For written notes on this lecture, please read chapter 3 of *The Practical Bioinformatician*. *Alternatively, please read* "Rule-Based Data Mining Methods for Classification Problems in Biomedical Domains", a tutorial at *PKDD04* by Jinyan Li and Limsoon Wong, September 2004. http://www.comp.nus.edu.sg/~wongls/talks/pkdd04/

# CS2220: Introduction to Computational Biology Unit 1b: Essence of Knowledge Discovery

Wong Limsoon



#### Outline



- Overview of supervised learning
  - Decision trees
- Decision tree ensembles
  - Bagging

#### Other methods

- K-nearest neighbour
- Support vector machines
- Naïve Bayes
- Hidden Markov models

# Overview of supervised learning



#### Supervised learning



- Also called classification
- Learn from past experience, and use the learned knowledge to classify new data
- Knowledge learned by intelligent algorithms
- Examples:
  - Clinical diagnosis for patients
  - Cell type classification

#### Data



- Classification application involves > 1 class of data. E.g.,
  - Normal vs disease cells for a diagnosis problem
- Training data is a set of instances (samples, points, etc.) with known class labels
- Test data is a set of instances whose class labels are to be predicted

#### **Notations**



Training data

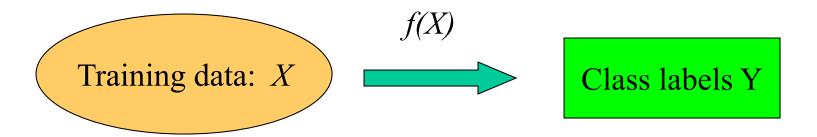
$$\{\langle x_1, y_1 \rangle, \langle x_2, y_2 \rangle, ..., \langle x_m, y_m \rangle\}$$
  
where  $x_j$  are n-dimensional vectors  
and  $y_j$  are from a discrete space Y.  
E.g., Y = {normal, disease}

Test data

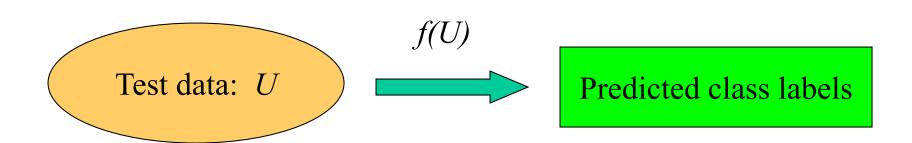
$$\{\langle u1, ? \rangle, \langle u2, ? \rangle, ..., \langle uk, ? \rangle \}$$

#### **Process**





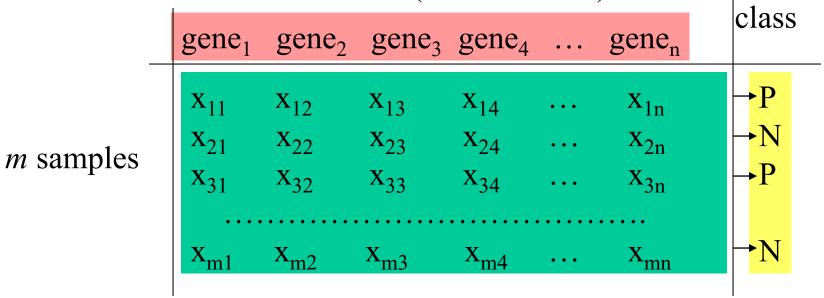
A classifier, a mapping, a hypothesis



#### Relational representation



*n* features (order of 1000)



## Features (aka attributes)



- Categorical features
  - color = {red, blue, green}
- Continuous or numerical features
  - gene expression
  - age
  - blood pressure
- Discretization

# Example



Outlook	Temp	Humidity	Windy	class
Sunny	75	70	true	Play
Sunny	80	90	true	Don't
Sunny	85	85	false	Don't
Sunny	72	95	true	Don't
Sunny	69	70	false	Play
Overcast	72	90	true	Play
Overcast	83	78	false	Play
Overcast	64	65	true	Play
Overcast	81	75	false	Play
Rain	71	80	true	Don't
Rain	65	70	true	Don't
Rain	75	80	false	Play
Rain	68	80	false	Play
Rain	70	96	false	Play

# Overall picture of supervised learning



Labelled Data + Algorithms



Biomedical

Financial

Government

Scientific

Decision trees

Emerging patterns

SVM

Neural networks

Classifiers (Medical Doctors)

# Recap: Evaluation of a classifier

- Performance on independent blind test data
  - Blind test data properly represent real world
- K-fold cross validation
  - Given a dataset, divide it into k even parts, k-1 of them are used for training, and the rest one part treated as test data
- LOOCV, a special case of K-fold cross validation
- Accuracy, error rate, false positive rate, false negative rate, sensitivity, specificity, precision



# Requirements of biomedical classification

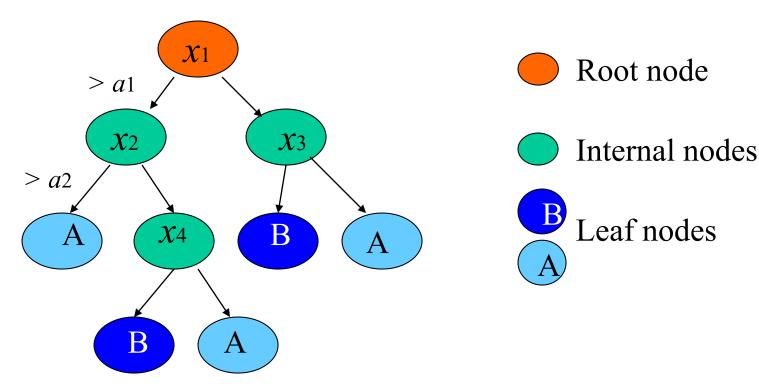
- High accuracy, sensitivity, specificity, precision
- High comprehensibility

