IT5003 Semester 2 2024/2025 Data Structures and Algorithms

Tutorial 04 Priority Queue For Week 06 (Sat)/07 (Mon)

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1 Introduction and Objective

This tutorial marks the end of the first $\frac{1}{3}$ of IT5003: Basic Python, basic analysis of algorithms (Big O worst-case time complexity only), various sorting algorithms, and various linear Data Structures (DSes): Array (Python List)/Linked List/Stack/Queue/Doubly Linked List/Deque.

This tutorial marks the start of the next $\frac{1}{3}$ of IT5003: Various non-linear DSes. Today, we will discuss the Priority Queue (PQ) ADT with its Binary Heap implementation (use https://visualgo.net/en/heap to help you answer some questions in this tutorial).

Reminder for Saturday lab groups: This session will clash with Singapore National Olympiad in Informatics Prelim session, that Prof Halim also manage..., This NOI project will take several lab groups on that Saturday. If your class is affected, your Saturday lab TA will update you on the alternative venue.

2 Tutorial 04 Questions

Basic Binary Heap

Q1). Quick check: Let's review all basic operations of Binary Heap that are currently available in VisuAlgo (use the Exploration mode of http://visualgo.net/en/heap). During the tutorial session, the tutor will randomize the Binary Heap structure, ask student to compare Binary Tree versus (1-based) Compact Array mode, Insert(random-Integer) (you can try inserting duplicates, it is now allowed), perform ExtractMax() operations (once, K-times (i.e., partial sort), or N-times (i.e., HeapSort())), the $O(N \log N)$ or the O(N) Create(from-a-random-array), UpdateKey(i, newv) and Delete(i).

Q2). What is the minimum and maximum number of <u>comparisons</u> between Binary Heap elements required to construct a Binary (Max) Heap of arbitrary n elements using the O(n) Create(array)? Note that this question has been integrated in VisuAlgo Online Quiz, so it may appear in future Online Quizzes:).



Figure 1: Now automated:)

More Binary Heap

Q3). Give an algorithm to find all vertices that have value > x in a Binary max heap of size n. Your algorithm must run in O(k) time where k is the number of vertices in the output. Key lesson: This is a new algorithm analysis type for most of you as the time complexity of the algorithm does not depends on the input size n but rather the output size k:O...

Note that this question has also been integrated in VisuAlgo Online Quiz, so it may appear in future Online Quizzes:).

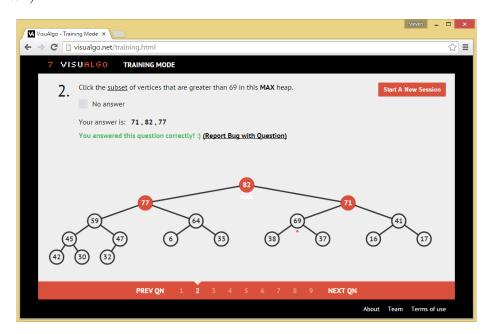


Figure 2: Also automated:)

Q4). Quick check: Show an easy way to convert a Binary Max Heap of a set Integers (as shown in VisuAlgo https://visualgo.net/en/heap?slide=9-4) into a Binary Min Heap (of the 'same' set of

Integers) without changing the underlying data structure at all. Hint: modify the data.

Q5). The <u>second</u> largest element in a max heap with more than two elements (to simplify this question, you can assume that all elements are unique) is always one of the children of the root. Is this true? If yes, show a simple proof. Otherwise, show a counter example.

Note that this kind of (simple) proof may appear in future CS2040/C/S written tests (unlikely asked to show proof in IT5003), so please refresh your CS1231/S (if you have taken that course) or just concentrate on how the tutor will answer this kind of question.

More ADT PQ Operations

Q6). There are two Binary Heap data structure features that are not available (yet) in C++ STL std::priority_queue, Python heapq, and Java PriorityQueue: Increase/Decrease/UpdateKey(old_v, new_v) and DeleteKey(v) where v is not necessarily the max element. These two operations are not yet included in VisuAlgo (the hidden slide https://visualgo.net/en/heap?slide=3-1) although the version where index i is known, is now included in VisuAlgo (see https://visualgo.net/en/heap?slide=9-5 and https://visualgo.net/en/heap?slide=9-6).

Q6a). Given https://www.comp.nus.edu.sg/~stevenha/cs2040/demos/BinaryHeapDemo.java||py (that is a Binary Max Heap), what should we modify/add so that we can implement DecreaseKey(old_v, new_lower_v) - notice that we never IncreaseKey?

Q6b). Given https://www.comp.nus.edu.sg/~stevenha/cs2040/demos/BinaryHeapDemo.java||py (that is a Binary Max Heap), what should we modify/add so that we can implement DeleteKey(v) where v is not necessarily the max element?

Hands-on 4

TA will run the second half of this session with a few to do list:

- IT5003: Very quick review of Python heapq
- Do a sample speed run of VisuAlgo online quiz that are applicable so far, e.g., https://visualgo.net/training?diff=Medium&n=5&tl=5&module=heap,
- Finally, live solve another chosen Kattis problem involving priority queue ADT.

Problem Set 3

We will end the tutorial with **another round of algorithmic** discussion of PS3 that will due soon (deferred to Mon, 03 Mar 25, 11.59pm, after Monday groups that day).