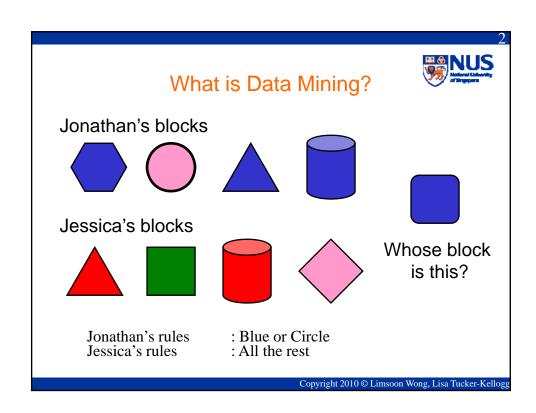
For written notes on this lecture, please read chapter 3 of The Practical Bioinformatician,

CS2220: Introduction to Computational Biology
Lecture 1: Essence of Knowledge Discovery

Lisa Tucker-Kellogg 14 January 2010 Slides thanks to Limsoon Wong 2009







## What is Data Mining?









Question: Can you explain how?

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## The Steps of Data Mining



- · Training data gathering
- Feature generation
  - k-grams, colour, texture, domain know-how, ...
- Feature selection
  - Entropy, χ2, CFS, t-test, domain know-how...
- Feature integration
  - SVM, ANN, PCL, CART, C4.5, kNN, ...

Some classifier/ methods

## What is Accuracy?



## What is Accuracy?



	predicted	predicted
	as positive	as negative
positive	TP	FN
negative	FP	TN

$$Accuracy = \frac{\text{No. of correct predictions}}{\text{No. of predictions}}$$
$$= \frac{\text{TP} + \text{TN}}{\text{TP} + \text{TN} + \text{FP} + \text{FN}}$$



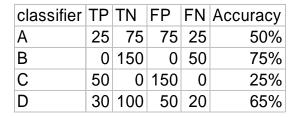
classifier	TP	TN	FP	FN	Accuracy
Α	25	25	25	25	50%
В	50	25	25	0	75%
С	25	50	0	25	75%
D	37	37	13	13	74%

- · Clearly, B, C, D are all better than A
- Is B better than C, D?
- Is C better than B, D?
- Is D better than B, C?

Accuracy may not tell the whole story

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## Examples (Unbalanced Population



- Clearly, D is better than A
- Is B better than A, C, D?

Exercise: What is B's Prediction strategy?

High accuracy is meaningless if population is unbalanced



	predicted	predicted
	as positive	as negative
positive	TP	FN
negative	FP	TN

Sensitivity = 
$$\frac{\text{No. of correct positive predictions}}{\text{No. of positives}}$$
$$= \frac{\text{TP}}{\text{TP} + \text{FN}}$$

Sometimes sensitivity wrt negatives is termed specificity

Exercise: Write down the formula for specificity

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#### What is Precision?



	predicted	predicted
	as positive	as negative
positive	TP	FN
negative	FP	TN

$$\frac{\text{Precision}}{\text{wrt positives}} = \frac{\text{No. of correct positive predictions}}{\text{No. of positives predictions}}$$
$$= \frac{\text{TP}}{\text{TP} + \text{FP}}$$



classifier	TP	TN	FP	FN	Accuracy	Sensitivity	Precision
Α	25	75	75	25	50%	50%	25%
В	0	150	0	50	75%		
С	50	0	150	0	25%		
D	30	100	50	20	65%	60%	38%

- What are the senstivity and precision of B and C?
- Is B better than A, C, D?

