For written notes on this lecture, please read chapter 3 of *The Practical Bioinformatician. Alternatively, please read* "Rule-Based Data Mining Methods for Classification Problems in Biomedical Domains", a tutorial at *PKDD04* by Jinyan Li and Limsoon Wong, September 2004. http://www.comp.nus.edu.sg/~wongls/talks/pkdd04/

#### CS2220: Introduction to Computational Biology Unit 1b: Essence of Knowledge Discovery

Wong Limsoon



## Outline



- Overview of
   supervised learning
  - Decision trees
- Decision tree ensembles
  - Bagging

- Other methods
  - K-nearest neighbour
  - Support vector machines
  - Naïve Bayes
  - Hidden Markov models

#### Overview of supervised learning



#### Supervised learning



- Also called classification
- Learn from past experience, and use the learned knowledge to classify new data
- Knowledge learned by intelligent algorithms
- Examples:
  - Clinical diagnosis for patients
  - Cell type classification





- Classification application involves > 1 class of data. E.g.,
  - Normal vs disease cells for a diagnosis problem
- Training data is a set of instances (samples, points, etc.) with known class labels
- Test data is a set of instances whose class labels are to be predicted

#### **Notations**



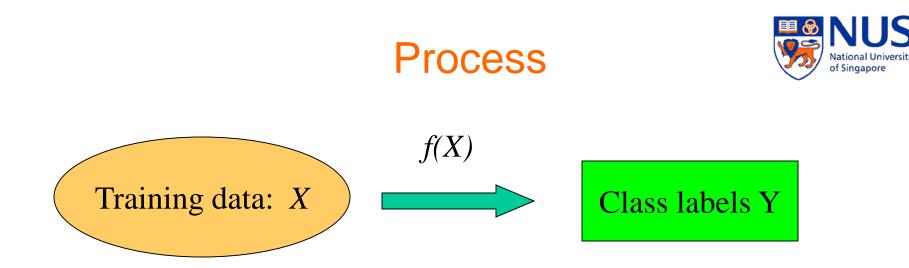
6

• Training data

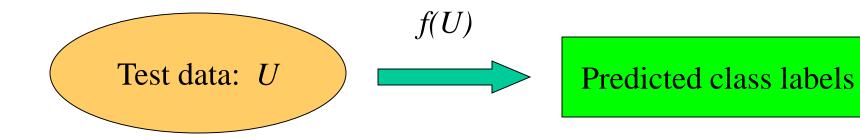
 $\{\langle x_1, y_1 \rangle, \langle x_2, y_2 \rangle, ..., \langle x_m, y_m \rangle\}$ where  $x_j$  are n-dimensional vectors and  $y_j$  are from a discrete space Y. E.g., Y = {normal, disease}

• Test data

 $\{\langle u1,?\rangle,\langle u2,?\rangle,...,\langle uk,?\rangle\,\}$ 



A classifier, a mapping, a hypothesis



#### **Relational representation**



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#### *n* features (order of 1000)



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#### Features (aka attributes)

- Categorical features
  - color = {red, blue, green}

#### • Continuous or numerical features

- gene expression
- age
- blood pressure
- Discretization

#### Example



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| Outlook  | Temp | Humidity | Windy | class |
|----------|------|----------|-------|-------|
| Sunny    | 75   | 70       | true  | Play  |
| Sunny    | 80   | 90       | true  | Don't |
| Sunny    | 85   | 85       | false | Don't |
| Sunny    | 72   | 95       | true  | Don't |
| Sunny    | 69   | 70       | false | Play  |
| Overcast | 72   | 90       | true  | Play  |
| Overcast | 83   | 78       | false | Play  |
| Overcast | 64   | 65       | true  | Play  |
| Overcast | 81   | 75       | false | Play  |
| Rain     | 71   | 80       | true  | Don't |
| Rain     | 65   | 70       | true  | Don't |
| Rain     | 75   | 80       | false | Play  |
| Rain     | 68   | 80       | false | Play  |
| Rain     | 70   | 96       | false | Play  |

## Overall picture of supervised learning



# Labelled Data + Algorithms

Biomedical Financial Government Scientific Decision trees Emerging patterns SVM Neural networks

Classifiers (Medical Doctors)

## Recap: Evaluation of a classifier

- Performance on independent blind test data
  - Blind test data properly represent real world
- K-fold cross validation
  - Given a dataset, divide it into k even parts, k-1 of them are used for training, and the rest one part treated as test data
- LOOCV, a special case of K-fold cross validation
- Accuracy, error rate, false positive rate, false negative rate, sensitivity, specificity, precision



