and T3 is the number of bugs whose correct fix location is ranked in the top three candidates. Patches shows the number of fixed programs that pass the (single) failure-inducing test. The detailed evaluation result of each defect can be found in Table 4 (ManyBugs) and Table 5 (our benchmark).

Crash-free constraint extraction. Out of 56 vulnerabilities, ExtractFix can successfully extract correct constraints for 43 defects, and all of them are correct according to our manual investigation. The results show that our constraint extraction can effectively extract crash-free-constraints, especially for integer overflow, divide-by-zero and developer assertions. We cannot extract correct constraint for some buffer overflow vulnerabilities and null pointer dereferences because the
Table 4. Patches generated by ExtractFix on ManyBugs Benchmark. Column Sanitizer represents the sanitizer used by each defects, where APISan is a sanitizer implemented by ourselves to detect violation of API specification, e.g., the destination and source parameters should not overlap in memcpy. Column Template shows the template id (defined in Table 1) used by each vulnerability, while column CFC represents whether we can extract correct crash-free constraints. Column FL is the fault localization results, where L-N represents that we need to try N fix location candidates until find the correct one. Column Patched shows whether we can generate patches to pass the given tests, while Correct? gives the correctness of generated patches. Distance presents the distance between fix location and crash location.

<table>
<thead>
<tr>
<th>Subject</th>
<th>ID</th>
<th>Type</th>
<th>Sanitizer</th>
<th>Template</th>
<th>CFC</th>
<th>FL</th>
<th>Patched</th>
<th>Correct?</th>
<th>Distance</th>
<th>Time(m)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
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<td></td>
<td></td>
<td></td>
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<td></td>
<td></td>
</tr>
<tr>
<td>Libtiff</td>
<td>207c78a</td>
<td>ND</td>
<td>UBSan</td>
<td>T5</td>
<td>✓</td>
<td>L-1</td>
<td>Sem Equiv.</td>
<td>4</td>
<td>3.44</td>
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</tr>
<tr>
<td></td>
<td>0a36d7f</td>
<td>BO</td>
<td>Lowfat</td>
<td>T2</td>
<td>✓</td>
<td>L-3</td>
<td>Plausible</td>
<td>10</td>
<td>5.66</td>
<td></td>
</tr>
<tr>
<td></td>
<td>ee65c74</td>
<td>IO</td>
<td>UBSan</td>
<td>T3</td>
<td>✓</td>
<td>L-3</td>
<td>Plausible</td>
<td>10</td>
<td>5.66</td>
<td></td>
</tr>
<tr>
<td></td>
<td>865f7b2</td>
<td>BO</td>
<td>Lowfat</td>
<td>T2</td>
<td>✓</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td></td>
<td></td>
</tr>
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<td>ND</td>
<td>UBSan</td>
<td>T5</td>
<td>✓</td>
<td>L-1</td>
<td>Sem Equiv.</td>
<td>2</td>
<td>3.86</td>
<td></td>
</tr>
<tr>
<td>Lighttd</td>
<td>1914</td>
<td>BU</td>
<td>Lowfat</td>
<td>T2</td>
<td>✓</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td></td>
<td></td>
</tr>
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<td></td>
<td>2662</td>
<td>AS</td>
<td>Assert</td>
<td>T1</td>
<td>✓</td>
<td>L-3</td>
<td>Sem Equiv.</td>
<td>9</td>
<td>8.09</td>
<td></td>
</tr>
<tr>
<td></td>
<td>2786</td>
<td>BO</td>
<td>Lowfat</td>
<td>T2</td>
<td>✓</td>
<td>L-1</td>
<td>Plausible</td>
<td>7</td>
<td>6.91</td>
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<tr>
<td></td>
<td>5bb0a44e06</td>
<td>ND</td>
<td>UBSan</td>
<td>T5</td>
<td>✓</td>
<td>L-4</td>
<td>Plausible</td>
<td>10</td>
<td>16.23</td>
<td></td>
</tr>
<tr>
<td></td>
<td>426f51e790</td>
<td>AA</td>
<td>APISan</td>
<td>T4</td>
<td>✓</td>
<td>L-1</td>
<td>Syn Equiv.</td>
<td>2</td>
<td>14.31</td>
<td></td>
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<tr>
<td></td>
<td>2a9698e43a</td>
<td>BO</td>
<td>Lowfat</td>
<td>T2</td>
<td>✓</td>
<td>L-1</td>
<td>Sem Equiv.</td>
<td>2</td>
<td>12.09</td>
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</tr>
<tr>
<td></td>
<td>8deb11c0c3</td>
<td>ND</td>
<td>UBSan</td>
<td>T5</td>
<td>✓</td>
<td>L-1</td>
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<td>1</td>
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<td>UBSan</td>
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<td>L-2</td>
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<td>5</td>
<td>9.89</td>
<td></td>
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<tr>
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<td>T5</td>
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<td>L-1</td>
<td>Syn Equiv.</td>
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<td>-</td>
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<td>T5</td>
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<td>-</td>
<td>-</td>
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<td></td>
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<td>L-1</td>
<td>Sem Equiv.</td>
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<td>7.89</td>
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</tr>
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<td>APISan</td>
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<td>F</td>
<td>Plausible</td>
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<td>T5</td>
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<td>L-5</td>
<td>Sem Equiv.</td>
<td>32</td>
<td>10.24</td>
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<td>UBSan</td>
<td>T5</td>
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<td>F</td>
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<td>2</td>
<td>30.02</td>
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<td></td>
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<td>7</td>
<td>5.89</td>
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<td>47</td>
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<td>-</td>
<td>-</td>
<td></td>
<td></td>
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<td>cfa9e90b20</td>
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<td>UBSan</td>
<td>T5</td>
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<td>L-1</td>
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<td></td>
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<tr>
<td>Total</td>
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<td></td>
<td></td>
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<td>19</td>
<td>12 (avg) 8.1</td>
<td>9.6</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>