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## Abstract Model of a Classifier



- Given a test sample S
- Compute scores p(S), n(S)
- Predict S as negative if p(S) < t \* n(s)
- Predict S as positive if  $p(S) \ge t * n(s)$

t is the decision threshold of the classifier

changing *t* affects the recall and precision, and hence accuracy, of the classifier



## An Example

ສ	P(S)	N(S)	Actual	Predicted	Predicted
			Class	Class	Class
				0 t = 3	0 t = 2
2	0.961252	0.038748	P	Р	P
3	0.435302	0.564698	N	N	N
6	0.691596	0.308404	P	N	P
7	0.180885	0.819115	N	N	N
8	0.814909	0.185091	P	P	P
10	0.887220	0.112780	P	P	P
			accuracy	3/6	6/6
			recall	3 / 4	4/4
			precision	3 / 3	4/4

#### Recall that ...

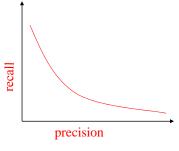
- Predict S as negative if p(S) < t \* n(s)
- Predict S as positive if  $p(S) \ge t * n(s)$

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#### Precision-Recall Trade-off

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- A predicts better than B if A has better recall and precision than B
- There is a trade-off between recall and precision
- In some applications, once you reach a satisfactory precision, you optimize for recall
- In some applications, once you reach a satisfactory recall, you optimize for precision



Exercise: Why is there a trade off betw recall and precision?



- · Accuracy is the obvious measure
  - But it conveys the right intuition only when the positive and negative populations are roughly equal in size
- Recall and precision together form a better measure
  - But what do you do when A has better recall than B and B has better precision than A?

So let us look at some alternate measures ....

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## F-Measure (Used in Info Extraction)

Take the harmonic mean of recall and precision

$$F = \frac{2 * recall * precision}{recall + precision}$$
 (wrt positives)

classifier	TP	TN	FP	FN	Accuracy	F-measure
Α	25	75	75	25	50%	33%
В	0	150	0	50	75%	undefined
С	50	0	150	0	25%	40%
D	30	100	50	20	65%	46%

Does not accord with intuition:

C predicts everything as +ve, but still rated better than A



### **Adjusted Accuracy**

• Weigh by the importance of the classes

Adjusted accuracy = 
$$\alpha$$
 \* Sensitivity +  $\beta$  \* Specificity where  $\alpha + \beta = 1$  typically,  $\alpha = \beta = 0.5$ 

classifier	TP	TN	FP	FN	Accuracy	Adj Accuracy
Α	25	75	75	25	50%	50%
В	0	150	0	50	75%	50%
С	50	0	150	0	25%	50%
D	30	100	50	20	65%	63%

But people can't always agree on values for  $\alpha$ ,  $\beta$ 

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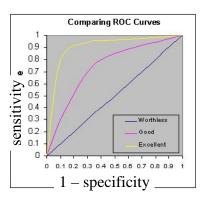
## **ROC Curves**

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- By changing t, we get a range of sensitivities and specificities of a classifier
- A predicts better than B if A has better sensitivities than B at most specificities
- Leads to ROC curve that plots sensitivity vs. (1 – specificity)

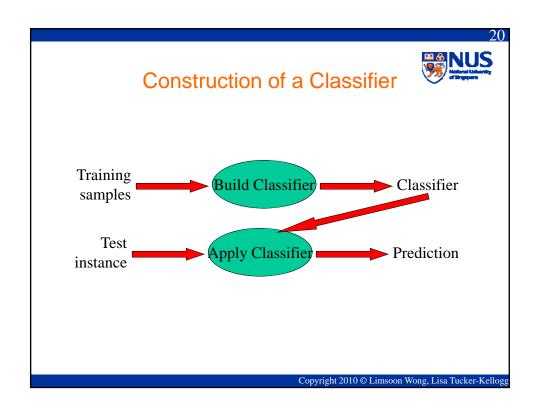
Exercise: Draw a typical curve of sensitivity vs specificity