# Importance of rule-based method

- Systematic selection of a small number of features used for the decision making
- ⇒ Increase comprehensibility of the knowledge patterns
- C4.5 and CART are two commonly used rule induction algorithms---a.k.a. decision tree induction algorithms

#### Structure of decision trees

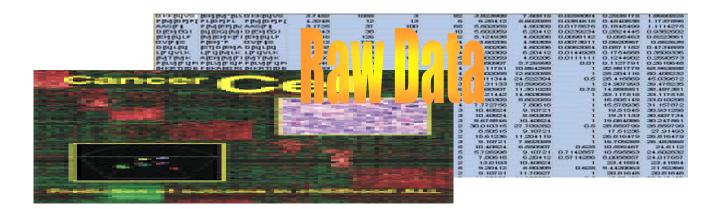




- If x1 > a1 & x2 > a2, then it's A class
- C4.5, CART, two of the most widely used
- Easy interpretation, but accuracy maybe unattractive

## Elegance of decision trees

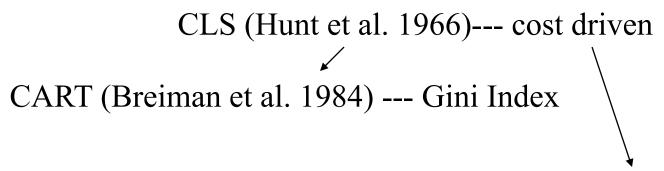




Every path from root to a leaf forms a decision rule

# Brief history of decision trees





ID3 (Quinlan, 1986) --- Information-driven

C4.5 (Quinlan, 1993) --- Gain ratio + Pruning ideas

## A simple dataset



Outlook	Temp	Humidity	Windy	class
Sunny	75	70	true	Play
Sunny	80	90	true	Don't
Sunny	85	85	false	Don't
Sunny	72	95	true	Don't
Sunny	69	70	false	Play
Overcast	72	90	true	Play
Overcast	83	78	false	Play
Overcast	64	65	true	Play
Overcast	81	75	false	Play
Rain	71	80	true	Don't
Rain	65	70	true	Don't
Rain	75	80	false	Play
Rain	68	80	false	Play
Rain	70	96	false	Play

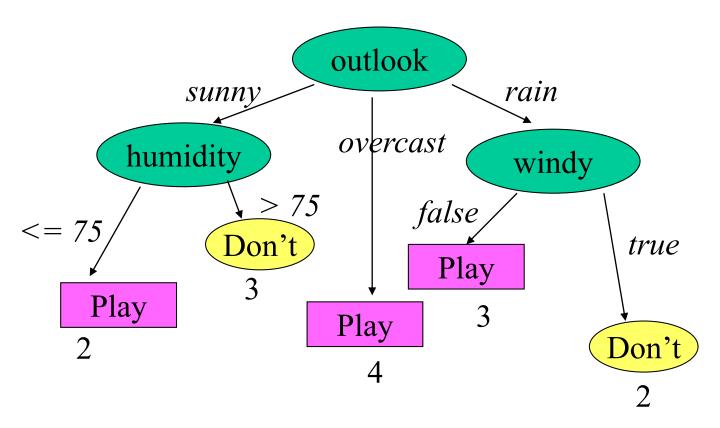
9 Play samples

5 Don't

A total of 14.

#### A decision tree





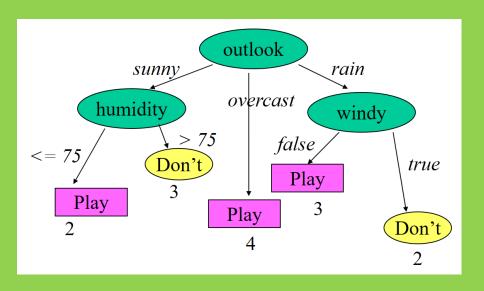
 Construction of a tree is equiv to determination of root node of the tree and root nodes of its sub-trees

Exercise: What is the accuracy of this tree?

# Food for thought



Outlook	Temp	Humidity	Windy	class
Sunny	75	70	true	Play
Sunny	80	90	true	Don't
Sunny	85	85	false	Don't
Sunny	72	95	true	Don't
Sunny	69	70	false	Play
Overcast	72	90	true	Play
Overcast	83	78	false	Play
Overcast	64	65	true	Play
Overcast	81	75	false	Play
Rain	71	80	true	Don't
Rain	65	70	true	Don't
Rain	75	80	false	Play
Rain	68	80	false	Play
Rain	70	96	false	Play

