

For written notes on this lecture, please read chapter 19 of *The Practical Bioinformatician* and *Hawkins & Kihara, JBCB 5(1):1-30, 2007*

CS2220: Introduction to Computational Biology

Lecture 6: Sequence Homology Interpretation

Limsoon Wong



Plan

- **Recap of sequence alignment**
- **Guilt by association**
- **Active site/domain discovery**
- **What if no homology of known function is found?**
 - Genome phylogenetic profiling
 - SVM-Pairwise
 - Protein-protein interactions
- **Key mutation site discovery**

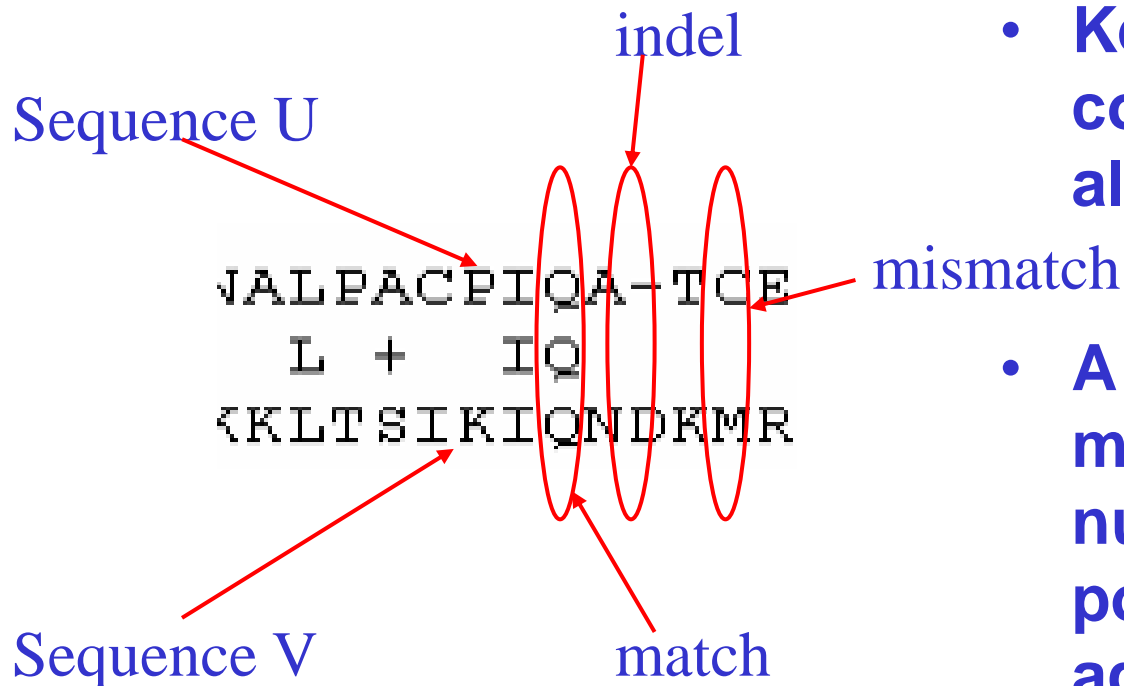
Very Brief Recap of Sequence Comparison/Alignment



Motivations for Sequence Comparison

- **DNA is blue print for living organisms**
 - ⇒ **Evolution is related to changes in DNA**
 - ⇒ **By comparing DNA sequences we can infer evolutionary relationships between the sequences w/o knowledge of the evolutionary events themselves**
- **Foundation for inferring function, active site, and key mutations**

Sequence Alignment



- Key aspect of seq comparison is seq alignment
- A seq alignment maximizes the number of positions that are in agreement in two sequences

Sequence Alignment: Poor Example

- Poor seq alignment shows few matched positions
 ⇒ The two proteins are not likely to be homologous

Alignment by FASTA of the sequences of amicyanin and domain 1 of ascorbate oxidase

```

                60          70          80          90          100
Amicyanin      MPHNVHVFVAGVLGEAALKGPMMKKEQAYSLTFTEAGTYDYHCTPHPFMRGKVVVE
                ...: . :... ::
Ascorbate Oxidase ILQRGTPWADGTASISQCAINPGETFFYNFTVDNPGTFFYHGHLMQRSAGLYGSLI
                70          80          90          100          110          120
  
```

No obvious match between
 Amicyanin and Ascorbate Oxidase

Sequence Alignment: Good Example

- **Good alignment usually has clusters of extensive matched positions**
- ⇒ **The two proteins are likely to be homologous**

```

□ >gil13476732|ref|NP\_108301.1| unknown protein [Mesorhizobium loti]
   gil14027493|dbj|BAB53762.1| unknown protein [Mesorhizobium loti]
      Length = 105
  
```

```
Score = 105 bits (262), Expect = 1e-22
```

```
Identities = 61/106 (57%), Positives = 73/106 (68%), Gaps = 1/106 (0%)
```

```

Query: 1   MKPGRLASIALAIIFLPMAVPAHAATIEITMENLVISPTEVSAKVGDTIRWVNKDVFAHT 60
          MK G L  ++           MA PA AATIE+T++ LV SP  V AKVGDTI WVN DV AHT
Sbjct: 1   MKAGALIRLSWLAALALMAAPAAAATIEVTIDKLVFSPATVEAKVGDTIEWVNNDVVAHT 60
  
```

good match between
 Amicyanin and unknown M. loti protein

Multiple Alignment: An Example

- Multiple seq alignment maximizes number of positions in agreement across several seqs
- seqs belonging to same “family” usually have more conserved positions in a multiple seq alignment

```

gi|126467|      FHFTSWPDFGVPFTP I GMLKFLKKVKACNP--QYAGAI V V HCSA GVGRTGTFVVIDAML D
gi|2499753     FHFTGWPDHGVPYHATGLLSF I RRVKLSNP--PSAGPI V V HCSA GAGRTGCIYIVIDIMLD
gi|462550|     YHYTQWPDMGVPEYALPVLTFVRRSSAARM--PETGPVI V V HCSA GVGRTGTIYIVIDSMLQ
gi|2499751     FHFTSWPDHGVPD TTDLL I NFRYLVRDYMKQSPPE S P I L V HCSA GVGRTGTF I AIDRLIY
gi|1709906     FQFTA WPDHGVP EHP T PFLAFLRRVKTCNP--PDAGPM V V HCSA GVGRTGCF IVIDAMLE
gi|126471|     LHFTSWPDFGVPFTP I GMLKFLKKVKTLNP--VHAGPI V V HCSA GVGRTGTF IVIDAMMA
gi|548626|     FHFTGWPDHGVPYHATGLLSF I RRVKLSNP--PSAGPI V V HCSA GAGRTGCIYIVIDIMLD
gi|131570|     FHFTGWPDHGVPYHATGLLGFVRQVKS KSP--PNAGPL V V HCSA GAGRTGCF IVIDIMLD
gi|2144715     FHFTSWPDHGVPD TTDLL I NFRYLVRDYMKQSPPE S P I L V HCSA GVGRTGTF I AIDRLIY
..*  ***  ***      .  *      ..*****  *****  ** ..

```

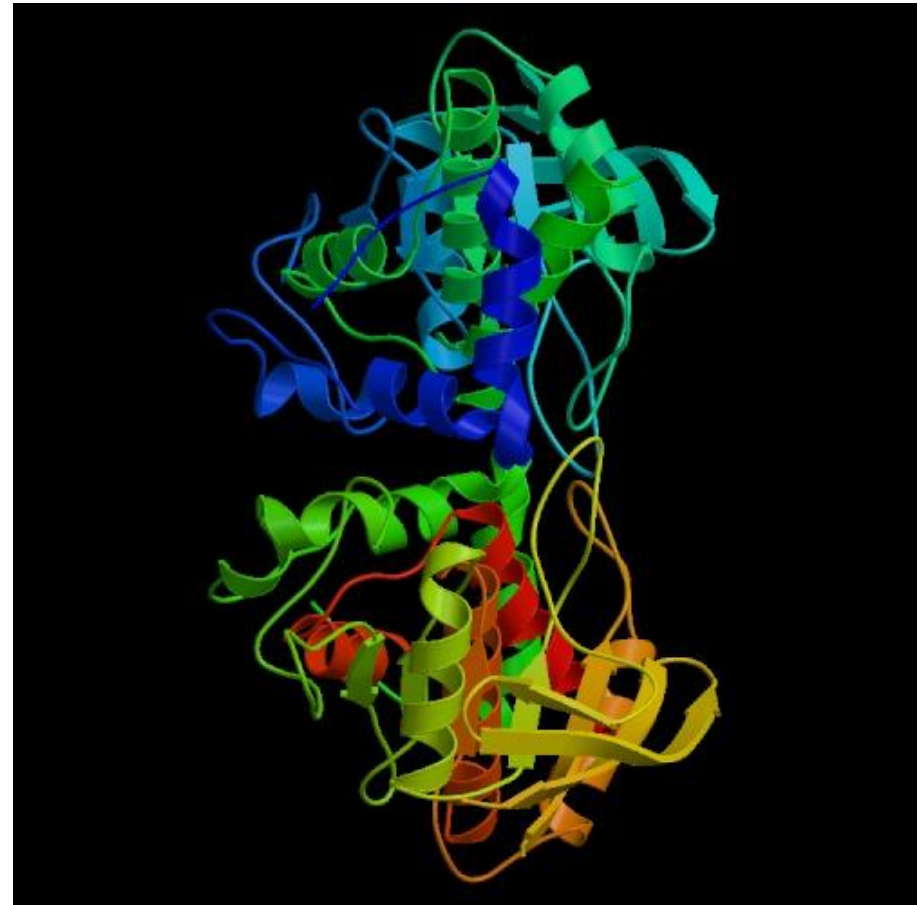
Conserved sites

Application of Sequence Comparison: Guilt-by-Association



A protein is a ...

- A protein is a large complex molecule made up of one or more chains of amino acids
- Protein performs a wide variety of activities in the cell



Function Assignment to Protein Sequence

SPSTNRKYPPPLPVDKLEEEINRRMADDNKLFREEFNALPACPIQATCEAASKEENKEKNR
YVNILPYDHSRVHLTPVEGVPDSYINASFINGYQEKNKFIAAQGPKEETVNDFWMIWE
QNTATIVMVTNLKERKECKCAQYWPDQGCWTYGNVRVSVEDVTVLVDYTVRKFCIQQVGD
VTNRKPQRLITQFHFTSWPDFGVPFTPIGMLKFLKKVKACNPQYAGAIVVHCSAGVGRTG
TFVVIDAMLDMMSERKVDVYGFVSRIRAQRQCMVQTDMQYVFYQALLEHYLYGDTELE
VT

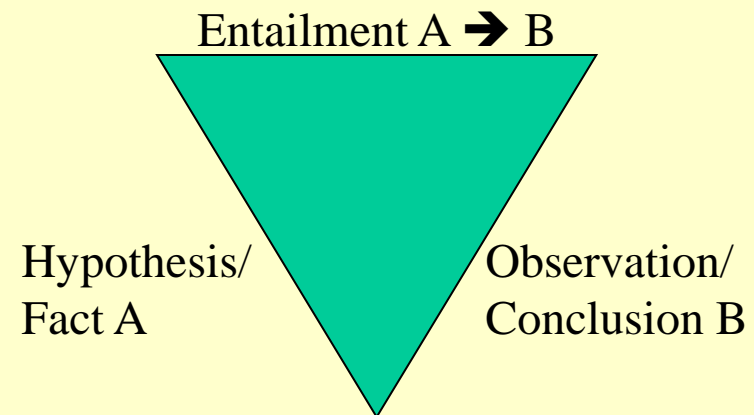
- **How do we attempt to assign a function to a new protein sequence?**

Invariant and Abductive Reasoning

- **Function is determined by 3D struct of protein & environment protein is in**
- **Constraints imposed by 3D struct & environment give rise to “invariant” properties observed in proteins having the ancestor with that function**

⇒ **Abductive reasoning**

- If those invariant properties are seen in a protein, then the protein is homolog of this protein



⇒ **“Guilt by association”**

Guilt-by-Association

- **Compare the target sequence T with sequences S_1, \dots, S_n of known function in a database**
- **Determine which ones amongst S_1, \dots, S_n are the mostly likely homologs of T**
- **Then assign to T the same function as these homologs**
- **Finally, confirm with suitable wet experiments**

Guilt-by-Association

Compare T with seqs of known function in a db

Poor Sequence Alignment

- Poor seq alignment shows few matched positions
 \Rightarrow The two proteins are not likely to be homologous