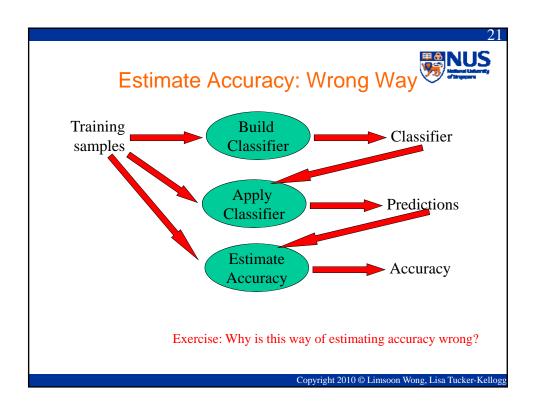
 Then the larger the area under the ROC curve, the better



## What is Cross Validation?







#### Recall ...



#### ...the abstract model of a classifier

- Given a test sample S
- Compute scores p(S), n(S)
- Predict S as negative if p(S) < t \* n(s)
- Predict S as positive if p(S) ≥ t \* n(s)

t is the decision threshold of the classifier



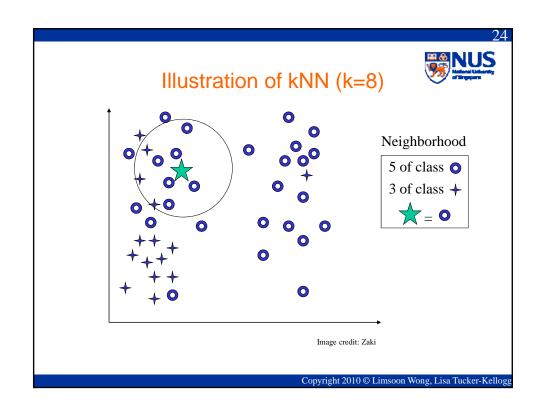
## K-Nearest Neighbour Classifier (k-N

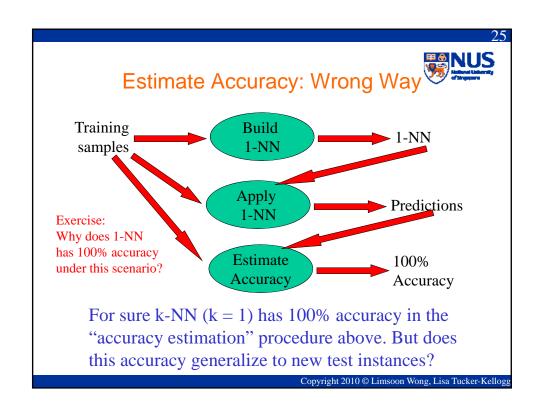
- Given a sample S, find the k observations S<sub>i</sub> in the known data that are "closest" to it, and average their responses
- Assume S is well approximated by its neighbours

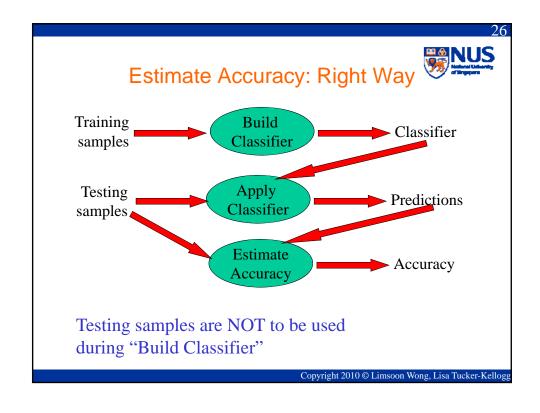
$$p(S) = \sum_{S_i \in N_k(S) \cap D^p} 1 \qquad n(S) = \sum_{S_i \in N_k(S) \cap D^N} 1$$

where  $N_k(S)$  is the neighbourhood of S defined by the k nearest samples to it.