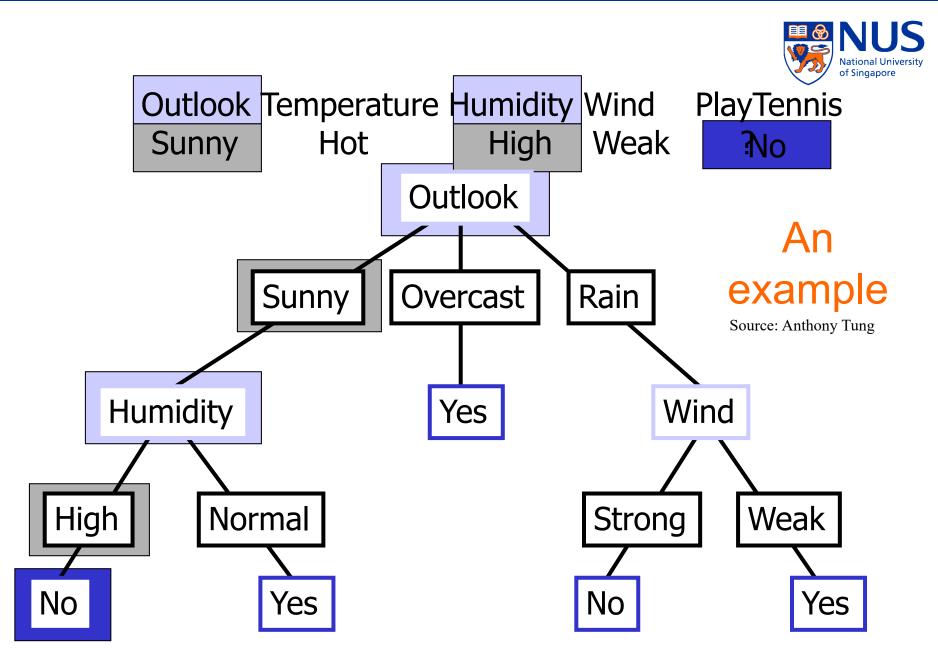


Copyrig

What is the accuracy of this decision tree?

Exercise #1

Wong Limsoon



# Most discriminatory feature



- Every feature can be used to partition the training data
- If the partitions contain a pure class of training instances, then this feature is most discriminatory

#### Example of partitions



- Categorical feature
  - Number of partitions of the training data is equal to the number of values of this feature
- Numerical feature
  - Two partitions

Categ	orical feature	Numerical featur	re			IUS
_						nal University gapore
Instance #		-	_Humidity	Windy	class	
1			70	true	Play	
2			90	true	Don't	
3			85	false	Don't	
4			95	true	Don't	
5			70	false	Play	
6			90	true	Play	
7			78	false	Play	
8			65	true	Play	
9			75	false	Play	
10			80	true	Don't	
11			70	true	Don't	
12			80	false	Play	
13			80	false	Play	
14			96	false	Play	

Categ	orical feature				
nstance #	Outlook	Temp	Humidity	Windy	class
1	Sunny	75	70	true	Play
2	Sunny	80	90	true	Don't
3	Sunny	85	85	false	Don't
4	Sunny	72	95	true	Don't
5	Sunny	69	70	false	Play
6	Overcast	72	90	true	Play
7	Overcast	83	78	false	Play
8	Overcast	64	65	true	Play
9	Overcast	81	75	false	Play
10	Rain	71	80	true	Don't
11	Rain	65	70	true	Don't
12	Rain	75	80	false	Play
13	Rain	68	80	false	Play
14	Rain	70	96	false	Play

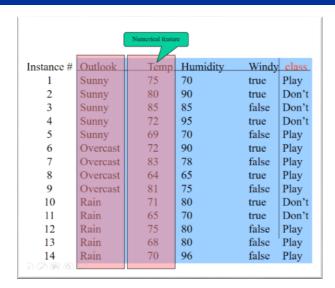
Total 14 training instances

A categorical feature is partitioned based on its number of possible values



Outlook = 6,7,8,9 overcast P,P,P,P

Outlook = 10,11,12,13,14 D, D, P, P, P





Temperature <= 70

5,8,11,13,14 P,P, D, P, P

Total 14 training instances

Temperature 1,2,3,4,6,7,9,10,12 > 70 P,D,D,P,P,P,D,P

A numerical feature is generally partitioned by choosing a "cutting point"

#### Decision tree construction



- Select the "best" feature as root node of the whole tree
- Partition dataset into subsets using this feature so that the subsets are as "pure" as possible
- After partition by this feature, select the best feature (wrt the subset of training data) as root node of this sub-tree
- Recursively, until the partitions become pure or almost pure

#### Let's construct a decision tree



Outlook	Temp	Humidity	Windy	class
Sunny	75	70	true	Play
Sunny	80	90	true	Don't
Sunny	85	85	false	Don't
Sunny	72	95	true	Don't
Sunny	69	70	false	Play
Overcast	72	90	true	Play
Overcast	83	78	false	Play
Overcast	64	65	true	Play
Overcast	81	75	false	Play
Rain	71	80	true	Don't
Rain	65	70	true	Don't
Rain	75	80	false	Play
Rain	68	80	false	Play
Rain	70	96	false	Play

Ask the class to pick root node and construct the tree recursively with them...
How good is that tree?

Exercise #2



Three measures to evaluate which feature is best

- Gini index
- Information gain
- Information gain ratio





```
\begin{aligned} & \text{gini}(S) &=& \frac{\text{diff of two arbitrary specimen in } S}{\text{mean specimen in } S} \\ &=& \text{prob}(\text{getting two specimen of diff class in } S) \\ &=& 1 - \text{prob}(\text{getting two specimen of same class in } S) \\ &=& 1 - \sum_i \text{prob}(\text{getting specimen of class } i \text{ in } S)^2 \end{aligned}
```

- Gini index is the expected value of the ratio of the diff of two arbitrary specimens to the mean value of all specimens
- Closer to 1, feature is similar to "background distribution". Closer to 0, feature is "unexpected"

#### Gini index



Let  $\mathcal{U} = \{C_1, ..., C_k\}$  be all the classes. Suppose we are currently at a node and D is the set of those samples that have been moved to this node. Let f be a feature and d[f] be the value of the feature f in a sample d. Let S be a range of values that the feature f can take. Then the Gini index for f in D for the range S is defined as

$$gini_f^D(S) = 1 - \sum_{C_i \in \mathcal{U}} \left( \frac{|\{d \in D \mid d \in C_i, d[f] \in S\}|}{|D|} \right)^2$$

The purity of a split of the value range S of an attribute f by some split-point into subranges  $S_1$ and  $S_2$  is then defined as

$$gini_f^D(S_1, S_2) = \sum_{S \in \{S_1, S_2\}} \frac{|\{d \in D \mid d[f] \in S\}|}{|D|} * gini_f^D(S)$$

we choose the feature f and the split-point p that minimizes  $gini_f^D(S_1, S_2)$  over all possible alternative features and split-points.