Alignment by FASTA of the sequences of amicyanin and domain 1 of ascorbate oxidase

```

Amicyanin      60      70      80      90     100
MPHNVHFVAGVLGSAALKGPMMKKEQAYSLSLTFTEAGTYDYHCTPHFFMRGKVVV
                .:. .:. .:. .:
Ascorbate Oxidase ILQRGTPWADGTASISQCAINPGE7FFYNFPVDNPGTFFYHGHLGMORSAGLYG
                70      80      90     100     110
  
```

No obvious match between Amicyanin and Ascorbate Oxidase

Discard this function as a candidate

Good Sequence Alignment

- Good alignment usually has clusters of extensive matched positions
 \Rightarrow The two proteins are likely to be homologous

```

>gi113476732|ref|NP_108301.1| unknown protein [Mesorhizobium loti]
gi114027493|dbj|BAE53762.1| unknown protein [Mesorhizobium loti]
Length = 105

Score = 105 bits (262), Expect = 1e-22
Identities = 61/106 (57%), Positives = 73/106 (68%), Gaps = 1/106 (0%)

Query: 1 MKPORLASIALAIIFLPMVFAHAATIEITMENLVISPTIEVSAKVVDITRWNKDVFAHT 60
      MK G L ++ MA PA AATIE+T++ LV SP V AKVGDIT WVN DV AHT
Sbjct: 1 MKAGALIELSLAALALMAFAAAATIEVTIDKLVFSPATVEAKVGDITIEWRNDVVAHT 60
  
```

good match between Amicyanin and unknown M. loti protein

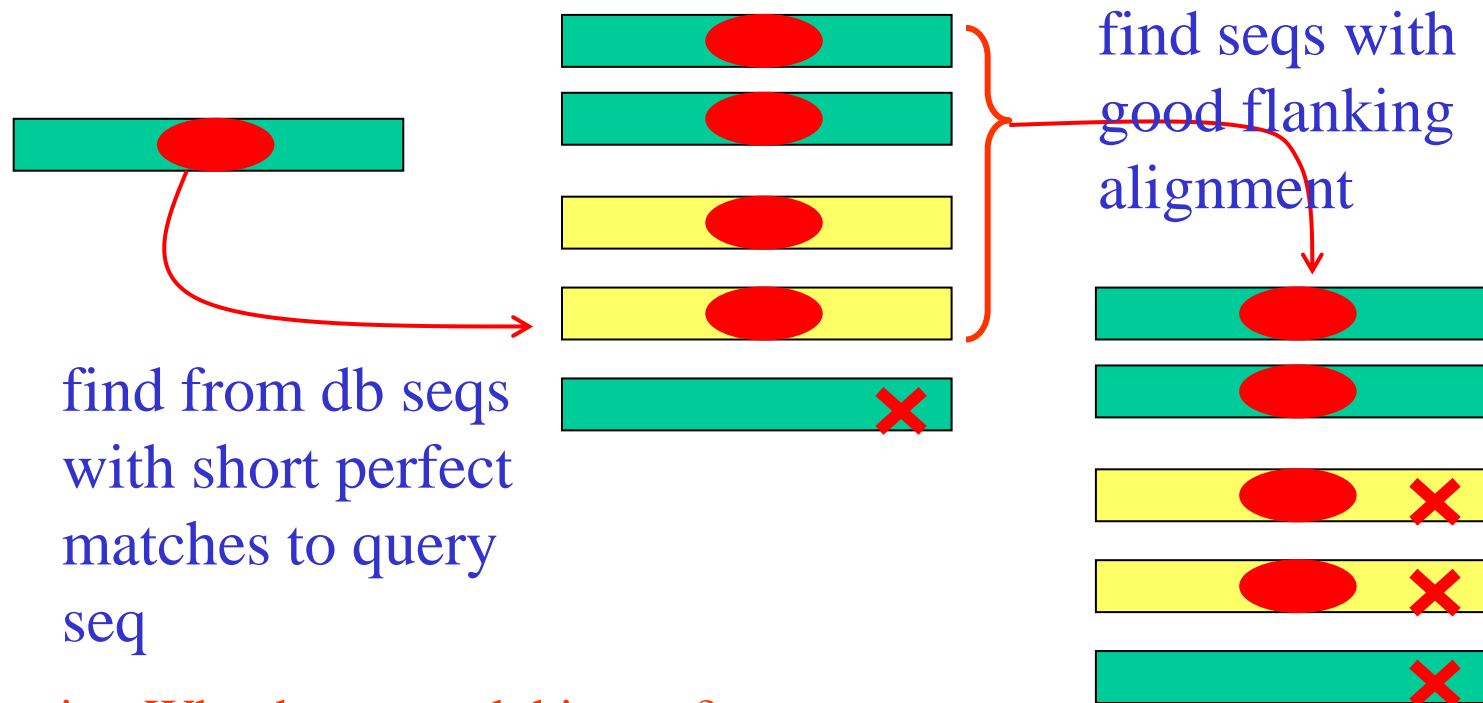
Assign to T same function as homologs

Confirm with suitable wet experiments

BLAST: How It Works

Altschul et al., *JMB*, 215:403--410, 1990

- **BLAST is one of the most popular tool for doing “guilt-by-association” sequence homology search**



Exercise: Why do we need this step?

Homologs obtained by BLAST

Sequences producing significant alignments:	Score (bits)	E Value
gi 14193729 gb AAK56109.1 AF332081_1 protein tyrosin phosph...	621 L	e-177
gi 126467 sp P18433 PTRA_HUMAN Protein-tyrosine phosphatase...	621 L	e-177
gi 4506303 ref NP_002827.1 protein tyrosine phosphatase, r...	621 L	e-176
gi 227294 prf 1701300A protein Tyr phosphatase	620	e-176
gi 18450369 ref NP_543030.1 protein tyrosine phosphatase, ...	621 L	e-176
gi 32067 emb CAA37447.1 tyrosine phosphatase precursor [Ho...	611 L	e-176
gi 285113 pir JC1285 protein-tyrosine-phosphatase (EC 3.1....	619	e-176
gi 6981446 ref NP_036895.1 protein tyrosine phosphatase, r...	611 L	e-176
gi 2098414 pdb 1YFO A Chain A, Receptor Protein Tyrosine Ph...	61 S	e-174
gi 32313 emb CAA38662.1 protein-tyrosine phosphatase [Homo...	61 L	e-174
gi 450583 gb AAB04150.1 protein tyrosine phosphatase >gi 4...	605	e-172
gi 6679557 ref NP_033006.1 protein tyrosine phosphatase, r...	60 L	e-172
gi 483922 gb AAA17990.1 protein tyrosine phosphatase alpha	599	e-170

- Thus our example sequence could be a protein tyrosine phosphatase α (PTP α)

Example Alignment with PTP α

Score = 632 bits (1629), Expect = e-180
 Identities = 294/302 (97%), Positives = 294/302 (97%)

```

Query: 1   SPSTNRKYPPLPVDKLEEE INRRMADDNKLFREEFNALPACPIQATCEAASXXXXXXXXXR 60
          SPSTNRKYPPLPVDKLEEE INRRMADDNKLFREEFNALPACPIQATCEAAS      R
Sbjct: 202 SPSTNRKYPPLPVDKLEEE INRRMADDNKLFREEFNALPACPIQATCEAASKEENKEKNR 261

Query: 61  YVNILPYDHSRVHLTPVEGVVSDYINASF INGYQEKNKF IAAQGPKEETVNDFWRMIWE 120
          YVNILPYDHSRVHLTPVEGVVSDYINASF INGYQEKNKF IAAQGPKEETVNDFWRMIWE
Sbjct: 262 YVNILPYDHSRVHLTPVEGVVSDYINASF INGYQEKNKF IAAQGPKEETVNDFWRMIWE 321

Query: 121 QNTATIVMVTNLKERKECKCAQYWPDQGCWTYGNVRVSVEDVTVLVDYTVRKFC IQQVGD 180
          QNTATIVMVTNLKERKECKCAQYWPDQGCWTYGNVRVSVEDVTVLVDYTVRKFC IQQVGD
Sbjct: 322 QNTATIVMVTNLKERKECKCAQYWPDQGCWTYGNVRVSVEDVTVLVDYTVRKFC IQQVGD 381

Query: 181 VTRKPKQLITQFHFTSWPDFGVVFTPIGMLKFLKKVKACNPQYAGAI VVHCSAGVGRTG 240
          VTRKPKQLITQFHFTSWPDFGVVFTPIGMLKFLKKVKACNPQYAGAI VVHCSAGVGRTG
Sbjct: 382 VTRKPKQLITQFHFTSWPDFGVVFTPIGMLKFLKKVKACNPQYAGAI VVHCSAGVGRTG 441

Query: 241 TFVVIDAMLDMHSEKVDVYGFVSRIRAQRCQMVQTD MQYVF IYQALLEHYLYGDTELE 300
          TFVVIDAMLDMHSEKVDVYGFVSRIRAQRCQMVQTD MQYVF IYQALLEHYLYGDTELE
Sbjct: 442 TFVVIDAMLDMHSEKVDVYGFVSRIRAQRCQMVQTD MQYVF IYQALLEHYLYGDTELE 501
  
```

Guilt-by-Association: Caveats

- **Ensure that the effect of database size has been accounted for**
- **Ensure that the function of the homology is not derived via invalid “transitive assignment”**
- **Ensure that the target sequence has all the key features associated with the function, e.g., active site and/or domain**

Law of Large Numbers

- Suppose you are in a room with 365 other people
- Q: What is the prob that a specific person in the room has the same birthday as you?
- A: $1/365 = 0.3\%$
- Q: What is the prob that there is a person in the room having the same birthday as you?
- A: $1 - (364/365)^{365} = 63\%$
- Q: What is the prob that there are two persons in the room having the same birthday?
- A: 100%

Interpretation of P-value

- Seq. comparison progs, e.g. BLAST, often associate a P-value to each hit
 - P-value is interpreted as prob that a random seq has an equally good alignment
 - Suppose the P-value of an alignment is 10^{-6}
 - If database has 10^7 seqs, then you expect $10^7 * 10^{-6} = 10$ seqs in it that give an equally good alignment
- ⇒ Need to correct for database size if your seq comparison prog does not do that!

Note: $P = 1 - e^{-E}$

Exercise: Name a commonly used method for correcting p-value for a situation like this

Lightning Does Strike Twice!

- **Roy Sullivan, a former park ranger from Virginia, was struck by lightning 7 times**
 - 1942 (lost big-toe nail)
 - 1969 (lost eyebrows)
 - 1970 (left shoulder seared)
 - 1972 (hair set on fire)
 - 1973 (hair set on fire & legs seared)
 - 1976 (ankle injured)
 - 1977 (chest & stomach burned)
- **September 1983, he committed suicide**