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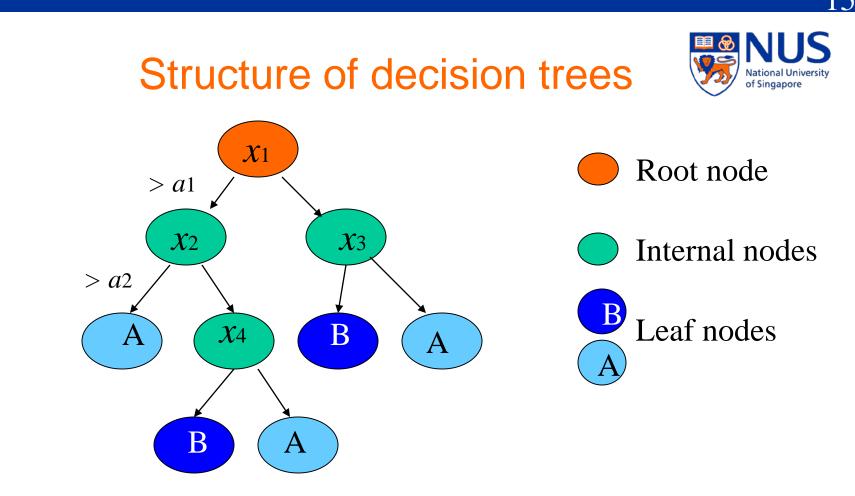
## Requirements of biomedical classification

 High accuracy, sensitivity, specificity, precision

• High comprehensibility

## Importance of rule-based method

- Systematic selection of a small number of features used for the decision making
- ⇒ Increase comprehensibility of the knowledge patterns
- C4.5 and CART are two commonly used rule induction algorithms---a.k.a. decision tree induction algorithms

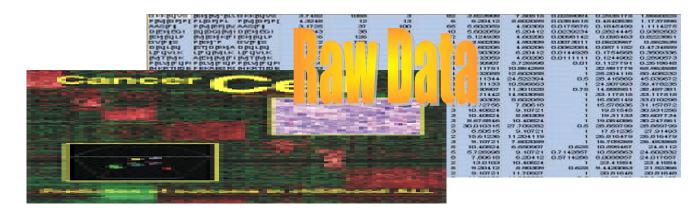


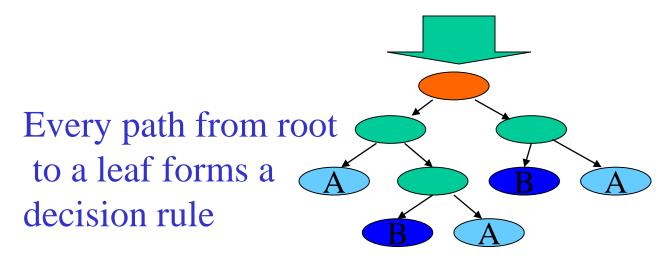
- If x1 > a1 & x2 > a2, then it's A class
- C4.5, CART, two of the most widely used
- Easy interpretation, but accuracy maybe unattractive

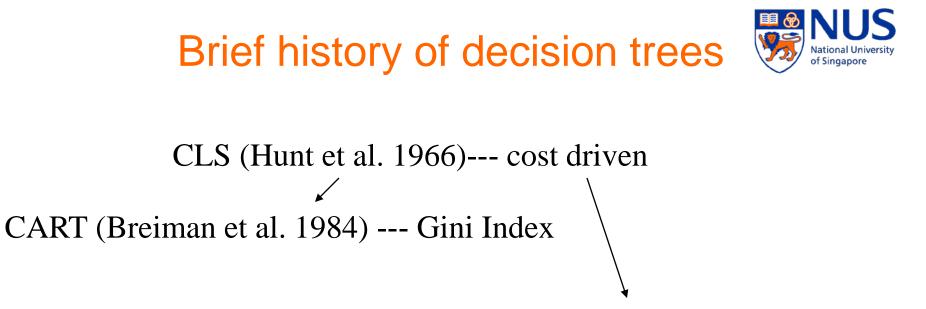


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#### **Elegance of decision trees**