Assume distance between samples is Euclidean distance for now





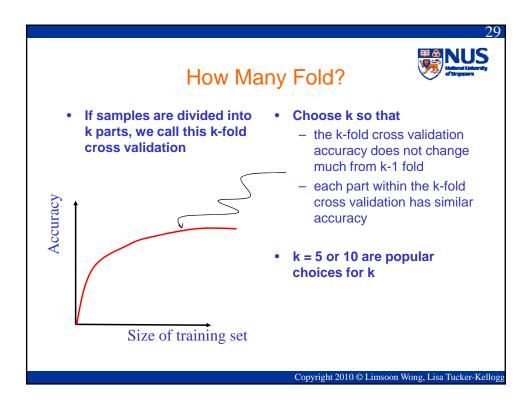


# How Many Training and Testing Samples?

- No fixed ratio between training and testing samples; but typically 2:1 ratio
- Proportion of instances of different classes in testing samples should be similar to proportion in training samples
- What if there are insufficient samples to reserve 1/3 for testing?
- Ans: Cross validation

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#### **Cross Validation Divide samples** 2.Train 3.Train 4.Train 5.Train into k roughly equal parts 3.Train 4.Train 5.Train 1.Train 2.Test Each part has similar proportion .Train 2.Train 4.Train 5.Train of samples from different classes 1.Train 2.Train 3.Train 4.Test Use each part to 1.Train 2.Train 3.Train 4.Train test other parts **Total up accuracy** Copyright 2010 © Limsoon Wong, Lisa Tucker-Kellog



#### Bias and Variance



Suppose a butcher weighs a steak with his thumb on the scale. That causes an error in the measurement, but little has been left to chance. Take another example. Suppose a drapery store uses a cloth tape measure which has stretched from 36 inches to 37 inches in length. Every "yard" of cloth they sell to a customer has an extra inch tacked onto it. This isn't a chance error, because it always works for the customer. The butcher's thumb and the stretched tape are two examples of bias, or systematic error.

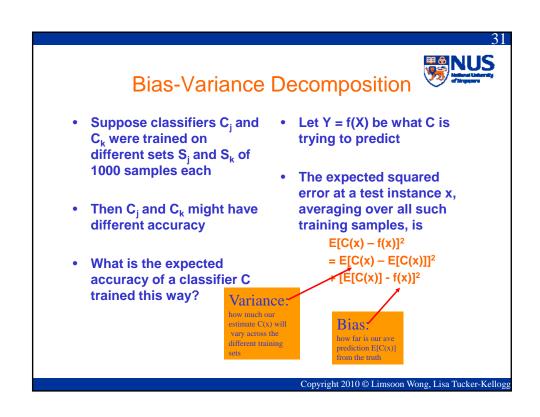
Bias affects all measurements the same way, pushing them in the same direction. Chance errors change from measurement to measurement, sometimes up and sometimes down.

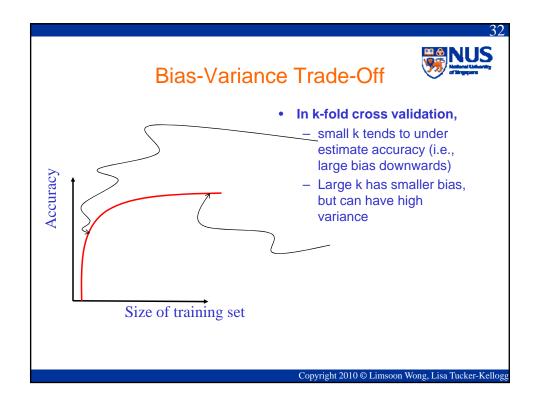
The basic equation has to be modified when each measurement is thrown off by bias as well as chance error:

individual measurement = exact value + bias + chance error.

If there is no bias in a measurement procedure, the long-run average of repeated measurements should give the exact value of the thing being measured: the

Source: Freedman et al., Statistics, Norton, 1998





## **Curse of Dimensionality**



## Recall ...



- ...the abstract model of a classifier
  - Given a test sample S
  - Compute scores p(S), n(S)
  - Predict S as negative if p(S) < t \* n(s)</li>
  - Predict S as positive if p(S) ≥ t \* n(s)

t is the decision threshold of the classifier





## K-Nearest Neighbour Classifier (k-N

- Given a sample S, find the k observations S<sub>i</sub> in the known data that are "closest" to it, and average their responses
- Assume S is well approximated by its neighbours

$$p(S) = \sum_{S_i \in N_k(S) \cap D^p} 1 \qquad n(S) = \sum_{S_i \in N_k(S) \cap D^N} 1$$

where  $N_k(S)$  is the neighbourhood of S defined by the k nearest samples to it.