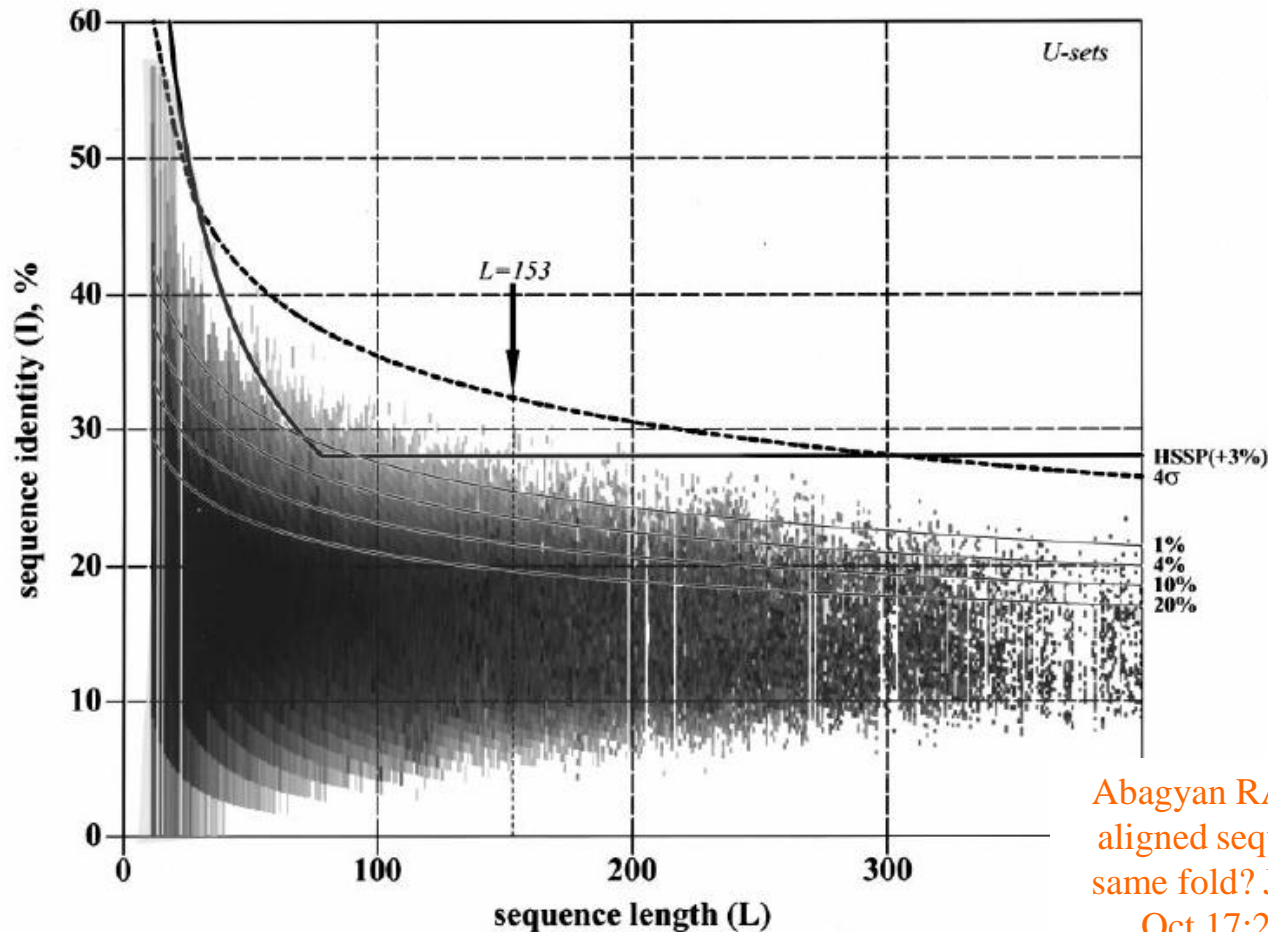
Cartoon: Ron Hipschman
Data: David Hand

Effect of Seq Compositional Bias

- **One fourth of all residues in protein seqs occur in regions with biased amino acid composition**
 - **Alignments of two such regions achieves high score purely due to segment composition**
- ⇒ **While it is worth noting that two proteins contain similar low complexity regions, they are best excluded when constructing alignments**
- **E.g., by default, BLAST employs the SEG algo to filter low complexity regions from proteins before executing a search**

Source: NCBI

Effect of Sequence Length



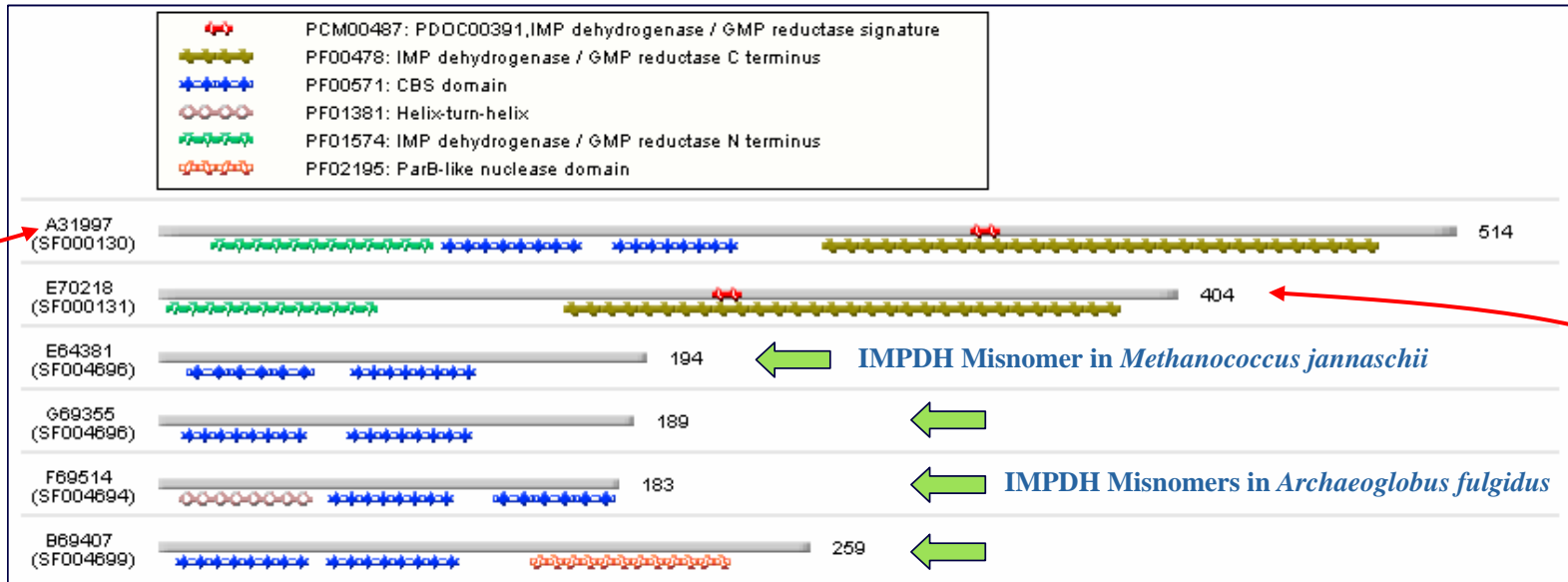
Abagyan RA, Batalov S. Do aligned sequences share the same fold? *J Mol Biol.* 1997 Oct 17;273(1):355-68

Examples of Invalid Function Assignment: The IMP Dehydrogenases (IMPDH)

18 entries were found

ID	Organism	PIR	Swiss-Prot/TrEMBL	RefSeq/GenPept	
NF00181857	Methanococcus jannaschii	E64381 conserved hypothetical protein MJ0653	Y653_METJA Hypothetical protein MJ0653	g1592300 inosine-5'-monophosphate dehydrogenase (guaB) NP_247637 inosine-5'-monophosphate dehydrogenase (guaB)	
NF00187788	Archaeoglobus fulgidus	G69355 MJ0653 homolog AF0847 <i>ALT_NAMES</i> : inosine-monophosphate dehydrogenase (guaB-1) homolog [misnomer]	O29411 INOSINE MONOPHOSPHATE DEHYDROGENASE (GUAB-1)	g2649754 inosine monophosphate dehydrogenase (guaB-1) NP_069681 inosine monophosphate dehydrogenase (guaB-1)	
NF00188267	Archaeoglobus fulgidus	F69514 yhcV homolog 2 <i>ALT_NAMES</i> : inosine-monophosphate dehydrogenase (guaB-2) homolog [misnomer]	O28162 INOSINE MONOPHOSPHATE DEHYDROGENASE (GUAB-2)	g2648410 inosine monophosphate dehydrogenase (guaB-2) NP_070943 inosine monophosphate dehydrogenase (guaB-2)	
NF00188697	Archaeo	<p style="text-align: center;">A partial list of IMP dehydrogenase misnomers in complete genomes remaining in some public databases</p>			osphate ive nophosphate ive
NF00197776	Thermo				nophosphate d protein nonophosphate d protein
NF00414709	Methanothermobacter thermautotrophicus	G69636 MJ0653 homolog AF111220 <i>ALT_NAMES</i> : inosine-monophosphate dehydrogenase related protein V [misnomer]	O27294 INOSINE-5'-MONOPHOSPHATE DEHYDROGENASE RELATED PROTEIN V	dehydrogenase related protein V NP_276354 inosine-5'-monophosphate dehydrogenase related protein V	
NF00414811	Methanothermobacter thermautotrophicus	D69035 MJ1232 protein homolog MTH126 <i>ALT_NAMES</i> : inosine-5'-monophosphate dehydrogenase related protein VII [misnomer]	O26229 INOSINE-5'-MONOPHOSPHATE DEHYDROGENASE RELATED PROTEIN VII	g2621166 inosine-5'-monophosphate dehydrogenase related protein VII NP_275269 inosine-5'-monophosphate dehydrogenase related protein VII	
NF00414837	Methanothermobacter thermautotrophicus	H69232 MJ1225-related protein MTH992 <i>ALT_NAMES</i> : inosine-5'-monophosphate dehydrogenase related protein IX [misnomer]	O27073 INOSINE-5'-MONOPHOSPHATE DEHYDROGENASE RELATED PROTEIN IX	g2622093 inosine-5'-monophosphate dehydrogenase related protein IX NP_276127 inosine-5'-monophosphate dehydrogenase related protein IX	
NF00414969	Methanothermobacter thermautotrophicus	B69077 yhcV homolog 2 <i>ALT_NAMES</i> : inosine-monophosphate dehydrogenase related protein X [misnomer]	O27616 INOSINE-5'-MONOPHOSPHATE DEHYDROGENASE RELATED PROTEIN X	g2622697 inosine-5'-monophosphate dehydrogenase related protein X NP_276687 inosine-5'-monophosphate dehydrogenase related protein X	



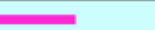



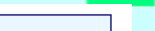


IMPDH Domain Structure

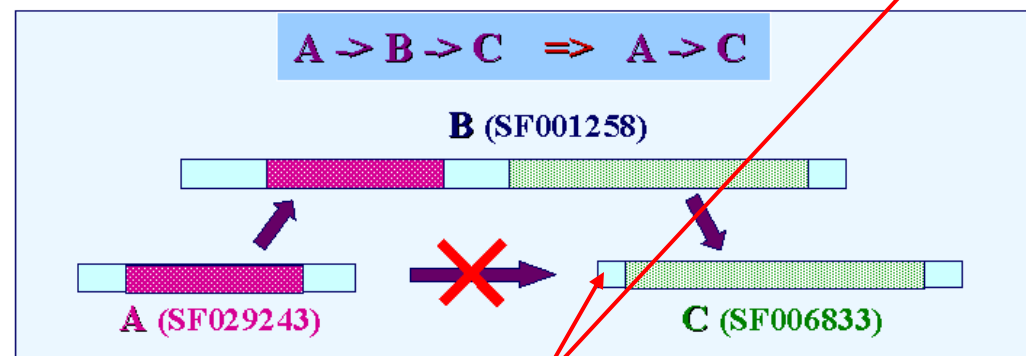


- Typical IMPDHs have 2 IMPDH domains that form the catalytic core and 2 CBS domains.
- A less common but functional IMPDH (E70218) lacks the CBS domains.
- Misnomers show similarity to the CBS domains

Invalid Transitive Assignment

Root of invalid transitive assignment

B →	<input type="checkbox"/> H70468	SF001258	051440	phosphoribosyl-AMP cyclohydrolase (EC 3.5.4.19) / phosphoribosyl-ATP pyrophosphatase (EC 3.6.1.31) [similarity]	<i>Aquifex aeolicus</i>	Prok/other	594.3	4.8e-26	205	39.086	197	
	<input type="checkbox"/> S76963	SF001258	039935	phosphoribosyl-AMP cyclohydrolase (EC 3.5.4.19) / phosphoribosyl-ATP pyrophosphatase (EC 3.6.1.31) [similarity]	<i>Synechocystis sp.</i>	Prok/gram-	557.0	5.7e-24	230	39.175	194	
	<input type="checkbox"/> T35073	SF029243	005738	probable phosphoribosyl-AMP cyclohydrolase	<i>Streptomyces coelicolor</i>	Prok/gram+	399.3	3.5e-15	128	42.157	102	
	<input type="checkbox"/> S53349	SF001257	001188	phosphoribosyl-AMP cyclohydrolase (EC 3.5.4.19) / phosphoribosyl-ATP pyrophosphatase (EC 3.6.1.31) / histidinol dehydrogenase (EC 1.1.1.23)	<i>Saccharomyces cerevisiae</i>	Euk/fungi	384.1	2.5e-14	799	31.863	204	
A →	<input type="checkbox"/> E69493	SF029243	005738	phosphoribosyl-AMP cyclohydrolase (EC 3.5.4.19) [similarity]	<i>Archaeoglobus fulgidus</i>	Archae	396.8	4.8e-15	108	47.778	90	
C →	<input type="checkbox"/> G64337	SF006833	030827	phosphoribosyl-ATP pyrophosphatase (EC 3.6.1.31) [similarity]	<i>Methanococcus jannaschii</i>	Archae	246.9	1.1e-06	95	36.842	95	
	<input type="checkbox"/> D81178	SF006833	101491	phosphoribosyl-ATP pyrophosphatase (EC 3.6.1.31) NMB0603 [similarity]	<i>Neisseria meningitidis</i>	Prok/gram-	230.9	2.6e-06	107	35.227	88	
	<input type="checkbox"/> G81925	SF006833	101491	phosphoribosyl-ATP pyrophosphatase (EC 3.6.1.31) NMA0807 [similarity]								
	<input type="checkbox"/> S51513	SF001257	001188	phosphoribosyl-AMP cyclohydrolase (EC 3.5.4.19) / phosphoribosyl-ATP pyrophosphatase (EC 3.6.1.31) / histidinol dehydrogenase (EC 1.1.1.23)								