#### Gini index of "Outlook"



Outlook	Temp	Humidity	Windy	class
Sunny	75	70	true	Play
Sunny	80	90	true	Don't
Sunny	85	85	false	Don't
Sunny	72	95	true	Don't
Sunny	69	70	false	Play
Overcast	72	90	true	Play
Overcast	83	78	false	Play
Overcast	64	65	true	Play
Overcast	81	75	false	Play
Rain	71	80	true	Don't
Rain	65	70	true	Don't
Rain	75	80	false	Play
Rain	68	80	false	Play
Rain	70	96	false	Play

$$gini_f^D(S) = 1 - \sum_{C_i \in \mathcal{U}} \left( \frac{|\{d \in D \mid d \in C_i, d[f] \in S\}|}{|D|} \right)^2$$

$$gini_f^D(S_1, S_2) = \sum_{S \in \{S_1, S_2\}} \frac{|\{d \in D \mid d[f] \in S\}|}{|D|} * gini_f^D(S)$$

- gini(Sunny) =  $1 (2/5)^2 (3/5)^2 = 0.48$
- gini(Overcast) =  $1 (4/4)^2 (0/5)^2 = 0$
- gini(Rain) =  $1 (3/5)^2 (2/5)^2 = 0.48$
- gini(Outlook) = 5/14 \* 0.48 + 4/14 \* 0 + 5/14 \* 0.48 = 0.34

# Characteristics of C4.5/CART tree National University of Singapore

- Single coverage of training data (elegance)
- Divide-and-conquer splitting strategy
- Fragmentation problem ⇒ Locally reliable but globally insignificant rules

Miss many globally significant rules; mislead system



Example Use of

**Decision Tree Methods:** 

Proteomics
Approaches to
Biomarker Discovery

- In prostate and bladder cancers (Adam et al. Proteomics, 2001)
- In serum samples to detect breast cancer (Zhang et al. Clinical Chemistry, 2002)
- In serum samples to detect ovarian cancer (Petricoin et al. Lancet; Li & Rao, PAKDD 2004)

#### Decision tree ensembles



#### Motivating example



- h<sub>1</sub>, h<sub>2</sub>, h<sub>3</sub> are indep classifiers w/ accuracy = 60%
- C<sub>1</sub>, C<sub>2</sub> are the only classes
- t is a test instance in C<sub>1</sub>
- $h(t) = argmax_{C \in \{C1,C2\}} | \{h_j \in \{h_1, h_2, h_3\} | h_j(t) = C\} |$
- Then prob(h(t) =  $C_1$ )
  - = prob( $h_1(t)=C_1 \& h_2(t)=C_1 \& h_3(t)=C_1$ ) + prob( $h_1(t)=C_1 \& h_2(t)=C_1 \& h_3(t)=C_2$ ) + prob( $h_1(t)=C_1 \& h_2(t)=C_2 \& h_3(t)=C_1$ ) + prob( $h_1(t)=C_2 \& h_2(t)=C_1 \& h_3(t)=C_1$ ) = 60% \* 60% \* 60% + 60% \* 60% \* 40% +
  - 60% \* 40% \* 60% + 40% \* 60% \* 60% = 64.8%

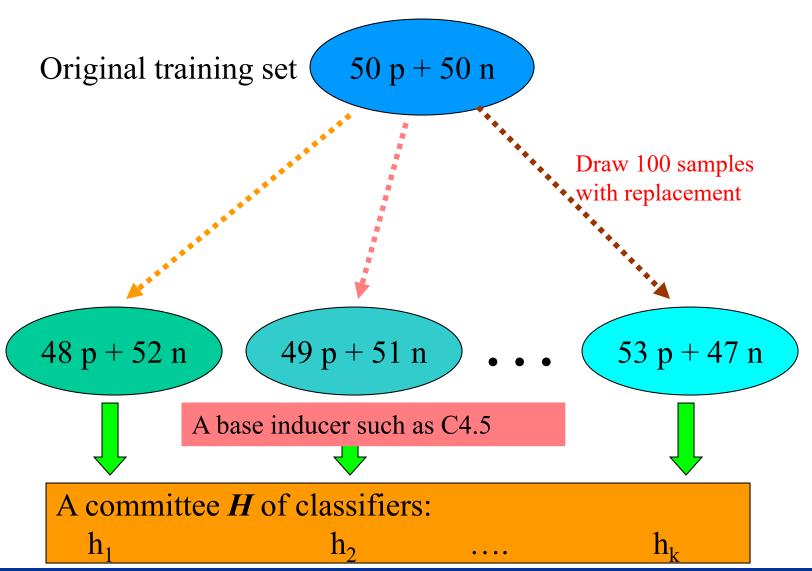
## Bagging



- Proposed by Breiman (1996)
- Also called Bootstrap aggregating
- Make use of randomness injected to training data