ID3 (Quinlan, 1986) --- Information-driven

C4.5 (Quinlan, 1993) --- Gain ratio + Pruning ideas

#### A simple dataset



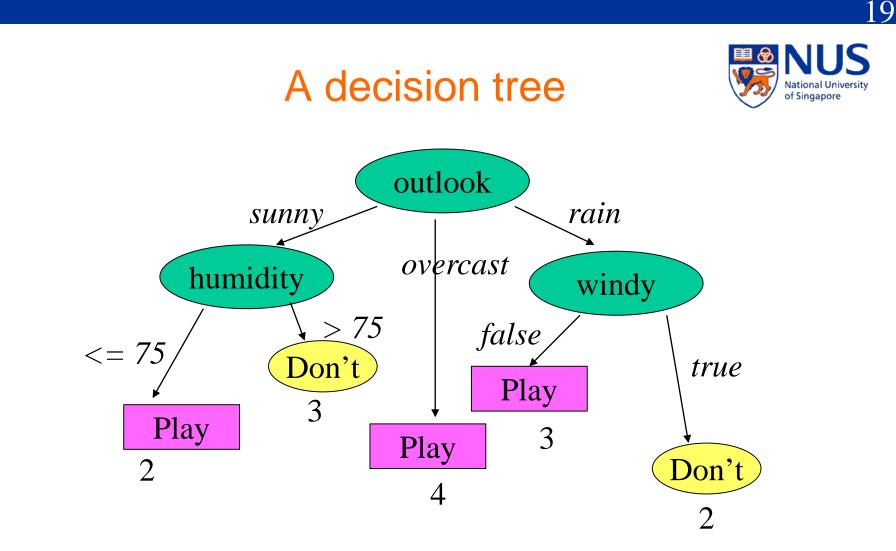
18

| Outlook  | Temp | Humidity | Windy | class |
|----------|------|----------|-------|-------|
| Sunny    | 75   | 70       | true  | Play  |
| Sunny    | 80   | 90       | true  | Don't |
| Sunny    | 85   | 85       | false | Don't |
| Sunny    | 72   | 95       | true  | Don't |
| Sunny    | 69   | 70       | false | Play  |
| Overcast | 72   | 90       | true  | Play  |
| Overcast | 83   | 78       | false | Play  |
| Overcast | 64   | 65       | true  | Play  |
| Overcast | 81   | 75       | false | Play  |
| Rain     | 71   | 80       | true  | Don't |
| Rain     | 65   | 70       | true  | Don't |
| Rain     | 75   | 80       | false | Play  |
| Rain     | 68   | 80       | false | Play  |
| Rain     | 70   | 96       | false | Play  |

9 Play samples

5 Don't

A total of 14.



• Construction of a tree is equiv to determination of root node of the tree and root nodes of its sub-trees

Exercise: What is the accuracy of this tree?

#### Food for thought

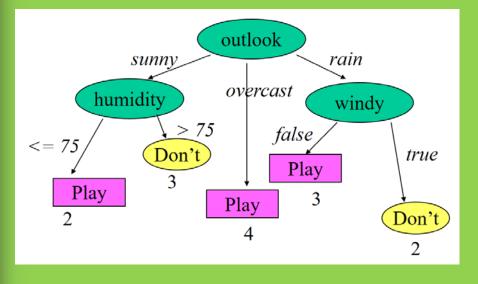


Exercise #1

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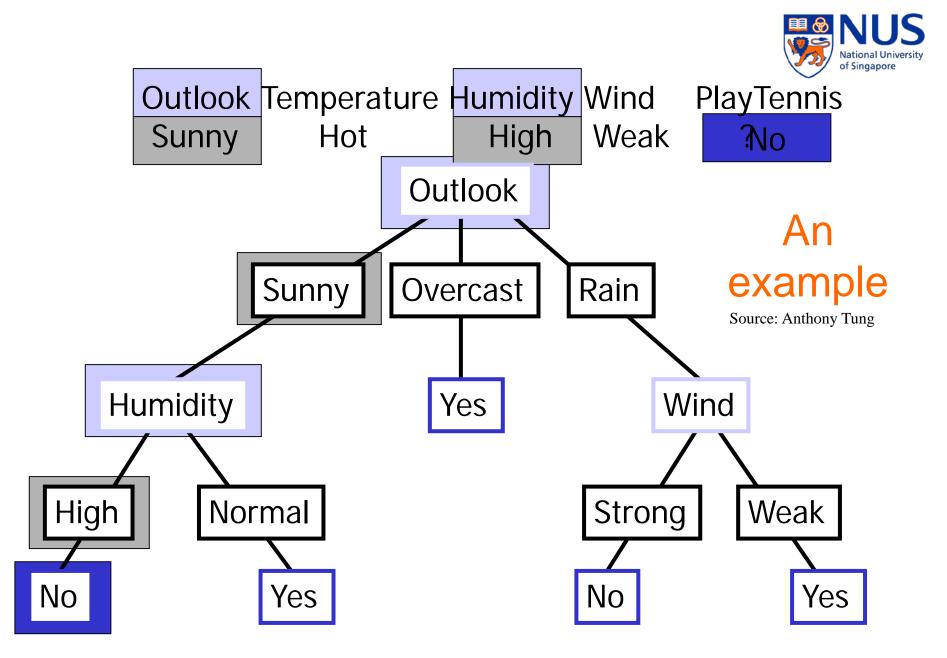
| Outlook  | Temp | Humidity | Windy | class |
|----------|------|----------|-------|-------|
| Sunny    | 75   | 70       | true  | Play  |
| Sunny    | 80   | 90       | true  | Don't |
| Sunny    | 85   | 85       | false | Don't |
| Sunny    | 72   | 95       | true  | Don't |
| Sunny    | 69   | 70       | false | Play  |
| Overcast | 72   | 90       | true  | Play  |
| Overcast | 83   | 78       | false | Play  |
| Overcast | 64   | 65       | true  | Play  |
| Overcast | 81   | 75       | false | Play  |
| Rain     | 71   | 80       | true  | Don't |
| Rain     | 65   | 70       | true  | Don't |
| Rain     | 75   | 80       | false | Play  |
| Rain     | 68   | 80       | false | Play  |
| Rain     | 70   | 96       | false | Play  |



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• What is the accuracy of this decision tree?