debugging information is ambiguous when symbolizing the condition enforced by sanitizers (the limitation of our prototype).

Fix localization. For the cases that we can extract correct constraints, we further evaluate the effectiveness of our fix localization. Out of 43 vulnerabilities, the correct fix locations of 24 defects are exactly the first candidate T1 recommended by our fix localization algorithm. The correct fix locations of 33 defects are correctly localized by looking into the top three candidates (T3).

Patch generation. Once constraints are correctly extracted and fix location candidates are determined, ExtractFix then generates patches via constraint propagation and program synthesis. Out of 56 vulnerabilities, ExtractFix can generate 43 patches. Those patches fix the bug by changing conditions, modifying the right-value of assignment or inserting an if-guard checker. For instance,
Table 5. Patches generated by ExtractFix. Column Sanitizer represents the sanitizer used by each defects, where APISan is a sanitizer implemented by ourselves to detect violation of API specification, e.g. the destination and source parameters should not overlap in memcpy. Column Template shows the template id (defined in Table 1) used by each vulnerability, while column CFC represents whether we can extract correct crash-free constraints. Column FL is the fault localization results, where L-N represents that we need to try N fix location candidates until find the correct one. Column Patched shows whether we can generate patches to pass the given tests, while Correct? gives the correctness of generated patches. Distance presents the distance between fix location and crash location.

<table>
<thead>
<tr>
<th>Subject</th>
<th>Vulnerability ID</th>
<th>Type</th>
<th>Sanitizer</th>
<th>Template</th>
<th>CFC</th>
<th>FL</th>
<th>Patched</th>
<th>Correct?</th>
<th>Distance</th>
<th>Time(m)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Libtiff</td>
<td>CVE-2016-5321</td>
<td>BO</td>
<td>Lowfat</td>
<td>T2</td>
<td>✓</td>
<td>L-1</td>
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<td>Syn Equiv.</td>
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<td>1.68</td>
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<td>T2</td>
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<td>L-1</td>
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<td>—</td>
<td>—</td>
<td>—</td>
</tr>
<tr>
<td></td>
<td>Bugzilla 2633</td>
<td>BO</td>
<td>Lowfat</td>
<td>T2</td>
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<td>L-5</td>
<td>✓</td>
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<td>—</td>
<td>—</td>
</tr>
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<td>T2</td>
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<td>✓</td>
<td>Plausible</td>
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<td>APISan</td>
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<td>✓</td>
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<td>L-1</td>
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<td>—</td>
</tr>
<tr>
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<td>UBSan</td>
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<td>✓</td>
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<td>L-1</td>
<td>✓</td>
<td>Sem Equiv.</td>
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<td>UBSan</td>
<td>T3</td>
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<td>F</td>
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<td>—</td>
</tr>
<tr>
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<td>T2</td>
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<td>-</td>
<td>X</td>
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<td>—</td>
<td>—</td>
</tr>
<tr>
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<td>CVE-2016-1838</td>
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<td>T2</td>
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<td>L-1</td>
<td>✓</td>
<td>—</td>
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<td>—</td>
</tr>
<tr>
<td></td>
<td>CVE-2012-5134</td>
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<td>Lowfat</td>
<td>T2</td>
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<td>T3</td>
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<td>L-1</td>
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<td>Lowfat</td>
<td>T2</td>
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<td>—</td>
<td>—</td>
</tr>
<tr>
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<td>CVE-2018-19664</td>
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<td>Lowfat</td>
<td>T2</td>
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<td>L-1</td>
<td>✓</td>
<td>—</td>
<td>—</td>
<td>—</td>
</tr>
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<td>UBSan</td>
<td>T3</td>
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<td>L-1</td>
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<td>—</td>
<td>—</td>
</tr>
<tr>
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<td>CVE-2012-2806</td>
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<td>T2</td>
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<td>L-3</td>
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<td>—</td>
<td>—</td>
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<td>APISan</td>
<td>T4</td>
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<td>—</td>
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<td>X</td>
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<td>—</td>
<td>—</td>
<td>—</td>
</tr>
<tr>
<td>Total</td>
<td>30</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td>24</td>
<td>24</td>
<td>16 (avg)4.0</td>
<td>(avg)9.3</td>
<td></td>
</tr>
</tbody>
</table>