### Main ideas





## Decision making by bagging



#### Given a new test sample T

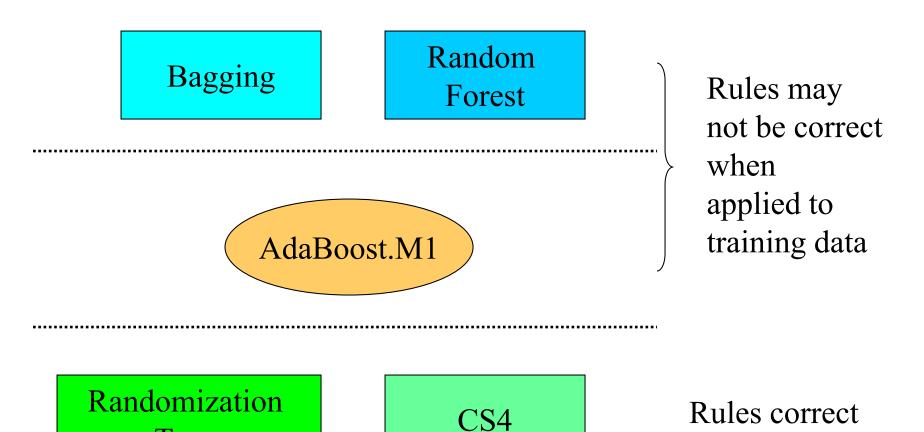
$$bagged(T) = \operatorname{argmax}_{C_j \in \mathcal{U}} |\{h_i \in \mathcal{H} \mid h_i(T) = C_j\}|$$

where 
$$U = \{C_1, ..., C_r\}$$

What does this formula mean?



## Summary of ensemble classifiers



Trees

Evercise: Describe the decision tre

Exercise: Describe the decision tree ensemble classifiers not explained in this ppt

# Other machine learning approaches



#### Outline



- K-nearest neighbor (kNN)
- Support vector machines (SVM)
- Naïve Bayes
- Hidden Markov models (HMM)

# K-nearest neighbours



#### How kNN works



- Given a new case
- Find k "nearest"
   neighbours, i.e., k
   most similar points in
   the training data set
- Assign new case to the same class to which most of these neighbours belong

 A common "distance" measure betw samples x and y is

$$\sqrt{\sum_f (x[f] - y[f])^2}$$

where f ranges over features of the samples

Exercise: What does the formula above mean?

## Illustration of kNN (k=8)



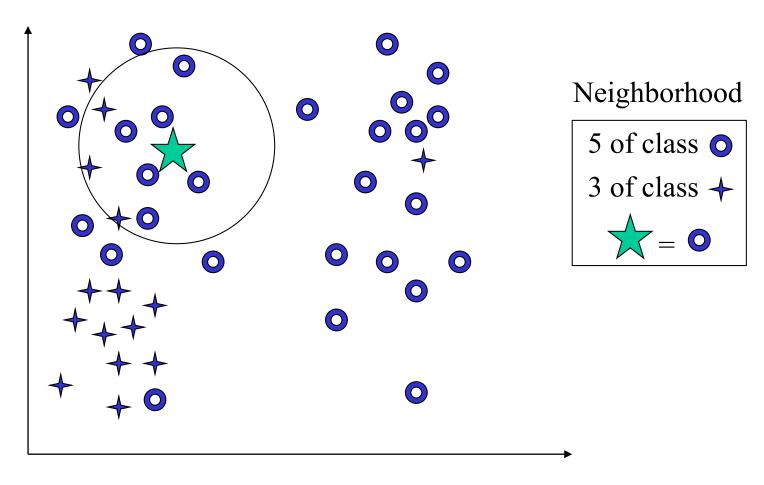


Image credit: Zaki

#### Some issues



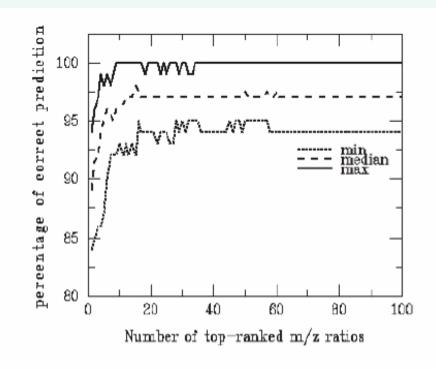
- Simple to implement
- Must compare new case against all training cases
- ⇒ May be slow during prediction
- No need to train
- But need to design distance measure properly
- ⇒ May need expert for this
- Can't explain prediction outcome
- ⇒ Can't provide a model of the data

#### Example Use of kNN

# s based on Nation of Sin

# Ovarian cancer diagnosis based SELDI proteomic data

- Li et al, Bioinformatics
   20:1638-1640, 2004
- Use kNN to diagnose ovarian cancers using proteomic spectra
- Data set is from Petricoin et al., Lancet 359:572-577, 2002



**Fig. 1.** Minimum, median and maximum of percentages of correct prediction as a function of the number of top-ranked m/z ratios in 50 independent partitions into learning and validation sets.

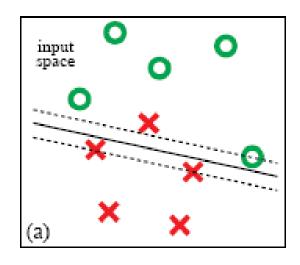
## Support vector machines

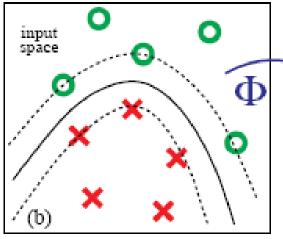


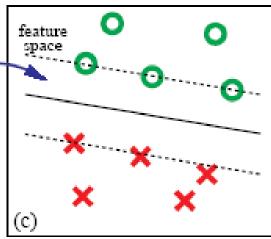
#### Basic idea



Image credit: Zien





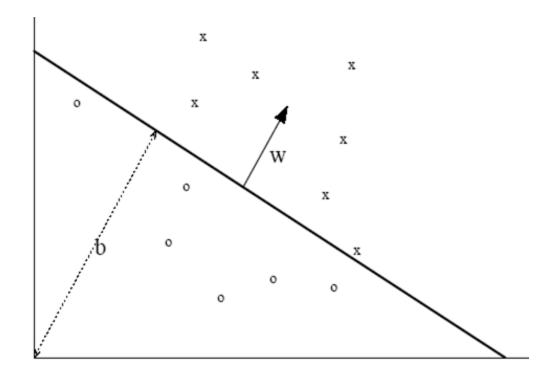


- (a) Linear separation not possible w/o errors
- (b) Better separation by nonlinear surfaces in input space
- (c) Nonlinear surface corr to linear surface in feature space. Map from input to feature space by "kernel" function  $\Phi$
- ⇒ "Linear learning machine" + kernel function as classifier