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Most discriminatory feature

- Every feature can be used to partition the training data
- If the partitions contain a pure class of training instances, then this feature is most discriminatory

#### Example of partitions



#### • Categorical feature

- Number of partitions of the training data is equal to the number of values of this feature
- Numerical feature
  - Two partitions

|  |                |                  |          |           |                   | 24                       |
|--|----------------|------------------|----------|-----------|-------------------|--------------------------|
| Catego   | orical feature | Numerical featur | re       |           |                   | US                       |
| ſ  |                |                  |          |           | Nation<br>of Sing | nal University<br>gapore |
| Instance #   | Outlook        | Temp             | Humidity | Windy     | class             |                          |
| 1  | Sunny          | 75               | 70       | true      | Play              |                          |
| 2  | Sunny          | 80               | 90       | true      | Don't             |                          |
| 3  | Sunny          | 85               | 85       | false     | Don't             |                          |
| 4  | Sunny          | 72               | 95       | true      | Don't             |                          |
| 5  | Sunny          | 69               | 70       | false     | Play              |                          |
| 6  | Overcast       | 72               | 90       | true      | Play              |                          |
| 7  | Overcast       | 83               | 78       | false     | Play              |                          |
| 8  | Overcast       | 64               | 65       | true      | Play              |                          |
| 9  | Overcast       | 81               | 75       | false     | Play              |                          |
| 10   | Rain           | 71               | 80       | true      | Don't             |                          |
| 11   | Rain           | 65               | 70       | true      | Don't             |                          |
| 12   | Rain           | 75               | 80       | false     | Play              |                          |
| 13   | Rain           | 68               | 80       | false     | Play              |                          |
| 14   | Rain           | 70               | 96       | false     | Play              |                          |
| $\mathbf{x} = \mathbf{x} = $ |                |                  |          | Comminate |                   |                          |

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| Categorical featureInstance #OutlookTempHumidityWindyclass1Sunny7570truePlay2Sunny8090trueDon't3Sunny8585falseDon't4Sunny7295trueDon't5Sunny6970falsePlay6Overcast7290truePlay7Overcast8378falsePlay8Overcast6465truePlay9Overcast8175falsePlay10Rain7180trueDon't12Rain6880falsePlay13Rain6880falsePlay14Rain7096falsePlay | Outlook = $sunny$ $1,2,3,4,5$ $P,D,D,D,P$ |
|---|---|
| Total 14 training   | Outlook = $6,7,8,9$                       |
| instances   | overcast $P,P,P,P$                        |
| A categorical feature is  | Outlook = $10,11,12,13,14$                |
| partitioned based on its  | D, D, P, P, P                             |
| number of possible values   | rain                                      |

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| Numerical feature |          |      |          |       |       |  |  |
|-------------------|----------|------|----------|-------|-------|--|--|
| Instance #        | Outlook  | Temp | Humidity | Windy | class |  |  |
| 1                 | Sunny    | 75   | 70       | true  | Play  |  |  |
| 2                 | Sunny    | 80   | 90       | true  | Don't |  |  |
| 3                 | Sunny    | 85   | 85       | false | Don't |  |  |
| 4                 | Sunny    | 72   | 95       | true  | Don't |  |  |
| 5                 | Sunny    | 69   | 70       | false | Play  |  |  |
| 6                 | Overcast | 72   | 90       | true  | Play  |  |  |
| 7                 | Overcast | 83   | 78       | false | Play  |  |  |
| 8                 | Overcast | 64   | 65       | true  | Play  |  |  |
| 9                 | Overcast | 81   | 75       | false | Play  |  |  |
| 10                | Rain     | 71   | 80       | true  | Don't |  |  |
| 11                | Rain     | 65   | 70       | true  | Don't |  |  |
| 12                | Rain     | 75   | 80       | false | Play  |  |  |
| 13                | Rain     | 68   | 80       | false | Play  |  |  |
| 14                | Rain     | 70   | 96       | false | Play  |  |  |

of Singapore Temperature 5,8,11,13,14 <=70P,P, D, P, P Temperature 1,2,3,4,6,7,9,10,12 P,D,D,D,P,P,P,D,P > 70

A numerical feature is generally partitioned by choosing a "cutting point"

Total 14 training

instances

26

#### **Decision tree construction**



- Select the "best" feature as root node of the whole tree
- Partition dataset into subsets using this feature so that the subsets are as "pure" as possible
- After partition by this feature, select the best feature (wrt the subset of training data) as root node of this sub-tree
- Recursively, until the partitions become pure or almost pure