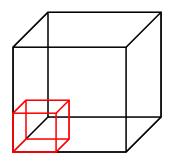
Assume distance between samples is Euclidean distance for now

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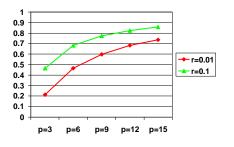
## **Curse of Dimensionality**



 How much of each dimension is needed to cover a proportion r of total sample space?



- Calculate by e<sub>p</sub>(r) = r<sup>1/p</sup>
- So, to cover 10% of a 15-D space, need 85% of each dimension!



Exercise: Why  $e_p(r) = r^{1/p}$ ?



## Consequence of the Curse

- Suppose the number of samples given to us in the total sample space is fixed
- Let the dimension increase
- Then the distance of the k nearest neighbours of any point increases
- Then the k nearest neighbours are less and less useful for prediction, and can confuse the k-NN classifier

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What is Feature Selection?





#### Tackling the Curse

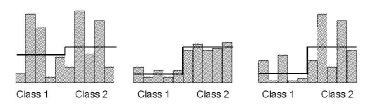
- Given a sample space of p dimensions
- It is possible that some dimensions are irrelevant
- Need to find ways to separate those dimensions (aka features) that are relevant (aka signals) from those that are irrelevant (aka noise)

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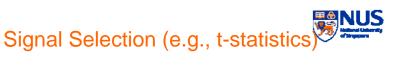
## Signal Selection (Basic Idea)



- Choose a feature w/ low intra-class distance
- Choose a feature w/ high inter-class distance



Exercise: Name 2 well-known signal selection statistics



The t-state of a signal is defined as

$$t = \frac{|\mu_1 - \mu_2|}{\sqrt{(\sigma_1^2/n_1) + (\sigma_2^2/n_2)}}$$

where  $\sigma_i^2$  is the variance of that signal in class i,  $\mu_i$  is the mean of that signal in class i, and  $n_i$  is the size of class i.

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#### Self-fulfilling Oracle

- Construct artificial dataset with 100 samples, each with 100,000 randomly generated features and randomly assigned class labels
- Select 20 features with the best t-statistics (or other methods)
- Evaluate accuracy by cross validation using only the 20 selected features
- The resultant estimated accuracy can be ~90%
- But the true accuracy should be 50%, as the data were derived randomly



## What Went Wrong?

- The 20 features were selected from the whole dataset
- Information in the held-out testing samples has thus been "leaked" to the training process
- The correct way is to re-select the 20 features at each fold; better still, use a totally new set of samples for testing

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## **Concluding Remarks**





#### What have we learned?

- Methodology of data mining
  - Feature generation, feature selection, feature integration
- Evaluation of classifiers
  - Accuracy, sensitivity, precision
  - Cross validation
- Curse of dimensionality
  - Feature selection concept
  - Self-fulfilling oracle

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## Any Questions?





#### Acknowledgements

- The first two slides were shown to Prof. Wong 10+ years ago by Tan Ah Hwee
- These slides were assembled by Prof. Wong during years of teaching CS2220

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#### References

- John A. Swets, Measuring the accuracy of diagnostic systems, *Science* 240:1285--1293, June 1988
- Trevor Hastie et al., *The Elements of Statistical Learning: Data Mining, Inference, and Prediction*, Springer, 2001. Chapters 1, 7
- Lance D. Miller et al., Optimal gene expression analysis by microarrays, *Cancer Cell* 2:353--361, 2002
- David Hand et al., Principles of Data Mining, MIT Press, 2001
- Jinyan Li et al., Data Mining Techniques for the Practical Bioinformatician, The Practical Bioinformatician, Chapter 3, pages 35—70, WSPC, 2004