BO: buffer overflow; BU: buffer underflow; IO: integer overflow; DZ: divide-by-zero; AA: API assert; ND: null pointer dereference

Beyond Tests: Program Vulnerability Repair via Crash Constraint Extraction

571 + if (nrows == 256) break;

Instead, ExtractFix fixes the bug by modifying the exit condition of while-loop, which is semantically equivalent to the developer patch:
Table 6. The number of patches and correct patches generated by Prophet, Angelix, Fix2Fit and ExtractFix. The first part (the first three rows) shows the results on ManyBugs benchmark, and the second part presents the results on our benchmark. In each subject, the tool that produces the most patches and the most correct patches is marked in bold.

<table>
<thead>
<tr>
<th>Program</th>
<th>#Vul</th>
<th>Total Patches</th>
<th>Correct Patches</th>
</tr>
</thead>
<tbody>
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<td></td>
<td></td>
<td>Prophet Angelix Fix2Fit ExtractFix</td>
<td>Prophet Angelix Fix2Fit ExtractFix</td>
</tr>
<tr>
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<td>5</td>
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<td>3</td>
</tr>
<tr>
<td>Lighttd</td>
<td>3</td>
<td>2</td>
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</tr>
<tr>
<td>Php</td>
<td>18</td>
<td>10</td>
<td>7</td>
</tr>
<tr>
<td>Libtiff</td>
<td>11</td>
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<td>7</td>
</tr>
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<td>Binutils</td>
<td>2</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>Libxml2</td>
<td>5</td>
<td>3</td>
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</tr>
<tr>
<td>Libjpeg</td>
<td>4</td>
<td>3</td>
<td>-</td>
</tr>
<tr>
<td>FFmpeg</td>
<td>2</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>Jasper</td>
<td>2</td>
<td>2</td>
<td>2</td>
</tr>
<tr>
<td>Coreutil</td>
<td>4</td>
<td>2</td>
<td>-</td>
</tr>
<tr>
<td>Total</td>
<td>56</td>
<td>31</td>
<td>21</td>
</tr>
</tbody>
</table>

567 - while (err >= limit)
567 + while (err >= limit && nrows < 256)

With this patch, it is guaranteed that the vulnerability cannot be triggered again. In our benchmark, once a correct constraint is generated, ExtractFix can always generate a patch.

**Multi-line fix** To fix the Libjpeg buffer overflow vulnerability of CVE-2012-2806, ExtractFix generates multiple-line fixes by changing two for-loop conditions.