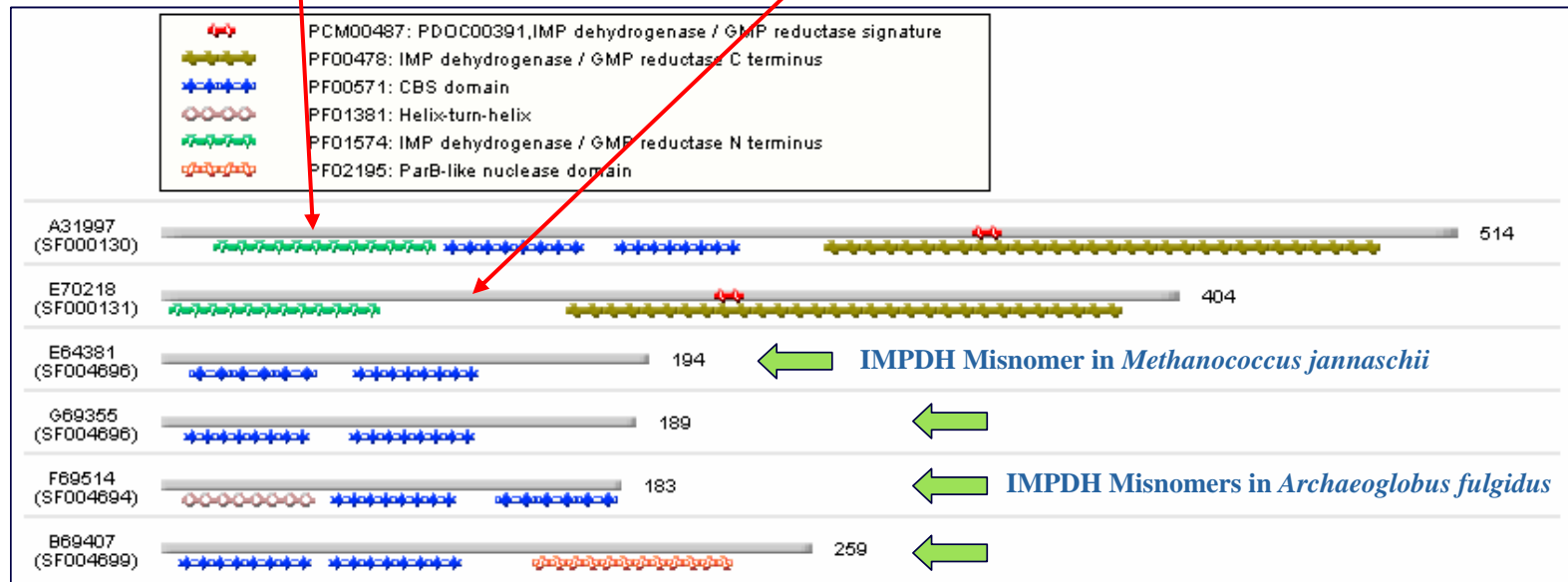
Mis-assignment
of function

No IMPDH domain

Emerging Pattern

Typical IMPDH

Functional IMPDH w/o CBS



- Most IMPDHs have 2 IMPDH and 2 CBS domains
 - Some IMPDH (E70218) lacks CBS domains
- ⇒ IMPDH domain is the emerging pattern

Application of Sequence Comparison: Active Site/Domain Discovery

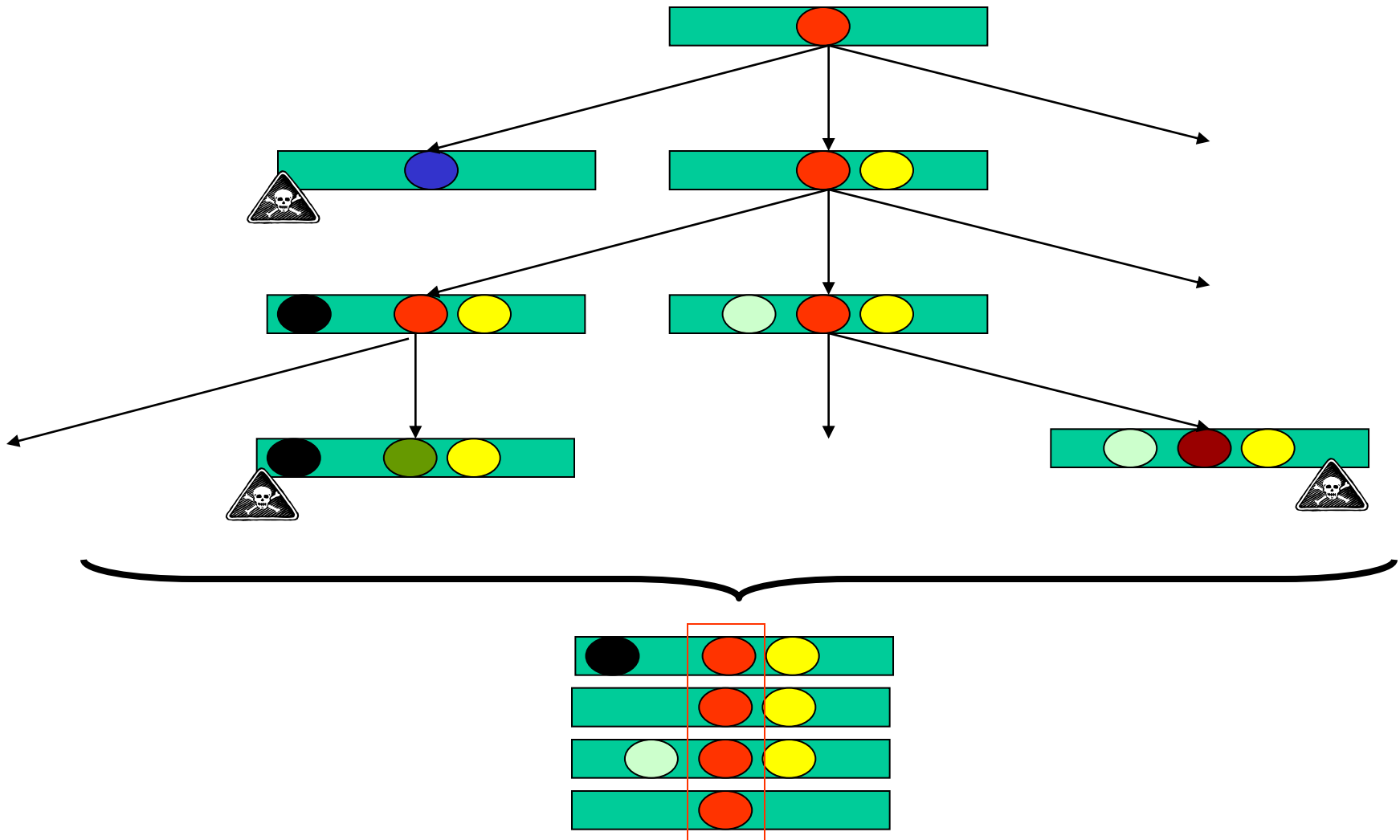


Discover Active Site and/or Domain

- **How to discover the active site and/or domain of a function in the first place?**
 - Multiple alignment of homologous seqs
 - Determine conserved positions
 - ⇒ Emerging patterns relative to background
 - ⇒ Candidate active sites and/or domains
- **Easier if sequences of distance homologs are used**

Exercise: Why?

In the course of evolution...



Multiple Alignment of PTPs

```

gi|126467|      FHFTSWPDFGVPFTP I GMLKFLKKVKACNP--QYAGAIVVHCSAGVGRTGTFVVIDAMLD
gi|2499753     FHFTGWPDHGVPHYHATGLLSF IRRVKLSNP--PSAGPIVVHCSAGAGRTGCIYIVIDIMLD
gi|462550|     YHYTQWPDMGVPEYALPVLTFVRRSSAARM--PETGPVLVHCSAGVGRTGTIYIVIDSMLO
gi|2499751     FHFTSWPDHGVPDTTDLLINFRYLVRDYMKQSPPEPILVHCSAGVGRTGTFIAIDRLIY
gi|1709906     FQFTA WPDHGVPEHPTPFLAFLRRVKTCNP--PDAGPMVVHCSAGVGRTGCFIVIDAMLE
gi|126471|     LHFTSWPDFGVPFTP I GMLKFLKKVKTLNP--VHAGPIVVHCSAGVGRTGTFIVIDAMMA
gi|548626|     FHFTGWPDHGVPHYHATGLLSF IRRVKLSNP--PSAGPIVVHCSAGAGRTGCIYIVIDIMLD
gi|131570|     FHFTGWPDHGVPHYHATGLLGFVRQVKS KSP--PNAGPLVVHCSAGAGRTGCFIVIDIMLD
gi|2144715     FHFTSWPDHGVPDTTDLLINFRYLVRDYMKQSPPEPILVHCSAGVGRTGTFIAIDRLIY
                ..*  ***  ***          .  *                               ..*****  *****  **  ..

```

- Notice the PTPs agree with each other on some positions more than other positions
 - These positions are more imp't wrt PTPs
 - Else they wouldn't be conserved by evolution
- ⇒ They are candidate active sites

Guilt-by-Association:
What if no homolog of known function is
found?



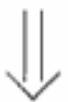
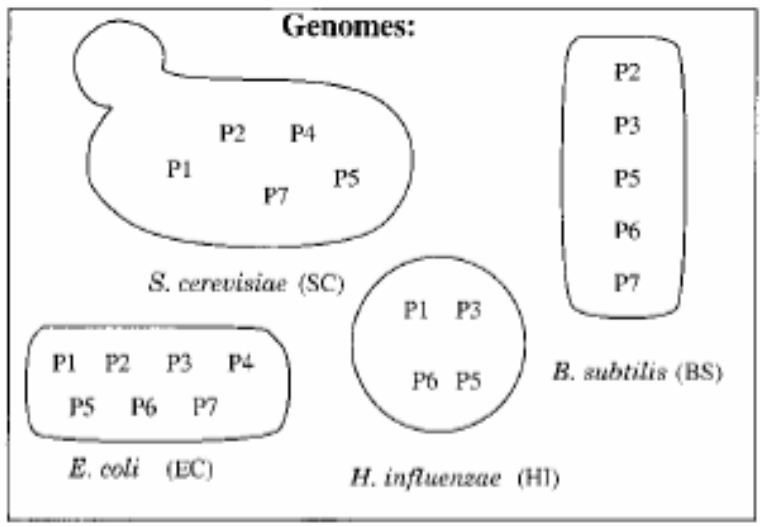
What if there is no useful seq homolog?