#### Let's construct a decision tree



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| Outlook  | Temp | Humidity | Windy | class  |
|----------|------|----------|-------|--------|
| Sunny    | 75   | 70       | true  | Play   |
| Sunny    | 80   | 90       | true  | Don't  |
| Sunny    | 85   | 85       | false | Don't  |
| Sunny    | 72   | 95       | true  | Don't  |
| Sunny    | 69   | 70       | false | Play   |
| Overcast | 72   | 90       | true  | Play   |
| Overcast | 83   | 78       | false | Play   |
| Overcast | 64   | 65       | true  | Play   |
| Overcast | 81   | 75       | false | Play   |
| Rain     | 71   | 80       | true  | Don't  |
| Rain     | 65   | 70       | true  | Don't  |
| Rain     | 75   | 80       | false | Play   |
| Rain     | 68   | 80       | false | Play   |
| Rain     | 70   | 96       | false | Play 💄 |

Ask the class to pick root node and construct the tree recursively with them... How good is that tree?

Exercise #2

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Three measures to evaluate which feature is best

- Gini index
- Information gain
- Information gain ratio

Look the last two up yourself

#### Gini index



$$gini(S) = \frac{\text{diff of two arbitrary specimen in } S}{\text{mean specimen in } S}$$

- = prob(getting two specimen of diff class in S)
- = 1 prob(getting two specimen of same class in S)

=  $1 - \sum_{i} \operatorname{prob}(\operatorname{getting specimen of class } i \text{ in } S)^2$ 

- Gini index is the expected value of the ratio of the diff of two arbitrary specimens to the mean value of all specimens
- Closer to 1, feature is similar to "background distribution". Closer to 0, feature is "unexpected"

#### Gini index



Let  $\mathcal{U} = \{C_1, ..., C_k\}$  be all the classes. Suppose we are currently at a node and D is the set of those samples that have been moved to this node. Let f be a feature and d[f]be the value of the feature f in a sample d. Let S be a range of values that the feature f can take. Then the Gini index for f in D for the range S is defined as

$$gini_f^D(S) = 1 - \sum_{C_i \in \mathcal{U}} \left( \frac{|\{d \in D \mid d \in C_i, d[f] \in S\}|}{|D|} \right)^2$$

The purity of a split of the value range S of an attribute f by some split-point into subranges  $S_1$ and  $S_2$  is then defined as

$$gini_f^D(S_1, S_2) = \sum_{S \in \{S_1, S_2\}} \frac{|\{d \in D \mid d[f] \in S\}|}{|D|} * gini_f^D(S)$$

we choose the feature f and the split-point p that minimizes  $gini_f^D(S_1, S_2)$  over all possible alternative features and split-points.

#### Gini index of "Outlook"



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| Outlook  | Temp | Humidity | Windy | class |
|----------|------|----------|-------|-------|
| Sunny    | 75   | 70       | true  | Play  |
| Sunny    | 80   | 90       | true  | Don't |
| Sunny    | 85   | 85       | false | Don't |
| Sunny    | 72   | 95       | true  | Don't |
| Sunny    | 69   | 70       | false | Play  |
| Overcast | 72   | 90       | true  | Play  |
| Overcast | 83   | 78       | false | Play  |
| Overcast | 64   | 65       | true  | Play  |
| Overcast | 81   | 75       | false | Play  |
| Rain     | 71   | 80       | true  | Don't |
| Rain     | 65   | 70       | true  | Don't |
| Rain     | 75   | 80       | false | Play  |
| Rain     | 68   | 80       | false | Play  |
| Rain     | 70   | 96       | false | Play  |

$$gini_f^D(S) = 1 - \sum_{C_i \in \mathcal{U}} \left( \frac{|\{d \in D \mid d \in C_i, \ d[f] \in S\}|}{|D|} \right)^2$$

$$gini_f^D(S_1, S_2) = \sum_{S \in \{S_1, S_2\}} \frac{|\{d \in D \mid d[f] \in S\}|}{|D|} * gini_f^D(S)$$

- gini(Sunny) =  $1 (2/5)^2 (3/5)^2 = 0.48$
- gini(Overcast) =  $1 (4/4)^2 (0/5)^2 = 0$
- gini(Rain) =  $1 (3/5)^2 (2/5)^2 = 0.48$
- gini(Outlook) = 5/14 \* 0.48 + 4/14 \* 0 + 5/14 \* 0.48 = 0.34

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- Single coverage of training data (elegance)
- Divide-and-conquer splitting strategy
- Fragmentation problem ⇒ Locally reliable but globally insignificant rules

Miss many globally significant rules; mislead system



Example Use of Decision Tree Methods: **Proteomics Approaches to Biomarker Discovery** 

- In prostate and bladder cancers (Adam et al. *Proteomics*, 2001)
- In serum samples to detect breast cancer (Zhang et al. *Clinical Chemistry*, 2002)
- In serum samples to detect ovarian cancer (Petricoin et al. *Lancet*; Li & Rao, *PAKDD* 2004)