**Comparison with state-of-the-art** We then compare the repairability of ExtractFix with Prophet, Angelix and Fix2Fit. We cannot run Angelix on some applications because the libraries (e.g. clang 2.9) used by Angelix no longer support the new versions of those applications. We did not run Fix2Fit on Libjpeg since it does not support the compilation using cmake. Prophet fails to build Binutils and FFmpeg. The columns 3-6 of Table 6 represent the number of patches generated by Prophet, Angelix, Fix2Fit and ExtractFix, respectively. Compared with Prophet and Angelix, ExtractFix generates the same or more patches for all the applications. Compared with Fix2Fit, ExtractFix generates more patches on Php, Libtiff, and Binutils, but less on Coreutils. This is because Fix2Fit generates plausible patches by efficiently searching from a large patch space and then uses fuzzing to rule out overfitted patches. In fact, our comparison with Fix2Fit is conservative in favor of Fix2Fit, since Fix2Fit’s fuzzing campaigns have an 8-hour timeout, while our program analysis based technique has a timeout of 1 hour (30 minutes for symbolic execution and 30 minutes for program synthesis). Even then, ExtractFix generates more plausible patches than Fix2Fit. More importantly, as we will see later, the patches generated by ExtractFix are of significantly higher quality than the patches from Fix2Fit.

Out of 56 vulnerabilities, ExtractFix extracts 43 correct constraints and generates 43 patches. ExtractFix generates more patches than Prophet, Angelix and Fix2Fit.

5.3.2 *Can ExtractFix alleviate the overfitting problem?*

The generated patch can handle the bug-triggering exploit, but it may overfit to the given exploit. To evaluate patch correctness, we take the developer patch as criteria and examine the patch
correctness by manually analyzing the developer patch. For each generated patch by \textsc{ExtractFix}, we check its syntactic and semantic equivalence with the developer patch by manually examining if the patch changes the program behavior in the same way as the developer patch.

In Table 3, column \textit{Correct Patch} gives the number or patches that are syntactically or semantically equivalent to developer patches. Out of the 43 patches, 28 patches are syntactically or semantically equivalent to developer patches, while 15 of them are plausible patches. We mark a patch as \textit{Plausible} if it partially fixes the vulnerability or changes program behavior differently compared to the developer patch. Plausible patches exist because (1) the \textit{CFC’} could be incomplete since backward propagation misses some paths between fix and crash location (e.g. paths inside \textit{for}, \textit{while} loop) (2) \textsc{ExtractFix} knows how to avoid triggering the vulnerability, but has narrow knowledge about the intended program behavior from developers. For instance, an integer overflow CVE-2017-7601 occurs when performing shift operation \((1L<<\text{bitssample})\) with \textit{bitssample} \(\geq 63\) (maximal positive signed long integer is \(2^{63} - 1\)). To fix this vulnerability, developers insert an if-checker \((\text{if} (\text{bitssample} > 16) \text{return } 0)\) before the crash line. With the guidance of crash free constraint \(\text{bitssample} < 63\), \textsc{ExtractFix} fix the bug by inserting \((\text{if} (\text{bitssample} \geq 63) \text{return } 0)\). The generated patch completely fixes the integer overflow, but may unintentionally modify the other program behaviors. While \textsc{ExtractFix} is designed to alleviate overfitting by completely fixing vulnerabilities, it may still change the program behavior in an unintended way.

We compare \textsc{ExtractFix} with Prophet, Angelix, and Fix2Fit for patch quality. The evaluation results are shown in Table 6, where columns 7-10 represent the number of correct patches generated by Prophet, Angelix, Fix2Fit, and \textsc{ExtractFix}, respectively. The test suite provided to repair tools is composed of the exploit and all available developer tests. Prophet, Angelix, and Fix2Fit are test-driven program repair tools, so the quality of patches generated by them highly depends on the quality of the test suite. For the defects from ManyBugs, test-driven program repair tools have a higher chance to generate correct patches since there are more available tests. On average, there are around 2.9k available tests for each defect from ManyBugs benchmarks (the first part of Table 6).\footnote{Around half of the 2.9k tests are irrelevant and will not drive the program to the fix locations. Even then, there are still a considerable number of useful tests in each subject.} All the test-driven program approaches generate a number of correct patches. Specifically, on the 26 defects, Prophet, Angelix, and Fix2Fit generate 7, 5, and 7 correct patches, respectively. Even then, \textsc{ExtractFix} generates much more (12) correct patches than all those approaches.

In our constructed benchmark (the second part of Table 6), the available tests are very limited, and only very few tests can cover the crash line. Therefore, the generated patches by these tools can easily overfit the given tests. Specifically, by manually checking the top patches against developer patches, only two patches generated by Prophet are correct and all the patches from Angelix overfit the failing tests. Fix2Fit can filter out some overfitted patches by test case generation, but the quality of the patches is not high as found by our experiments. Out of the 20 patches generated by Fix2Fit, only four patches are correct, while others still overfit the given test suite. In contrast, \textsc{ExtractFix} generates as many as 16 correct patches.