- **Guilt by other types of association!**
 - Domain modeling (e.g., HMMPFAM)
 - ✓ Similarity of phylogenetic profiles
 - ✓ Similarity of dissimilarities (e.g., SVM-PAIRWISE)
 - Similarity of subcellular co-localization & other physico-chemico properties (e.g., PROTFUN)
 - Similarity of gene expression profiles
 - ✓ Similarity of protein-protein interaction partners
 - ...
 - Fusion of multiple types of info

Phylogenetic Profiling

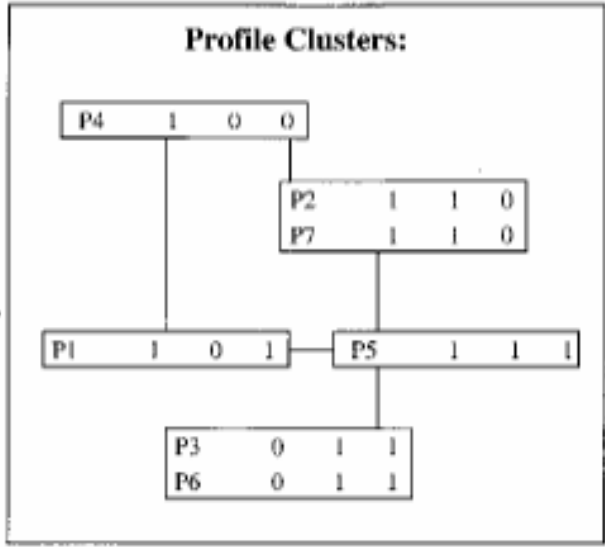
Pellegrini et al., *PNAS*, 96:4285--4288, 1999

- **Gene (and hence proteins) with identical patterns of occurrence across phyla tend to function together**
- ⇒ **Even if no homolog with known function is available, it is still possible to infer function of a protein**



Phylogenetic Profile:

	EC	SC	BS	HI
P1	1	0	1	1
P2	1	1	0	0
P3	0	1	1	1
P4	1	0	0	0
P5	1	1	1	1
P6	0	1	1	1
P7	1	1	0	0



Conclusion: P2 and P7 are functionally linked, P3 and P6 are functionally linked

Phylogenetic Profiling: How it Works

Phylogenetic Profiling: P-value

The probability of observing by chance z occurrences of genes X and Y in a set of N lineages, given that X occurs in x lineages and Y in y lineages is

$$P(z|N, x, y) = \frac{w_z * \overline{w}_z}{W}$$

where

$$\begin{aligned}
 w_z &= \binom{N}{z} \\
 \overline{w}_z &= \binom{N-z}{x-z} * \binom{N-x}{y-z} \\
 W &= \binom{N}{x} * \binom{N}{y}
 \end{aligned}$$

No. of ways to distribute z co-occurrences over N lineage's

No. of ways to distribute the remaining $x-z$ and $y-z$ occurrences over the remaining $N-z$ lineage's

No. of ways of distributing X and Y over N lineage's without restriction

Phylogenetic Profiles: Evidence

Pellegrini et al., *PNAS*, 96:4285--4288, 1999

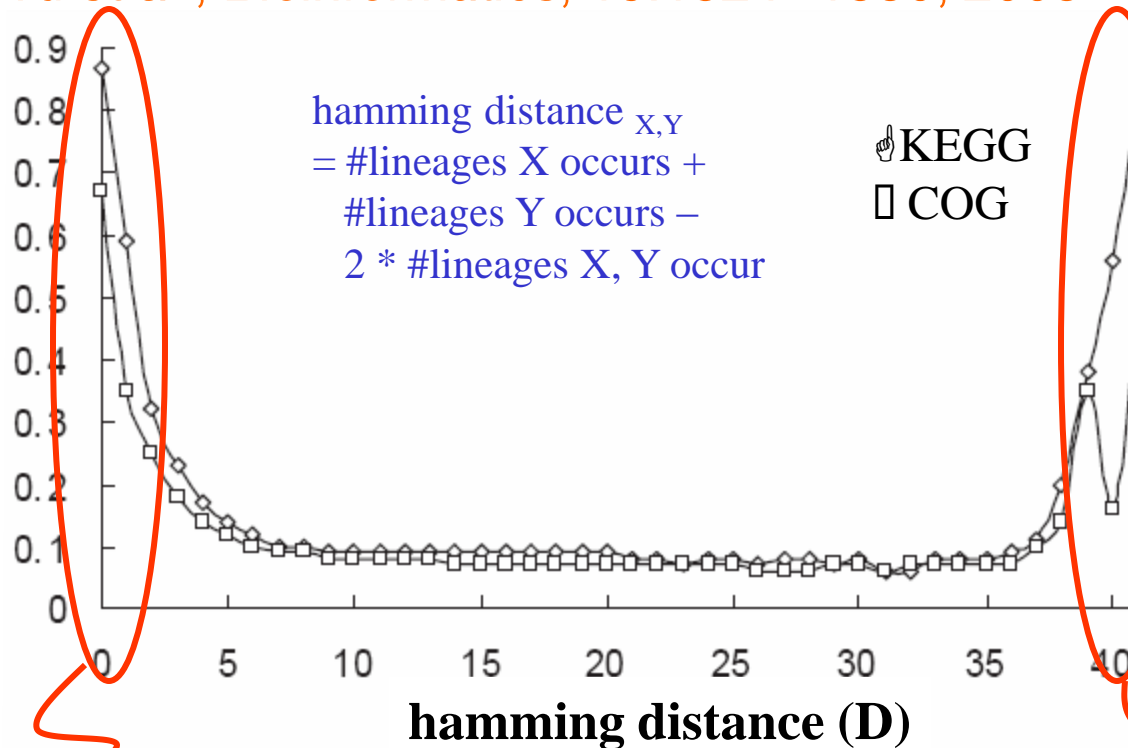
Keyword	No. of non-homologous proteins in group	No. neighbors in keyword group	No. neighbors in random group
Ribosome	60	197	27
Transcription	36	17	10
tRNA synthase and ligase	26	11	5
Membrane proteins*	25	89	5
Flagellar	21	89	3
Iron, ferric, and ferritin	19	31	2
Galactose metabolism	18	31	2
Molybdoterin and Molybdenum, and molybdoterin	12	6	1
Hypothetical [†]	1,084	108,226	8,440

- **E. coli proteins grouped based on similar keywords in SWISS-PROT have similar phylogenetic profiles**

Phylogenetic Profiling: Evidence

Wu et al., *Bioinformatics*, 19:1524--1530, 2003

fraction of gene pairs
having hamming distance D
and share a common pathway
in KEGG/COG



- Proteins having low hamming distance (thus highly similar phylogenetic profiles) tend to share common pathways

Exercise: Why do proteins having high hamming distance also have this behaviour?






Guilt by Association of Dissimilarities



Differences of “unknown” to other fruits are same as “apple” to other fruits



“unknown” is an “apple”!

	 Orange ₁	 Banana ₁	...
Apple ₁ 	Color = red vs orange Skin = smooth vs rough Size = small vs small Shape = round vs round	Color = red vs yellow Skin = smooth vs smooth Size = small vs small Shape = round vs oblong	...
Orange ₂ 	Color = orange vs orange Skin = rough vs rough Size = small vs small Shape = round vs round	Color = orange vs yellow Skin = rough vs smooth Size = small vs small Shape = round vs oblong	...
Unknown ₁ 	Color = red vs orange Skin = smooth vs rough Size = small vs small Shape = round vs round	Color = red vs yellow Skin = smooth vs smooth Size = small vs small Shape = round vs oblong	...
...

SVM-Pairwise Framework

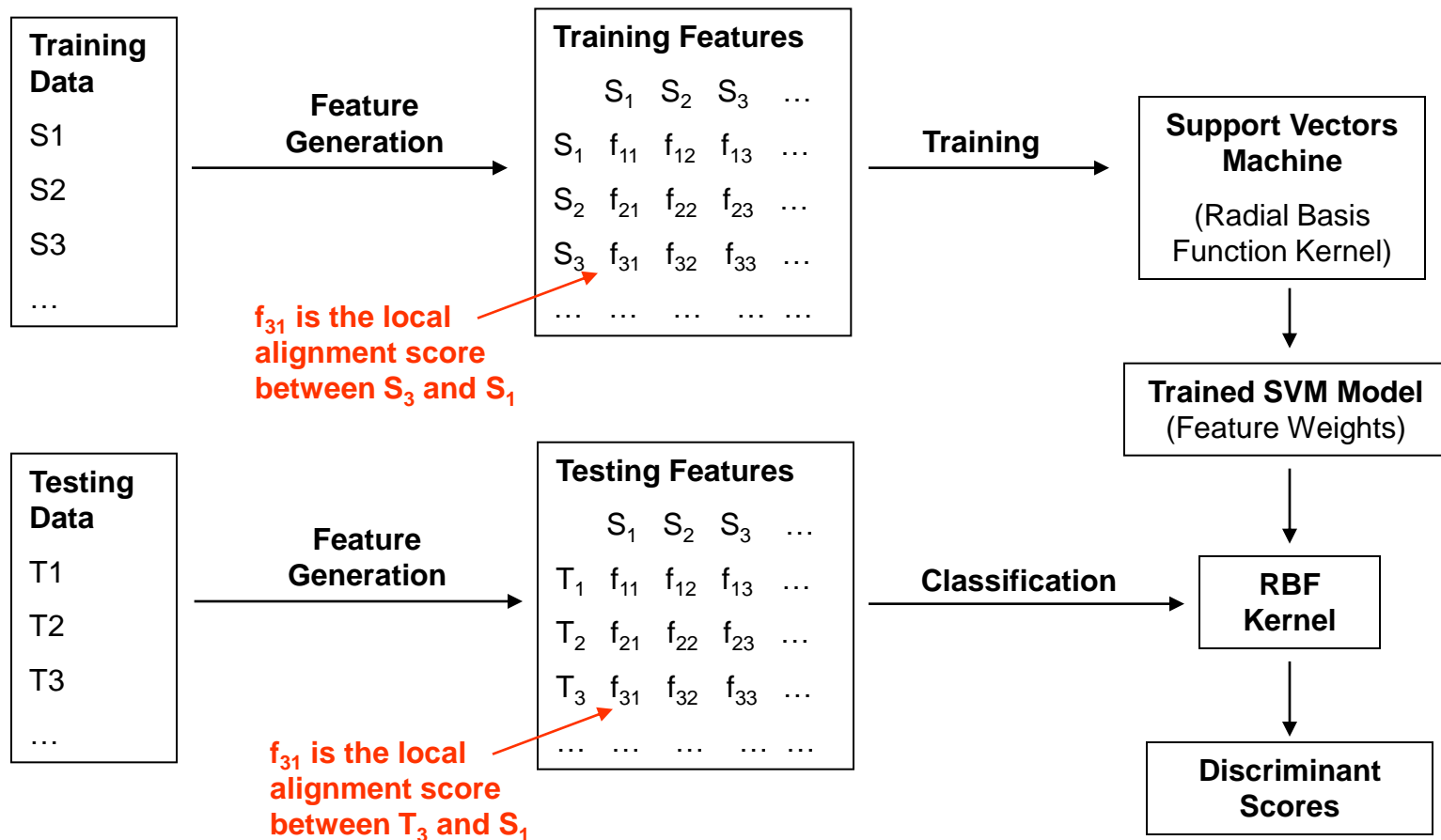
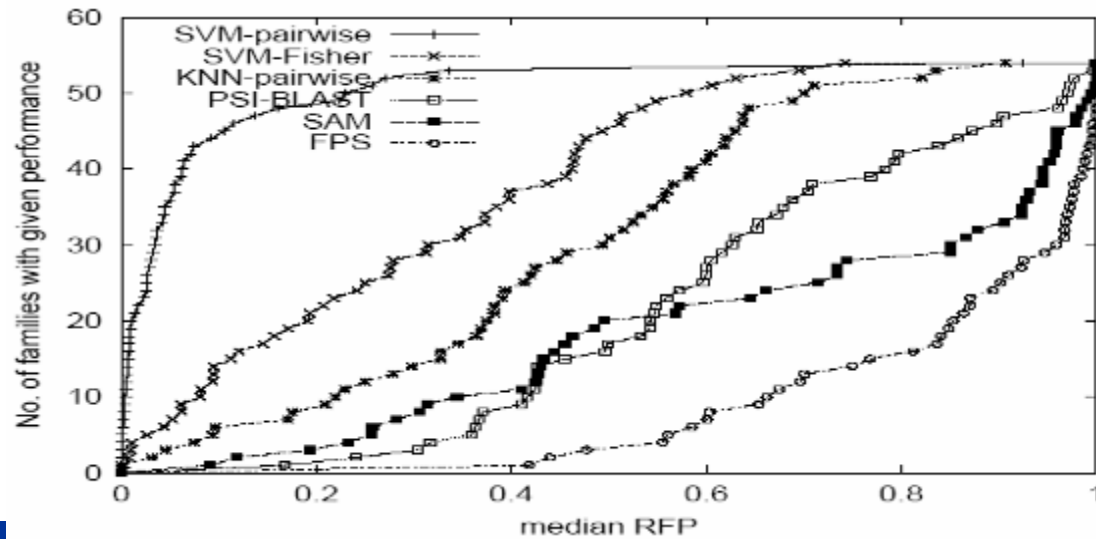
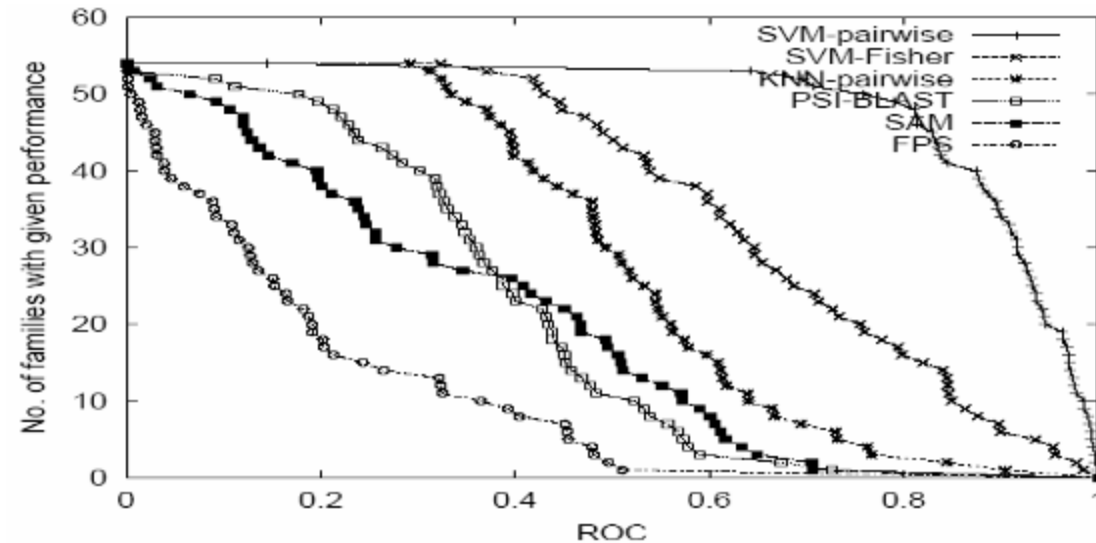