#### Decision tree ensembles



## Motivating example



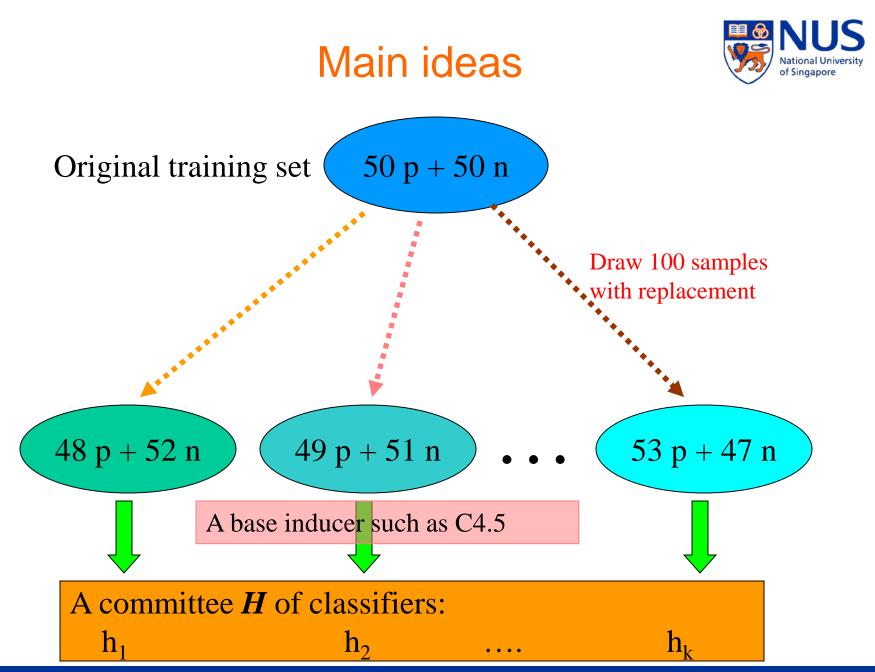
36

- $h_1$ ,  $h_2$ ,  $h_3$  are indep classifiers w/ accuracy = 60%
- C<sub>1</sub>, C<sub>2</sub> are the only classes
- t is a test instance in C<sub>1</sub>
- $h(t) = argmax_{C \in \{C1, C2\}} |\{h_j \in \{h_1, h_2, h_3\} | h_j(t) = C\}|$
- Then prob(h(t) = C<sub>1</sub>)
  - $= \operatorname{prob}(h_{1}(t)=C_{1} \& h_{2}(t)=C_{1} \& h_{3}(t)=C_{1}) + \operatorname{prob}(h_{1}(t)=C_{1} \& h_{2}(t)=C_{1} \& h_{3}(t)=C_{2}) + \operatorname{prob}(h_{1}(t)=C_{1} \& h_{2}(t)=C_{2} \& h_{3}(t)=C_{1}) + \operatorname{prob}(h_{1}(t)=C_{2} \& h_{2}(t)=C_{1} \& h_{3}(t)=C_{1}) \\ = 60\% * 60\% * 60\% + 60\% * 60\% * 40\% + 60\% * 40\% + 60\% * 60\% * 60\% = 64.8\%$





- Proposed by Breiman (1996)
- Also called Bootstrap aggregating
- Make use of randomness injected to training data



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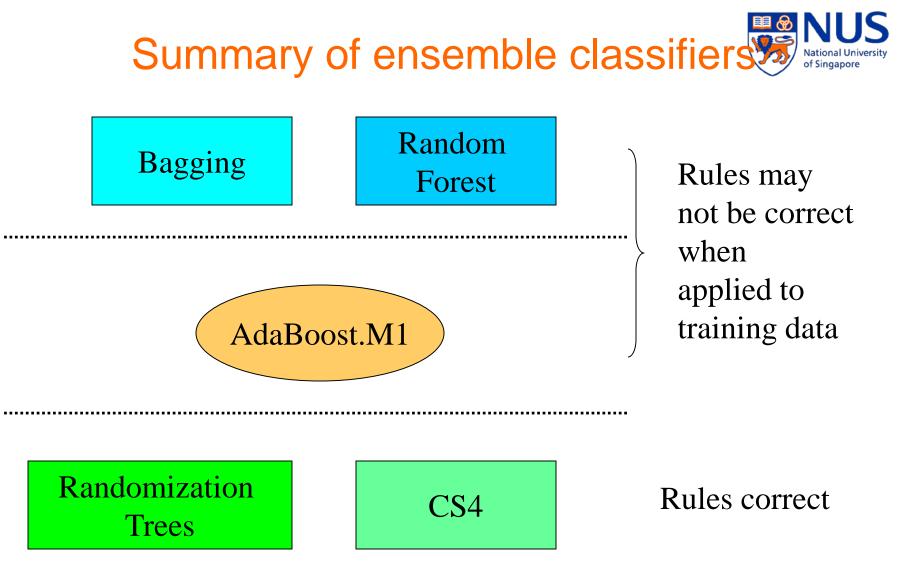
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Given a new test sample T

$$bagged(T) = \operatorname{argmax}_{C_j \in \mathcal{U}} |\{h_i \in \mathcal{H} \mid h_i(T) = C_j\}|$$
  
where  $\mathcal{U} = \{C_1, ..., C_r\}$ 

• What does this formula mean?