## Linear learning machines



- Hyperplane separating the x's and o's points is given by (W•X) + b = 0, with (W•X) =  $\Sigma_i$ W[j]\*X[j]
- $\Rightarrow$  Decision function is IIm(X) = sign((W•X) + b))



### Linear learning machines



Solution is a linear combination of training points
 X<sub>k</sub> with labels Y<sub>k</sub>

$$W = \sum_{k} \alpha_{k}^{*} Y_{k}^{*} X_{k},$$
with  $\alpha_{k} > 0$ , and  $Y_{k} = \pm 1$ 

$$\Rightarrow Ilm(X) = sign(\sum_{k} \alpha_{k}^{*} Y_{k}^{*} (X_{k} \cdot X) + b)$$

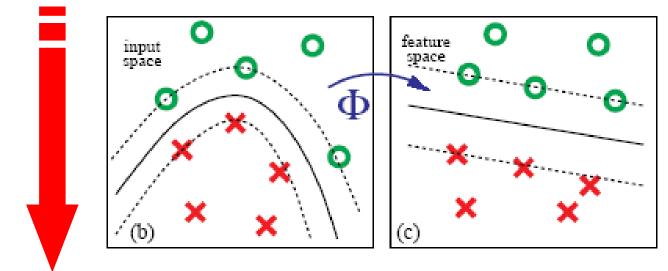


"data" appears only in dot product!

#### Kernel function



•  $IIm(X) = sign(\Sigma_k \alpha_k^* Y_k^* (X_k \bullet X) + b)$ 



- $svm(X) = sign(\sum_{k} \alpha_{k}^{*} Y_{k}^{*} (\Phi X_{k} \bullet \Phi X) + b)$
- $\Rightarrow \text{svm}(X) = \text{sign}(\Sigma_k \alpha_k^* Y_k^* K(X_k, X) + b)$ where  $K(X_k, X) = (\Phi X_k^* \Phi X)$

#### Kernel function



- $svm(X) = sign(\sum_{k} \alpha_{k}^{*} Y_{k}^{*} K(X_{k}, X) + b)$
- $\Rightarrow$  K(A,B) can be computed w/o computing  $\Phi$
- In fact replace it w/ lots of more "powerful" kernels besides (A • B). E.g.,
  - $K(A,B) = (A \cdot B)^d$
  - $K(A,B) = \exp(-||AB||^2/(2*\sigma)), ...$

#### How SVM works



- $svm(X) = sign(\sum_{k} \alpha_{k}^{*} Y_{k}^{*} K(X_{k}, X) + b)$
- To find  $\alpha_k$  is a quadratic programming problem

max: 
$$\Sigma_k \alpha_k - 0.5 * \Sigma_k \Sigma_h \alpha_k \alpha_h Y_k Y_h K(X_k, X_h)$$

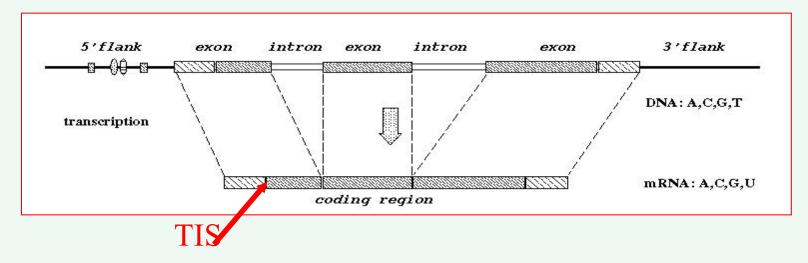
subject to: 
$$\Sigma_k \alpha_k * Y_k = 0$$

and for all 
$$\alpha_k$$
,  $C \ge \alpha_k \ge 0$ 

To find b, estimate by averaging

$$Y_h - \sum_k \alpha_k^* Y_k^* K(X_h, X_k)$$
  
for all  $\alpha_h \ge 0$ 

# Example Use of SVM: Recognition of protein translation initiation sites



- Zien et al., Bioinformatics 16:799-807, 2000
- Use SVM to recognize protein translation initiation sites from genomic sequences
- Raw data set is same as Liu & Wong, JBCB 1:139-168, 2003

## Naïve Bayes



### Bayes theorem



$$P(h|d) = \frac{P(d|h) * P(h)}{P(d)}$$

- P(h) = prior prob that hypothesis h holds
- P(d|h) = prob of observing data d given h holds
- P(h|d) = posterior prob that h holds given observed data d

## Bayesian approach



• Let H be all possible classes. Given a test instance w/ feature vector  $\{f_1 = v_1, ..., f_n = v_n\}$ , the most probable classification is given by

$$\operatorname{argmax}_{h_j \in H} P(h_j | f_1 = v_1, \dots, f_n = v_n)$$

Using Bayes Theorem, rewrites to

$$\operatorname{argmax}_{h_j \in H} \frac{P(f_1 = v_1, \dots, f_n = v_n | h_j) * P(h_j)}{P(f_1 = v_1, \dots, f_n = v_n)}$$