For bugs that are vulnerabilities supported by \textsc{ExtractFix}, \textsc{ExtractFix} outperforms Prophet, Angelix and Fix2Fit in generating patches that are both syntactically and semantically equivalent to developer patches.

5.3.3 How efficient is \textsc{ExtractFix} in generating patches?
Scalability is one of the most challenging problems of symbolic execution, hence semantic-based program repair. In our evaluation, we show that our approach can scale to real-world large applications, e.g. FFmpeg with 617K lines of codes. Meanwhile, the execution time to generate patches is
given in Table 3. On average, we only need 9.46 minutes to generate a patch, with a maximum of 41 minutes. Our approach is efficient because (1) our symbolic execution is only performed on a small partial program. As shown in Table 3 and 5, the averaged distance between fix and crash location is around 6, with maximum of 47. (2) our second-order program synthesis takes into account the distance between patch candidates with original expression and first evaluates candidates that are close to the original expression.

ExtractFix can scale to large programs, such as FFmpeg. On average, it takes 9.46 minutes to generate patches.

5.4 Threats to Validity

**Internal Validity** The main threat to internal validity is that ExtractFix performs backward propagation via symbolic execution which may miss some paths and result in incomplete constraint propagation. Fortunately, we only perform symbolic execution on a very small part of the program. What matters is that the incompleteness doesn’t seem to have a big impact on the effectiveness of the analysis. Another threat to internal validity is that we derive our CFC templates from frequently reported bugs and vulnerabilities, we note that our set of templates is not exhaustive. By extending CFC templates, ExtractFix can easily support fixing other kinds of bugs/vulnerabilities whose property violation is sanitizable and expressible as a simple formula. The last internal threat is that we perform a manual inspection of the experimental results which might be error-prone. To mitigate this, two authors of the paper double-checked the generated patches.

**External Validity** The main threat to external validity is that our selection of subjects may not generalize to other programs. We cannot evaluate ExtractFix on the dataset used in [15, 26, 49], because FootPatch fixes resource/memory leak (C/C++) and null pointer dereference (Java), a large part of defects in ManyBugs are logic bugs, and the exploits and fixes of some datasets (exploits) used by SENX are not available. Instead, we evaluate ExtractFix on a set of real programs and real CVEs to show its usability. In the future, it may be worthwhile to evaluate our approaches on more relevant CVEs and bugs.

6 RELATED WORK

In this section, we discuss the approaches that generate patches via semantic analysis and address the overfitting problem in program repair. For a general summarization of program repair techniques, the readers could refer to the overview articles [28, 44] or the surveys [13, 40].

**Generate and Validate Program Repair** Search-based approaches first generate a patch space and then search correct patch via meta-heuristic [27], random search [42], test-equivalence analysis [34] or learning approaches [33]. The correctness of patches is validated using the given test suites. Search-based program repair is able to generate high-quality patches and can easily scale to large programs. The weakness of search-based program repair comes from the incompleteness of test suites. Because of the incompleteness of test suites, the generated patches may overfit the given tests and can break untested functionality. Different from these approaches, ExtractFix uses symbolic analysis and reasoning to generate correct patches beyond tests.

**Semantic Program Repair** Semantics-based techniques like SemFix [41], Nopol [60], DirectFix [37], Angelix [38] and JFIX [23] generate patches in two steps. First, they formulate the requirement to pass all given tests as constraints for the identified program statements. Second, they synthesize a patch for these statements based on the inferred constraints. This type of approach is related to ExtractFix because these approaches also involve constraint extraction and patch synthesis. Semantics-based techniques extract constraints representing partial specifications to pass
the given tests. The inferred specifications lay out the requirement for the patch to pass the given test suite. In contrast, the constraints extracted by \textsc{ExtractFix} represent the underlying cause of the crash and the conditions that should be satisfied to fix vulnerabilities. Therefore, \textsc{ExtractFix} can alleviate the overfitting problem in automated program repair by generating patches that generalize beyond the given tests. Specifically, \textsc{ExtractFix} only needs a single exploit trace to generalize the vulnerability, where existing semantic repair techniques usually need a test-suite.

\textbf{Patch Ranking} One way of addressing overfitting in program repair is to rank patches according to statistical information learned from code repositories [39]. Typical approaches learn from existing patches [25, 33, 45], existing source code [58], or both [18, 54] to rank the patches in the order of likelihood to be correct. On the other hand, Xiong, et al. [57] propose to filter out the patches based on syntactic and semantic distance between patched and original program. Since these approaches are based on statistical information or heuristics, there is no guarantee that the generated patches can be generalized beyond tests. In contrast, our approach extracts crash-free constraints and ensures the constraint is satisfied on all tests.