Image credit: Kenny Chua

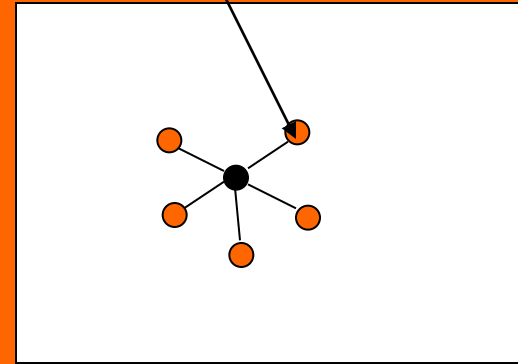
Performance of SVM-Pairwise

- **Receiver Operating Characteristic (ROC)**
 - The area under the curve derived from plotting true positives as a function of false positives for various thresholds.
- **Rate of median False Positives (RFP)**
 - The fraction of negative test examples with a score better or equals to the median of the scores of positive test examples.

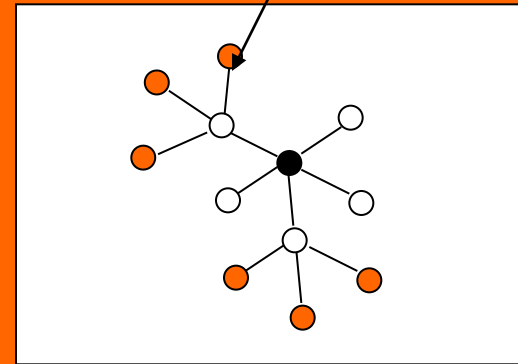


Protein Function Prediction from Protein Interactions

Level-1 neighbour



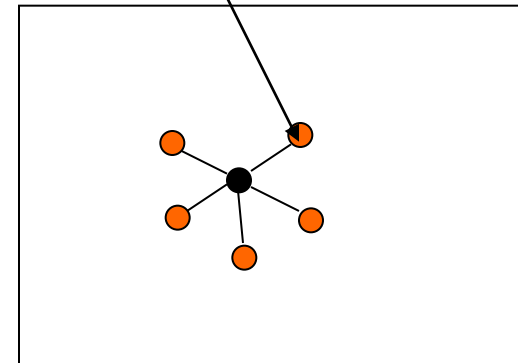
Level-2 neighbour



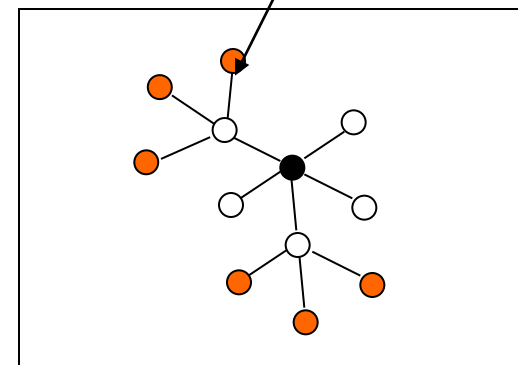
Functional Association Thru Interactions

- **Direct functional association:**
 - Interaction partners of a protein are likely to share functions w/ it
 - Proteins from the same pathways are likely to interact
- **Indirect functional association**
 - Proteins that share interaction partners with a protein may also likely to share functions w/ it
 - Proteins that have common biochemical, physical properties and/or subcellular localization are likely to bind to the same proteins

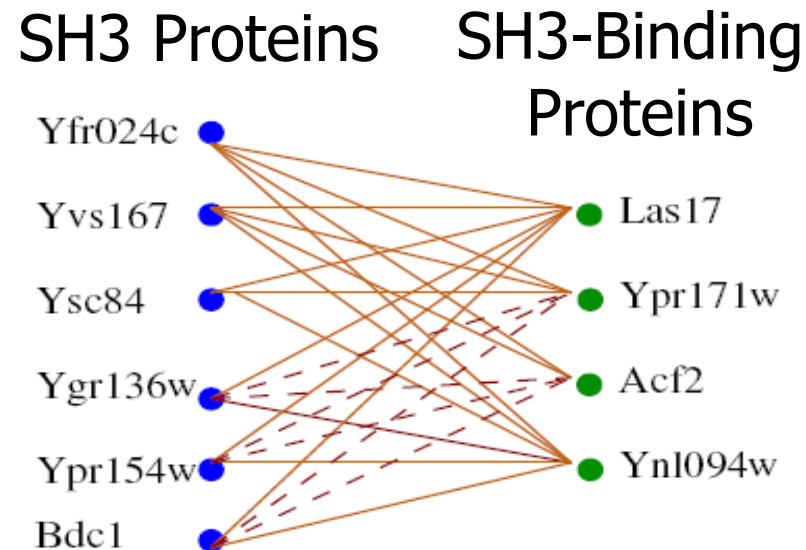
Level-1 neighbour



Level-2 neighbour

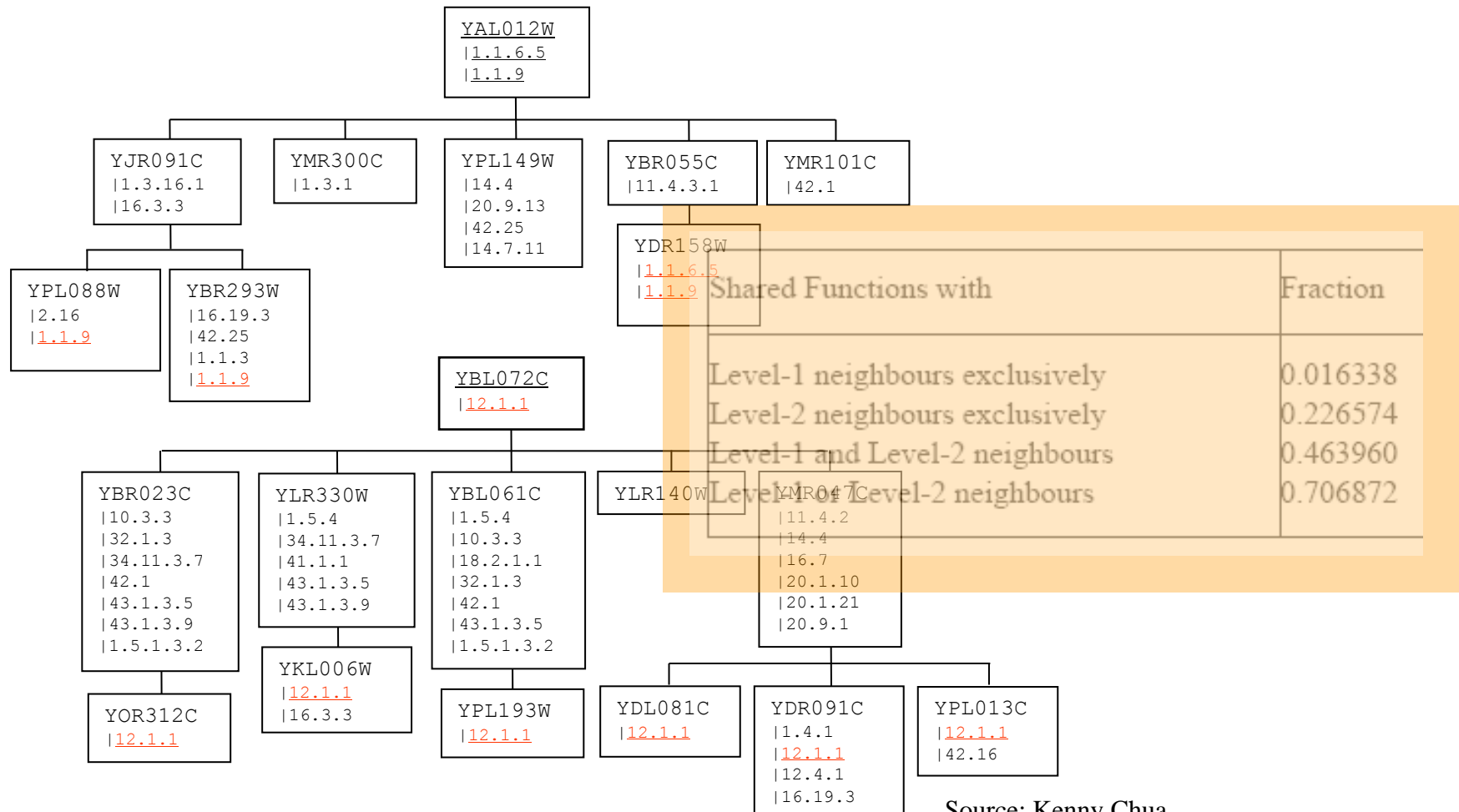


An illustrative Case of Indirect Functional Association?



- *Is indirect functional association plausible?*
- *Is it found often in real interaction data?*
- *Can it be used to improve protein function prediction from protein interaction data?*

Freq of Indirect Functional Association



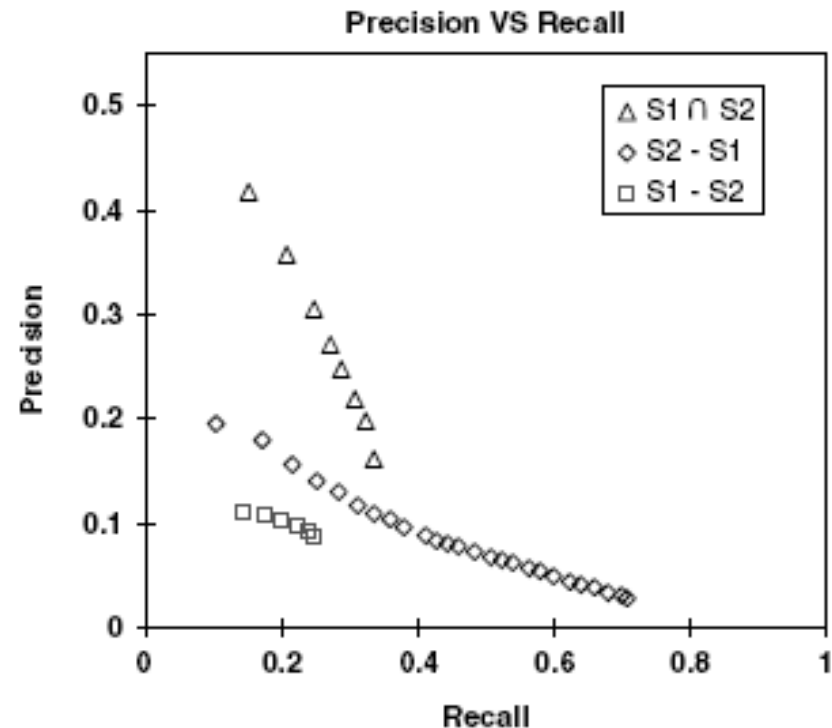
Source: Kenny Chua

Prediction Power By Majority Voting

- Remove overlaps in level-1 and level-2 neighbours to study predictive power of “level-1 only” and “level-2 only” neighbours
- Sensitivity vs Precision analysis**

$$PR = \frac{\sum_i^K k_i}{\sum_i^K m_i} \quad SN = \frac{\sum_i^K k_i}{\sum_i^K n_i}$$

- n_i is no. of fn of protein i
- m_i is no. of fn predicted for protein i
- k_i is no. of fn predicted correctly for protein i



⇒ “level-2 only” neighbours performs better

⇒ L1 ∩ L2 neighbours has greatest prediction power

Functional Similarity Estimate: Czekanowski-Dice Distance

- **Functional distance between two proteins** (Brun et al, 2003)

$$D(u, v) = \frac{|N_u \Delta N_v|}{|N_u \cup N_v| + |N_u \cap N_v|}$$

- N_k is the set of interacting partners of k
- $X \Delta Y$ is symmetric diff betw two sets X and Y
- Greater weight given to similarity

⇒ **Similarity can be defined as**

$$S(u, v) = 1 - D(u, v) = \frac{2X}{2X + (Y + Z)}$$

Is this a good measure if u and v have very diff number of neighbours?