• Since denominator is independent of  $h_j$ , this simplifies to

$$\operatorname{argmax}_{h_i \in H} P(f_1 = v_1, \dots, f_n = v_n | h_j) * P(h_j)$$

## Naïve Bayes



- But estimating  $P(f_1=v_1, ..., f_n=v_n|h_j)$  accurately may not be feasible unless training data set is large
- "Solved" by assuming  $f_1, ..., f_n$  are conditionally independent of each other
- Then  $\underset{h_j \in H}{\operatorname{argmax}} P(f_1 = v_1, \dots, f_n = v_n | h_j) * P(h_j)$   $= \underset{i}{\operatorname{argmax}} \prod_{h_j \in H} P(f_i = v_i | h_j) * P(h_j)$

where  $P(h_j)$  and  $P(f_i=v_i|h_j)$  can often be estimated reliably from typical training data set

Exercise: How do you estimate  $P(h_j)$  and  $P(f_j=v_j|h_j)$ ?

Abstractly, the probability model for a classifier is a conditional model

$$p(C|F_1,\ldots,F_n)$$

over a dependent class variable C with a small number of outcomes or *classes*, conditional on several feature variables  $F_1$  through  $F_n$ . The problem is that if the number of features n is large or when a feature can take on a large number of values, then basing such a model on probability tables is infeasible. We therefore reformulate the model to make it more tractable.

Using Bayes' theorem, we write

$$p(C|F_1,...,F_n) = \frac{p(C) \ p(F_1,...,F_n|C)}{p(F_1,...,F_n)}.$$

In practice we are only interested in the numerator of that fraction, since the denominator does not depend on C and the values of the features  $F_i$  are given, so that the denominator is effectively constant. The numerator is equivalent to the joint probability model

$$p(C, F_1, \ldots, F_n)$$

which can be rewritten as follows, using repeated applications of the definition of conditional probability:

$$p(C, F_1, ..., F_n)$$

$$= p(C) \ p(F_1, ..., F_n | C)$$

$$= p(C) \ p(F_1 | C) \ p(F_2, ..., F_n | C, F_1)$$

$$= p(C) \ p(F_1 | C) \ p(F_2 | C, F_1) \ p(F_3, ..., F_n | C, F_1, F_2)$$

$$= p(C) \ p(F_1 | C) \ p(F_2 | C, F_1) \ p(F_3 | C, F_1, F_2) \ p(F_4, ..., F_n | C, F_1, F_2, F_3)$$

and so forth. Now the "naive" conditional independence assumptions come into play: assume that each feature  $F_i$  is conditionally independent of every other feature  $F_i$  for  $j \neq i$ . This means that

$$p(F_i|C, F_j) = p(F_i|C)$$

and so the joint model can be expressed as

$$p(C, F_1, ..., F_n) = p(C) \ p(F_1|C) \ p(F_2|C) \ p(F_3|C) \cdots$$
  
=  $p(C) \prod_{i=1}^n p(F_i|C).$ 

Source: Wikipedia

## Independence vs Conditional independence



- Independence: P(A,B) = P(A) \* P(B)
- Conditional Independence: P(A,B|C) = P(A|C) \* P(B|C)
- Indep does not imply conditional indep
  - Consider tossing a fair coin twice
    - A is event of getting head in 1st toss
    - B is event of getting head in 2nd toss
    - C is event of getting exactly one head
  - Then A={HT, HH}, B={HH, TH} and C={HT, TH}
  - $P(A,B|C) = P({HH}|C) = 0$
  - $-P(A|C) = P(A,C)/P(C) = P({HT})/P(C) = (1/4)/(1/2) = 1/2$
  - Similarly, P(B|C) = 1/2

Source: Choi Kwok Pui

# Example Use of Bayesian: Design of screen NUS National University of Singapore for macromolecular crystallization

- Hennessy et al., Acta Cryst D56:817-827, 2000
- Xtallization of proteins requires search of expt settings to find right conditions for diffractionquality xtals
- BMCD is a db of known xtallization conditions
- Use Bayes to determine prob of success of a set of expt conditions based on BMCD

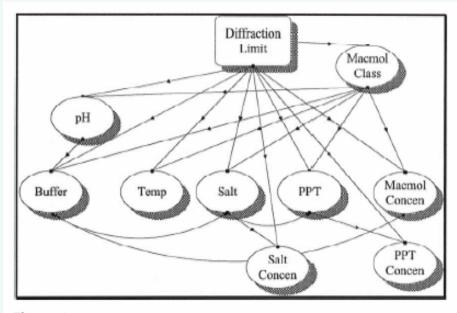


Figure 1

Crystallization parameter dependency graph. The graph represents the parameters included in the calculation of the estimated probability of success and their dependencies. A connecting arc from pH to buffer indicates that the probability distribution for the buffer may depend on the value of the pH. The lack of a connecting arc between two parameters reflects conditional independence (the probability distribution for a parameter is independent of the value of the other parameter).