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Exercise: Describe the decision tree ensemble classifiers not explained in this ppt

#### Other machine learning approaches



#### Outline



Exercise #4

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- K-nearest neighbor (kNN)
- Support vector machines (SVM)
- Naïve Bayes
- Hidden Markov models (HMM)

## Can you present one of these machine learning approaches?

### K-nearest neighbours



#### How kNN works



- Given a new case
- Find k "nearest" neighbours, i.e., k most similar points in the training data set
- Assign new case to the same class to which most of these neighbours belong

 A common "distance" measure betw samples x and y is

$$\sqrt{\sum_f (x[f] - y[f])^2}$$

where f ranges over features of the samples

Exercise: What does the formula above mean?



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#### Illustration of kNN (k=8)

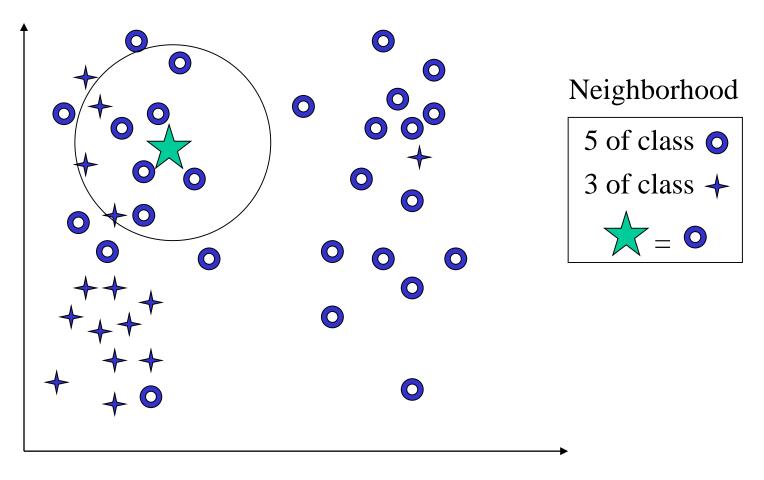


Image credit: Zaki

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#### Some issues



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- Simple to implement
- Must compare new case against all training cases
- $\Rightarrow$  May be slow during prediction
- No need to train
- But need to design distance measure properly
- $\Rightarrow$  May need expert for this
- Can't explain prediction outcome
- $\Rightarrow$  Can't provide a model of the data

#### Example Use of kNN Ovarian cancer diagnosis based of singapore SELDI proteomic data

- Li et al, *Bioinformatics* 20:1638-1640, 2004
- Use kNN to diagnose ovarian cancers using proteomic spectra
- Data set is from Petricoin et al., *Lancet* 359:572-577, 2002

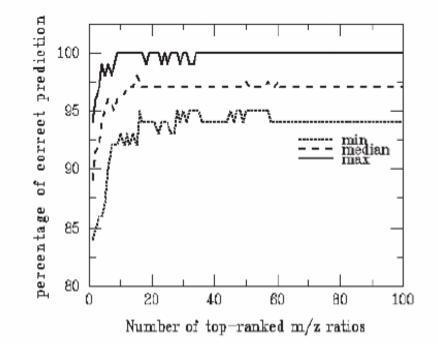


Fig. 1. Minimum, median and maximum of percentages of correct prediction as a function of the number of top-ranked m/z ratios in 50 independent partitions into learning and validation sets.

#### Support vector machines



#### **Basic idea**



Image credit: Zien

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 $\cap$ C feature n input input space space space. Φ 1 b, (c)(a) (b)

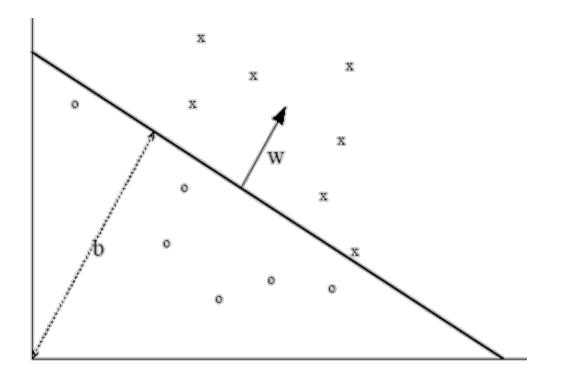
(a) Linear separation not possible w/o errors
(b) Better separation by nonlinear surfaces in input space
(c) Nonlinear surface corr to linear surface in feature space. Map from input to feature space by "kernel" function Φ