Functional Similarity Estimate: FS-Weighted Measure

- FS-weighted measure**

$$S(u, v) = \frac{2|N_u \cap N_v|}{|N_u - N_v| + 2|N_u \cap N_v|} \times \frac{2|N_u \cap N_v|}{|N_v - N_u| + 2|N_u \cap N_v|}$$

- N_k is the set of interacting partners of k**
- Greater weight given to similarity**

⇒ **Rewriting this as**

$$S(u, v) = \frac{2X}{2X + Y} \times \frac{2X}{2X + Z}$$

Correlation w/ Functional Similarity

- Correlation betw functional similarity & estimates

Neighbours	CD-Distance	FS-Weight
S_1	0.471810	0.498745
S_2	0.224705	0.298843
$S_1 \cup S_2$	0.224581	0.29629

- Equiv measure slightly better in correlation w/ similarity for L1 & L2 neighbours

Reliability of Expt Sources

- **Diff Expt Sources have diff reliabilities**
 - Assign reliability to an interaction based on its expt sources (Nabieva et al, 2004)

- **Reliability betw u and v computed by:**

$$r_{u,v} = 1 - \prod_{i \in E_{u,v}} (1 - r_i)$$

- r_i is reliability of expt source i ,
- $E_{u,v}$ is the set of expt sources in which interaction betw u and v is observed

Source	Reliability
Affinity Chromatography	0.823077
Affinity Precipitation	0.455904
Biochemical Assay	0.666667
Dosage Lethality	0.5
Purified Complex	0.891473
Reconstituted Complex	0.5
Synthetic Lethality	0.37386
Synthetic Rescue	1
Two Hybrid	0.265407

Functional Similarity Estimate: FS-Weighted Measure with Reliability

- Take reliability into consideration when computing FS-weighted measure:

$$S_R(u, v) = \frac{2 \sum_{w \in (N_u \cap N_v)} r_{u,w} r_{v,w}}{\left(\sum_{w \in N_u - N_v} r_{u,w} + \sum_{w \in (N_u \cap N_v)} r_{u,w} (1 - r_{v,w}) \right) + 2 \sum_{w \in (N_u \cap N_v)} r_{u,w} r_{v,w}} \times \frac{2 \sum_{w \in (N_u \cap N_v)} r_{u,w} r_{v,w}}{\left(\sum_{w \in N_v - N_u} r_{v,w} + \sum_{w \in (N_u \cap N_v)} r_{v,w} (1 - r_{u,w}) \right) + 2 \sum_{w \in (N_u \cap N_v)} r_{u,w} r_{v,w}}$$

- N_k is the set of interacting partners of k
- $r_{u,w}$ is reliability weight of interaction between u and w

⇒ Rewriting

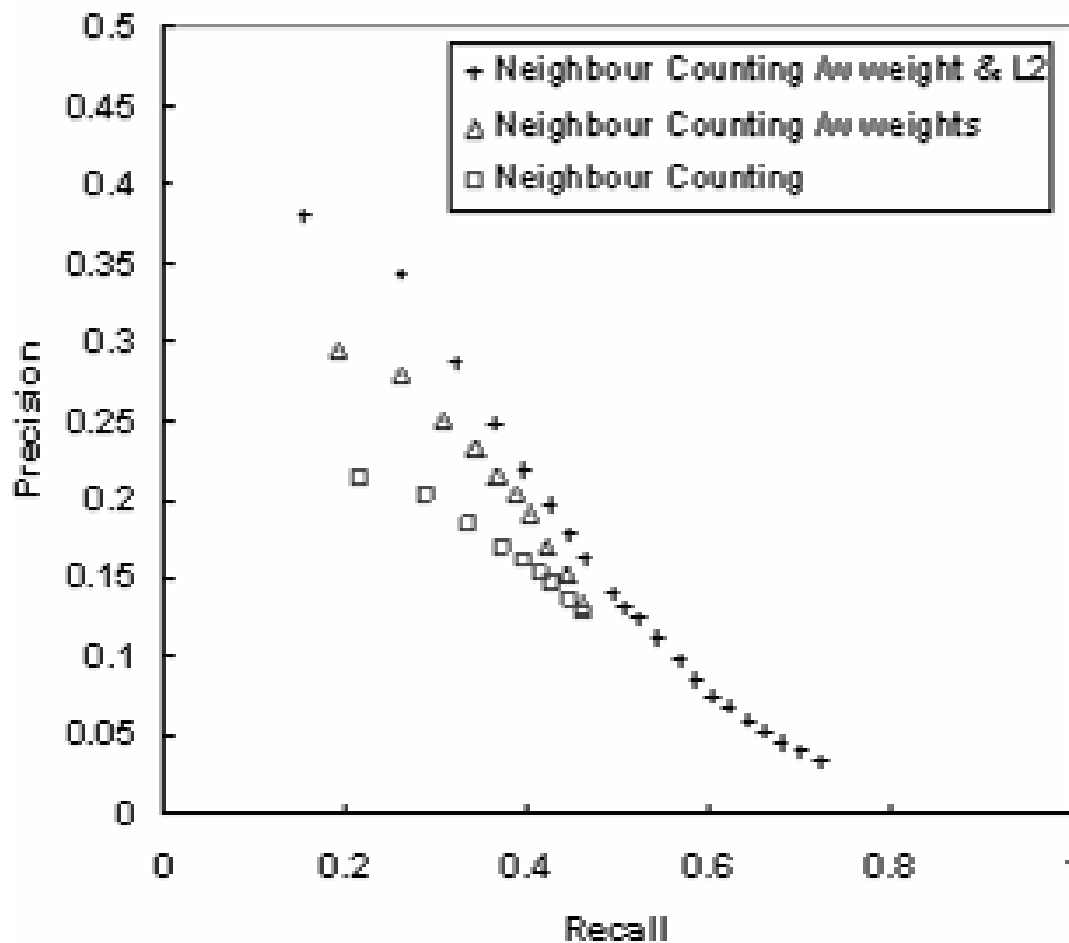
$$S(u, v) = \frac{2X}{2X + Y} \times \frac{2X}{2X + Z}$$

Integrating Reliability

- **Equiv measure shows improved correlation w/ functional similarity when reliability of interactions is considered:**

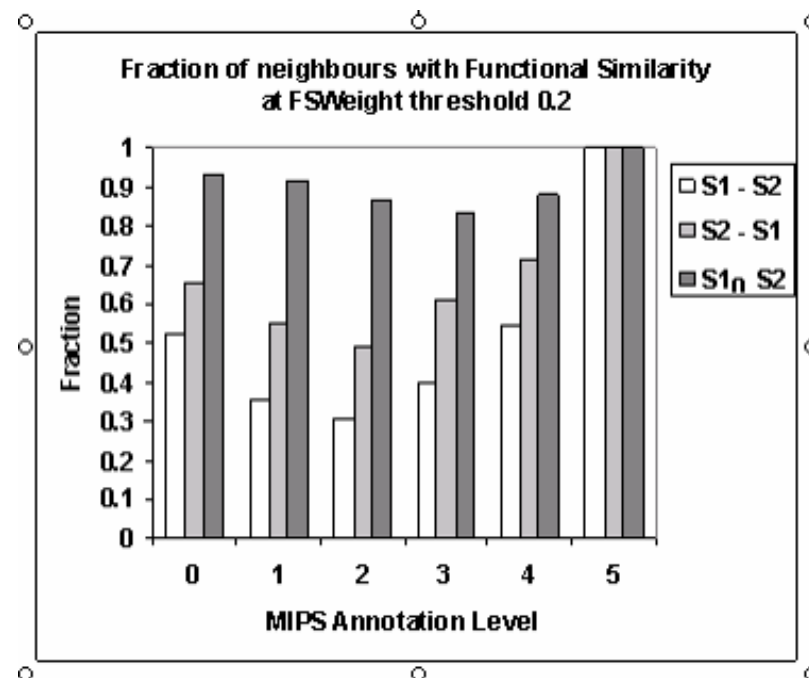
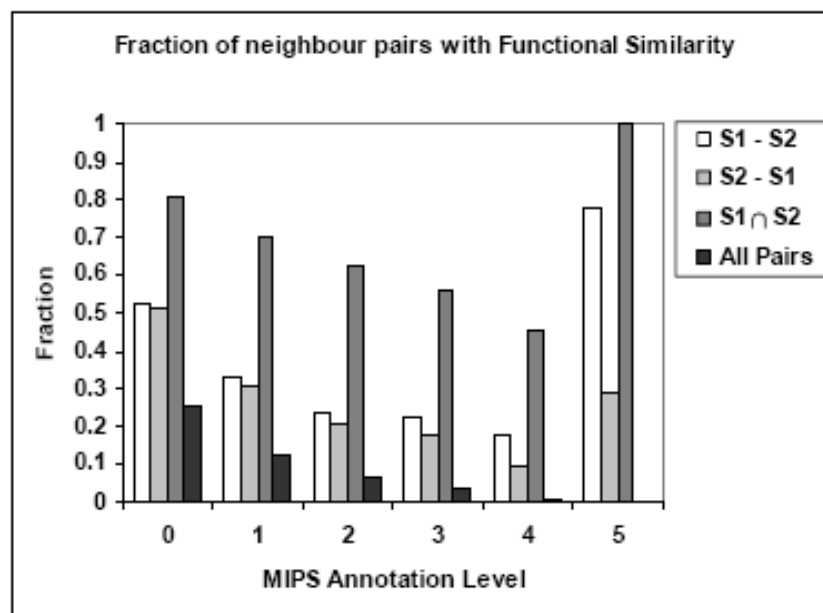
Neighbours	CD-Distance	FS-Weight	FS-Weight R
S ₁	0.471810	0.498745	0.532596
S ₂	0.224705	0.298843	0.375317
S ₁ ∪ S ₂	0.224581	0.29629	0.363025

Improvement to Prediction Power by Majority Voting



Considering only
neighbours w/ FS
weight > 0.2

Improvement to Over-Rep of Functions in Neighbours



Use L1 & L2 Neighbours for Prediction

- FS-weighted Average**

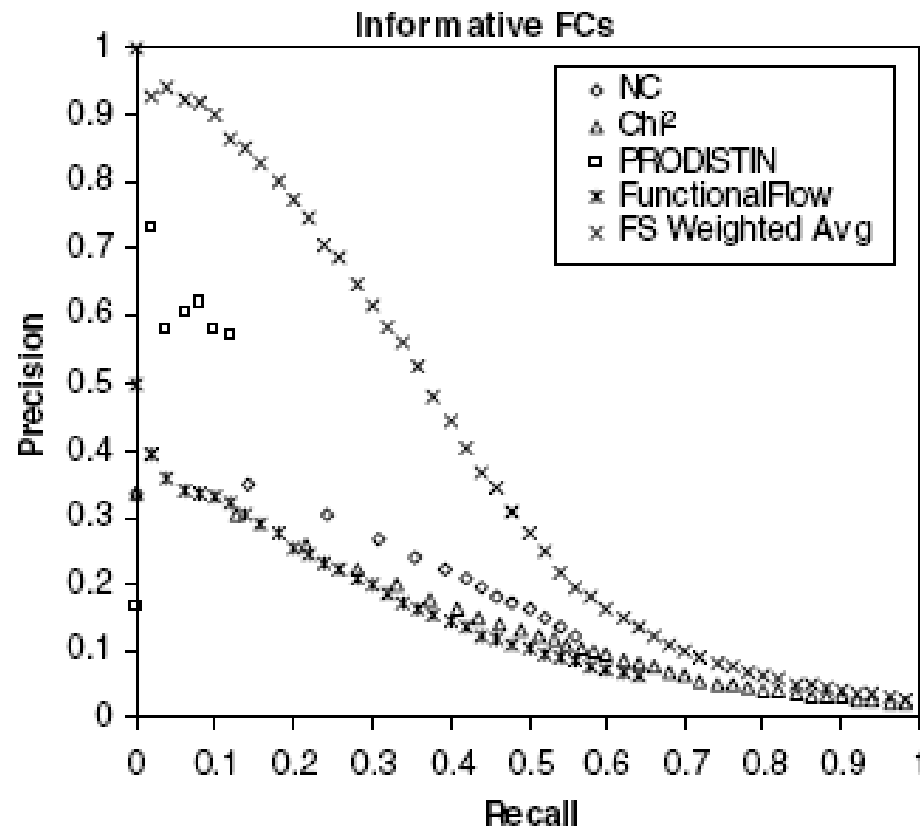
$$f_x(u) = \frac{1}{Z} \left[\lambda r_{int} \pi_x + \sum_{v \in N_u} \left(S_{TR}(u, v) \delta(v, x) + \sum_{w \in N_v} S_{TR}(u, w) \delta(w, x) \right) \right]$$