### Hidden Markov models



#### What is a HMM



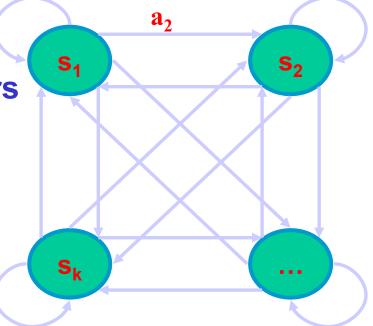
HMM is a stochastic generative

model for seqs

Defined by model parameters

- finite set of states S
- finite alphabet A
- transition prob matrix T
- emission prob matrix E

 Move from state to state as per T while emitting symbols as per E



#### Order of a HMM



- In nth order HMM, T & E depend on all n previous states
- E.g., for 1st order HMM, given emissions  $X = x_1, x_2, \dots$ , & states  $S = s_1, s_2, \dots$ , the prob of this seq is

$$Prob(X, S) = \prod_{i} Prob(x_{i}|s_{i}) = \prod_{i} E(x_{i}|s_{i}) * T(s_{i-1}, s_{i})$$

## Using HMM



- Given the model parameters, compute the probability of a particular output sequence. Solved by the forward algorithm
- Given the model parameters, find the most likely sequence of (hidden) states which could have generated a given output sequence. Solved by the Viterbi algorithm
- Given an output sequence, find the most likely set of state transition and output probabilities. Solved by the Baum-Welch algorithm

Exercise: Describe these algorithms

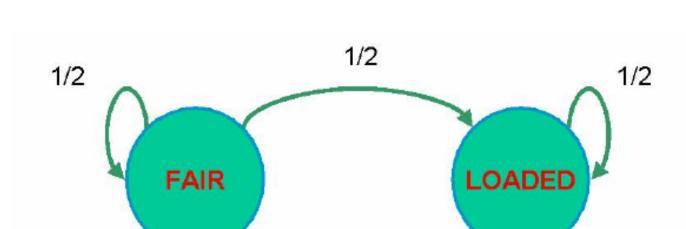
## Example: Dishonest casino



- Casino has two dices:
  - Fair dice
    - P(i) = 1/6, i = 1..6
  - Loaded dice
    - P(i) = 1/10, i = 1..5
    - P(i) = 1/2, i = 6
- Casino switches betw fair
   & loaded die with prob 1/2.
   Initially, dice is always fair

- Game:
  - You bet \$1
  - You roll
  - Casino rolls
  - Highest number wins \$2
- Question: Suppose we played 2 games, and the sequence of rolls was 1, 6, 2, 6. Were we likely to have been cheated?

## "Visualization" of dishonest casin



1/2

#### **Emission Matrix**

E(1 Fair) =	1/6	E(1 Loaded) =	1/10
E(2 Fair) =		E(2 Loaded) =	1/10
E(3 Fair) =	1/6	E(3 Loaded) =	1/10
E(4 Fair) =	1/6	E(4 Loaded) =	1/10
E(5 Fair) =	1/6	E(5 Loaded) =	1/10
F(61Fair) =	1/6	F(611 paded) =	1/2

#### **Transition Matrix**

T(Loaded, Loaded) = 1/2 T(Loaded, Fair) = 1/2 T(Fair, Fair) = 1/2 T(Fair, Loaded) = 1/2 T(?, Fair) = 1.0 T(?, Loaded) = 0.0

## 1, 6, 2, 6? We were probably cheated...



$$Prob(X, S = Fair, Fair, Fair, Fair) = E(1|Fair) * T(?, Fair) * \\ E(6|Fair) * T(Fair, Fair) * \\ E(2|Fair) * T(Fair, Fair) * \\ E(6|Fair) * T(Fair, Fair) * \\ = \frac{1}{6} * 1 * \frac{1}{6} * \frac{1}{2} * \frac{1}{6} * \frac{1}{2} * \frac{1}{6} * \frac{1}{2} \\ = 9.6451 * 10^{-5}$$

$$Prob(X, S = Fair, Loaded, Fair, Loaded) = E(1|Fair) * T(?, Fair) * \\ E(6|Loaded) * T(Fair, Loaded) * \\ E(2|Fair) * T(Loaded, Fair) * \\ E(6|Loaded) * T(Fair, Loaded) * \\ = \frac{1}{6} * 1 * \frac{1}{2} * \frac{1}{2} * \frac{1}{6} * \frac{1}{2} * \frac{1}{2} * \frac{1}{2} * \frac{1}{2} * \\ = 8.6806 * 10^{-4}$$

# Example Use of HMM: Protein families model Grand Singap

- Baldi et al., PNAS 91:1059-1063, 1994
- HMM is used to model families of biological sequences, such as kinases, globins, & immunoglobulins
- Bateman et al., NAR 32:D138-D141, 2004
- HMM is used to model 6190 families of protein domains in Pfam

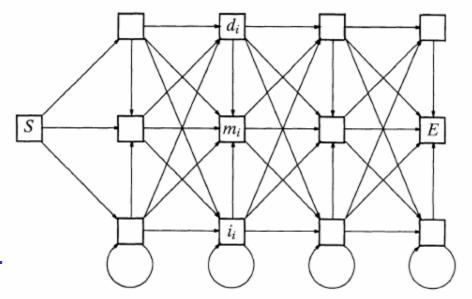


Fig. 1. HMM architecture. S and E are the start and end states. Sequence of main states  $m_i$  is the backbone. Side states  $d_i$  (resp.  $i_i$ ) correspond to deletions (resp. insertions).

## Concluding remarks...



#### What have we learned?



- Decision trees
- Decision trees ensembles
  - Bagging
- Other methods
  - K-nearest neighbour
  - Support vector machines
  - Naïve Bayes
  - Hidden Markov models

## Any question?







- http://www.cs.waikato.ac.nz/ml/weka
- Weka is a collection of machine learning algorithms for data mining tasks. The algorithms can either be applied directly to a dataset or called from your own Java code. Weka contains tools for data pre-processing, classification, regression, clustering, association rules, and visualization.

Exercise: Download a copy of WEKA. What are the names of classifiers in WEKA that correspond to C4.5 and SVM?

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- The dishonest casino example came from slides inherited from Ken Sung
- The "indep vs conditional indep" example came from Choi Kwok Pui

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