\textbf{Patch Filtering} Several approaches [11, 56, 61] generate new test inputs to test the generated patches, and discard patches that result in crashes. On the other hand, Gao, et al. propose to provide the generated patches to developers for review in an interactive way [12]. Different from these approaches that perform a-posteriori filtering, our approach directly considers the crash-free constraint in the patch generation and ensures not to generate a patch violating the crash-free constraint.

\textbf{Static Program Repair} Instead of relying on test cases, several approaches propose program repair driven by static analysis and verification techniques. These approaches generate patches for static analysis violation by reasoning in separation logic [49] or learning repair strategies from the wild [1]. Specifically, the work of [49] generates patches that are guaranteed to satisfy certain heap properties (this covers few common bug types such as memory leaks, resource leaks or null de-reference). Different from our approach that is based on program synthesis to generate a patch, their approach is still search-based, where semantic search [20] is used to identify code snippets that satisfy the desired properties. Furthermore, the entire framework is based on the reasoning in separation logic and is used to fix heap properties only.

\textbf{Fix Localization in APR} Fix localization (FL) techniques determine a set of suspicious buggy statements for fixing, which is one of the key steps in automated program repair. Spectrum-based FL [43, 55] is widely used in existing APR which finds candidate fix locations by analyzing the execution trace of passing and failing tests. The FL results depend on the quality of the tests, but high-quality tests are not always available. According to a recent study [32], only a subset of bugs can be currently localized by Spectrum-based FL techniques. In contrast, our approach does not rely on complete test suites, and may only require a bug-trigger input. Instead of purely relying on test cases, existing techniques improve the fix localization by further utilizing bug report [21, 31] or deep learning approaches [30]. Our dependency-based fix localization is orthogonal to those approaches. Combining with those approaches may generate better fix localization results. Compared with \textsc{VFix} [59], which localizes buggy statements via value flow analysis for null pointer deference, our approach is more general and can be applied to other kinds of bugs.

\textbf{Reference Implementation} In many development scenarios, there exists a reference implementation, and the developers try to be compatible with the reference implementation while optimizing other aspects such as performance. For example, when implementing a Java compiler, OpenJDK is the reference implementation, and other implementations such as Jikes JVM tries to optimize the performance. Based on this observation, [36] proposes program repair with a reference implementation, where the reference implementation serves as an oracle to avoid overfitting. Compared with this approach, our approach does not need a reference implementation.
**Customized Program Repair** Some program repair approaches are designed to repair a specific type of bugs, such as fixing memory leaks [10, 29] or concurrency bugs [3, 19]. This type of work is related to ours because these approaches also assume the existence of a bug constraint and try to generate patches satisfying the constraint. In contrast, our work does not focus on a specific type of bug but tries to derive a general approach that works for any bug types where a bug constraint can be derived.

**Vulnerability Repair** The recent work SENX [15] aims to repair vulnerabilities using a combination of predicate generation, patch placement, and patch synthesis. The main difference with SENX is that SenX does not have any analytical understanding of which fix locations are suitable and what fixes to insert, and usually inserts trivial if-conditions to disable the crash at/near the crash location ([15] Table III). Besides, SENX does not perform any constraint propagation. In the absence of constraint propagation, SENX relies on heuristics to guide patch generation, which limits it to specific classes of bugs. In contrast, ExtractFix is not limited to certain vulnerabilities. Most of the patches generated by ExtractFix are more general and modify expressions/statements different from the crash location.

7 CONCLUSION

Overfitting of generated patches is a key challenge in automated program repair. Overfitting results from weak specifications, such as a test-suite, driving program repair. In this work, we have sought to tackle overfitting by directly extracting constraint specifications from an observed vulnerability. Even though the vulnerability is observed on a specific test input (the so-called exploit), our extracted constraint captures the "general reason" behind the vulnerability via symbolization. By propagating the extracted constraint from the crash location to other potential fix locations, we generate fixes via fix localization and patch synthesis. Our work thus goes beyond test-suite driven repair and provides a workflow and tool for exploring the fix space of common software security vulnerabilities as well.

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Beyond Tests: Program Vulnerability Repair via Crash Constraint Extraction