- r_{int} is fraction of all interaction pairs sharing function
- λ is weight of contribution of background freq
- $\delta(k, x) = 1$ if k has function x , 0 otherwise
- N_k is the set of interacting partners of k
- π_x is freq of function x in the dataset
- Z is sum of all weights

$$Z = 1 + \sum_{v \in N_u} \left(S_{TR}(u, v) + \sum_{w \in N_v} S_{TR}(u, w) \right)$$

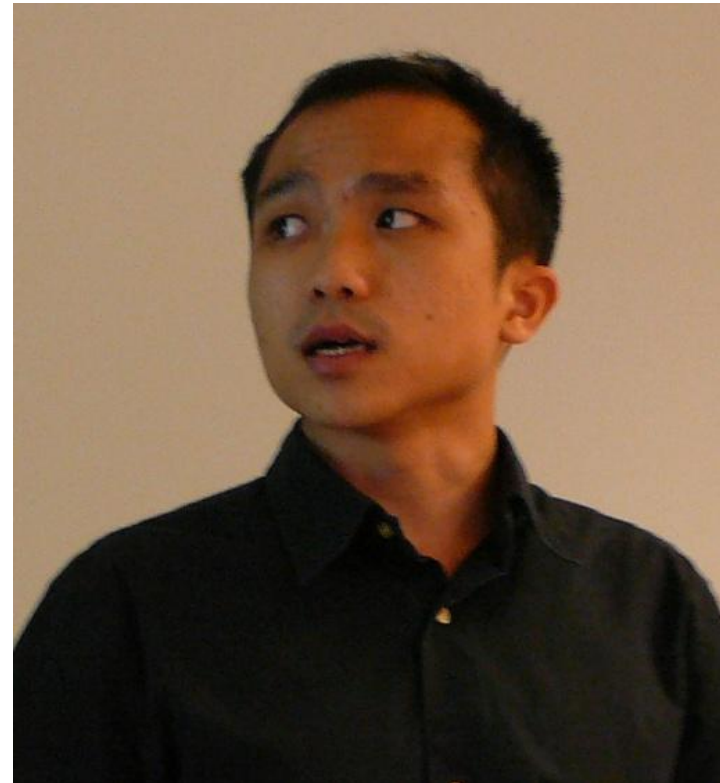
Performance of FS-Weighted Averaging

- LOOCV comparison with Neighbour Counting, Chi-Square, PRODISTIN



About the Inventor: Chua Hon Nian

- **Chua Hon Nian**
 - PhD, NUS, 2008
 - Postdoc at Harvard & Univ of Toronto
 - 49th hottest paper in Computer Science published in 2006
 - Winner, DREAM2 challenge PPI subnetwork, 2007



Application of Sequence Comparison: Key Mutation Site Discovery




Identifying Key Mutation Sites

K.L.Lim et al., *JBC*, 273:28986--28993, 1998

Sequence from a typical PTP domain D2

```
>gi|00000|PTP&-D2
```

```
EEEFKKLTSIKIQNDKMRTGNLFPANMKKNRVLQIIPYEFNRVIIPVKRGEENTDYVNASF
IDGYRQKDSYIASQGPLLHTIEDFWRMIWEWKSCSIVMLTELEERGQEKCAQYWPSDGLV
SYGDIITVELKKEEECESYTVRDLLVTNTRENKSRQIRQFHFGWPEVGIIPSDGKGMISII
AAVQKQQQQSGNHPITVHCSAGAGRTGTFCALSTVLERVKAEGILDVVFQTVKSLRLQRPH
MVQTLQYEFQYKVVQYIDAFSDYANFK
```

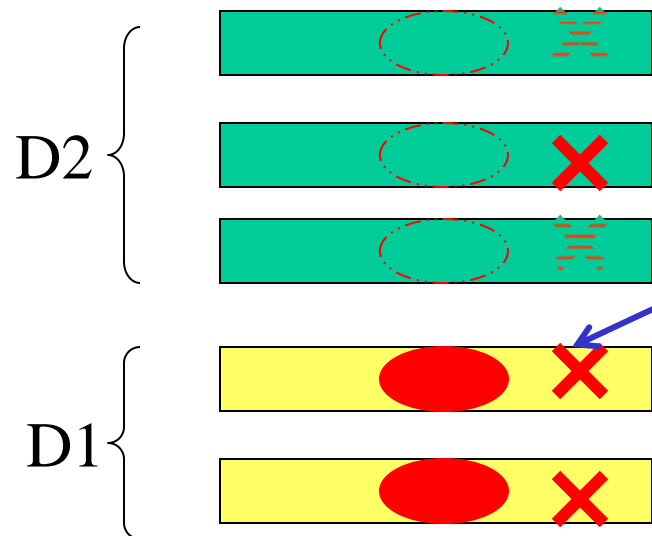


- Some PTPs have 2 PTP domains
- PTP domain D1 is has much more activity than PTP domain D2
- Why? And how do you figure that out?

Emerging Patterns of PTP D1 vs D2

- **Collect example PTP D1 sequences**
- **Collect example PTP D2 sequences**
- **Make multiple alignment A1 of PTP D1**
- **Make multiple alignment A2 of PTP D2**
- **Are there positions conserved in A1 that are violated in A2?**
- **These are candidate mutations that cause PTP activity to weaken**
- **Confirm by wet experiments**

Emerging Patterns of PTP D1 vs D2



This site is consistently conserved in D1,
 but is not consistently missing in D2
 \Rightarrow it is not an EP
 \Rightarrow not a likely cause of D2's loss of function

Exercise: Why?

This site is consistently conserved in D1,
 but is consistently missing in D2
 \Rightarrow it is an EP
 \Rightarrow possible cause of D2's loss of function

 absent
 present

Key Mutation Site: PTP D1 vs D2

```

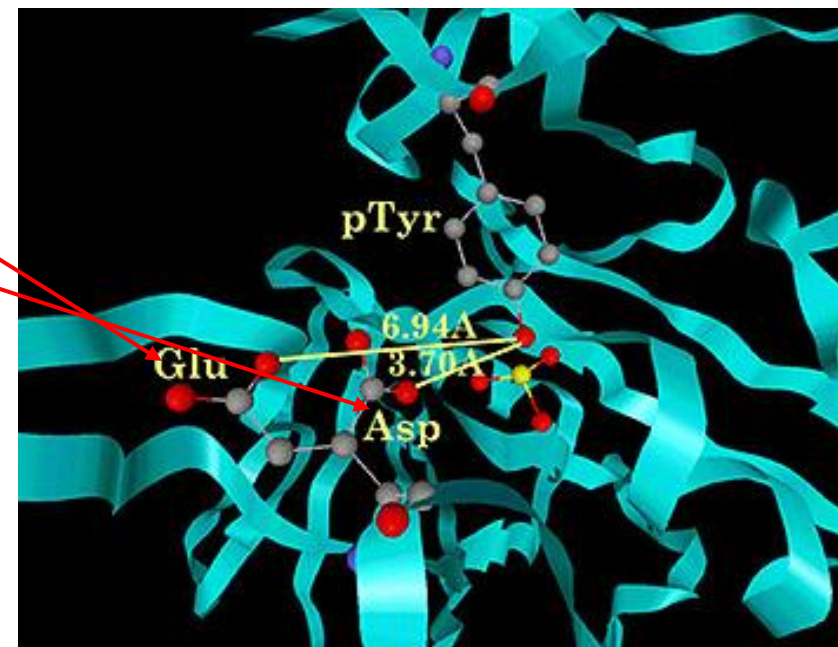
                ?  !  ?              ?              ?              ?  ??
gi|00000|P   D2  QFHFHGWPEVGIPSDGKGMISIIAAVQKQQQQ-SGNHPITVHCSAGAGRTGTFCALSTVL
gi|126467|   QFHFTSWPDFGVPFTP IGMLKFLKKVKACNP--QYAGAIVVHCSAGVGRTGTFVVIDAML
gi|2499753   QFHFTGWPDHGVPYHATGLLSF IRRVKLSNP--PSAGPIVVHCSAGAGRTGCYIVIDIML
gi|462550|   QYHYTQWPDMGVPEYALPVLTFVRRSSAARM--PETGPVLVHCSAGVGRTGTYIVIDSML
gi|2499751   QFHFTSWPDHGVPDTTDLLINFRYLVRDYMKQSPPEPILVHCSAGVGRTGTFIAIDRLI
gi|1709906   D1  QFQFTA WPDHGVP EHP TPFLAFLRRVKTCNP--PDAGPMVVHCSAGVGRTGCFIVIDAML
gi|126471|   QLHFTSWPDFGVPFTP IGMLKFLKKVKTLNP--VHAGPIVVHCSAGVGRTGTFIVIDAMM
gi|548626|   QFHFTGWPDHGVPYHATGLLSF IRRVKLSNP--PSAGPIVVHCSAGAGRTGCYIVIDIML
gi|131570|   QFHFTGWPDHGVPYHATGLLGFRVQVKSISP--PNAGPLVVHCSAGAGRTGCFIVIDIML
gi|2144715   QFHFTSWPDHGVPDTTDLLINFRYLVRDYMKQSPPEPILVHCSAGVGRTGTFIAIDRLI
                * ..  ** . *. *                . ***** **** .. . .

```

- **Positions marked by “!” and “?” are likely places responsible for reduced PTP activity**
 - All PTP D1 agree on them
 - All PTP D2 disagree on them

Key Mutation Site: PTP D1 vs D2

		?	!	?
gi 00000 P	D2	QFHFHGWPEN	GIPSDGK	
gi 126467		QFHFTS	WPDFGVP	FFTP I
gi 2499753		QFHFTGWP	DHGVPYHAT	
gi 462550		QYHYTQWP	DMGVPEYAL	
gi 2499751		QFHFTSWP	DHGVPDTTD	
gi 1709906	D1	QFQFTA	WPDHGVPEHPT	
gi 126471		QLHFTS	WPDFGVPFFTP I	
gi 548626		QFHFTGWP	DHGVPYHAT	
gi 131570		QFHFTGWP	DHGVPYHAT	
gi 2144715		QFHFTSWP	DHGVPDTTD	
		* ..	**.	*.*



- Positions marked by “!” are even more likely as 3D modeling predicts they induce large distortion to structure

Confirmation by Mutagenesis Expt

- **What wet experiments are needed to confirm the prediction?**
 - Mutate E \rightarrow D in D2 and see if there is gain in PTP activity
 - Mutate D \rightarrow E in D1 and see if there is loss in PTP activity

Exercise: Why do you need this 2-way expt?

About the Inventor: Prasanna Kolatkar

- **Prasanna Kolatkar**
 - Research Fellow, BIC, NUS, 1997-1999
 - Currently Group Leader at GIS



Concluding Remarks



What have we learned?

- **General methodologies & applications**
 - Guilt by association for protein function inference
 - Invariants for active site discovery
 - Emerging patterns for mutation site discovery
- **Important tactics**
 - Genome phylogenetic profiling
 - SVM-Pairwise
 - Protein-protein interactions

Any Question?



Acknowledgements

- **Some of the slides are based on slides given to me by Kenny Chua**

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