 $\Rightarrow$  "Linear learning machine" + kernel function as classifier

#### Linear learning machines



- Hyperplane separating the x's and o's points is given by (W•X) + b = 0, with (W•X) = Σ<sub>j</sub>W[j]\*X[j]
- $\Rightarrow$  Decision function is IIm(X) = sign((W•X) + b))





#### Linear learning machines

- Solution is a linear combination of training points  $X_k$  with labels  $Y_k$ 

$$\mathbf{W} = \sum_{\mathbf{k}} \alpha_{\mathbf{k}}^{*} \mathbf{Y}_{\mathbf{k}}^{*} \mathbf{X}_{\mathbf{k}},$$

with  $\alpha_k > 0$ , and  $Y_k = \pm 1$ 

 $\Rightarrow IIm(X) = sign(\Sigma_k \alpha_k * Y_k * (X_k \bullet X) + b)$ 



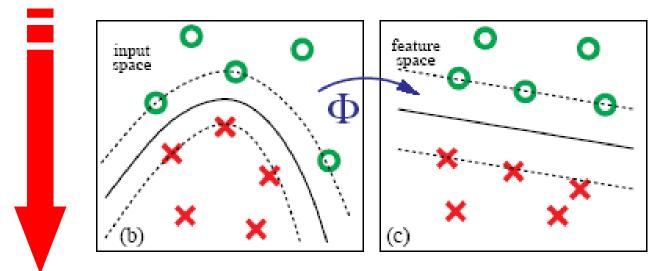
"data" appears only in dot product!

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#### Kernel function

• IIm(X) = sign( $\Sigma_k \alpha_k^* Y_k^* (X_k \bullet X) + b$ )



- $svm(X) = sign(\Sigma_k \alpha_k^* Y_k^* (\Phi X_k \bullet \Phi X) + b)$
- $\Rightarrow svm(X) = sign(\Sigma_k \alpha_k^* Y_k^* K(X_k, X) + b)$ where K(X\_k, X) = ( $\Phi X_k^{\bullet} \Phi X$ )

#### **Kernel** function



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- $svm(X) = sign(\Sigma_k \alpha_k^* Y_k^* K(X_k, X) + b)$
- $\Rightarrow$  K(A,B) can be computed w/o computing  $\Phi$
- In fact replace it w/ lots of more "powerful" kernels besides (A • B). E.g.,

$$- K(A,B) = (A \bullet B)^d$$

$$- K(A,B) = \exp(- ||AB||^2 / (2^*\sigma)), \dots$$

#### How SVM works



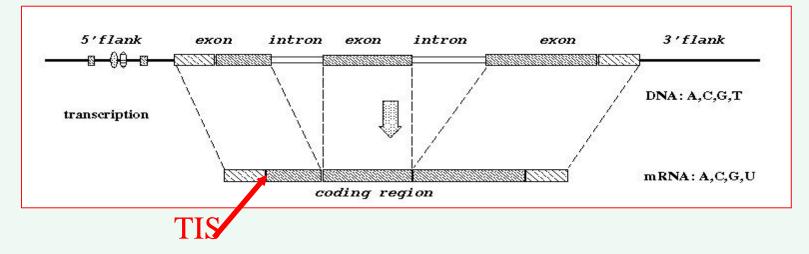
- $\operatorname{svm}(X) = \operatorname{sign}(\Sigma_k \alpha_k^* Y_k^* K(X_k, X) + b)$
- To find  $\alpha_k$  is a quadratic programming problem max:  $\Sigma_k \alpha_k - 0.5 * \Sigma_k \Sigma_h \alpha_k * \alpha_h Y_k * Y_h * K(X_k, X_h)$ subject to:  $\Sigma_k \alpha_k * Y_k = 0$ and for all  $\alpha_k$ ,  $C \ge \alpha_k \ge 0$
- To find b, estimate by averaging

$$\begin{split} \mathbf{Y}_{h} &- \boldsymbol{\Sigma}_{k} \boldsymbol{\alpha}_{k}^{*} \mathbf{Y}_{k}^{*} \ \mathbf{K}(\mathbf{X}_{h}, \mathbf{X}_{k}) \\ \text{for all } \boldsymbol{\alpha}_{h} \geq \mathbf{0} \end{split}$$



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# Example Use of SVM: Recognition of protein translation initiation sites



- Zien et al., *Bioinformatics* 16:799-807, 2000
- Use SVM to recognize protein translation initiation sites from genomic sequences
- Raw data set is same as Liu & Wong, *JBCB* 1:139-168, 2003







#### Bayes theorem

$$P(h|d) = \frac{P(d|h) * P(h)}{P(d)}$$

- P(h) = prior prob that hypothesis h holds
- P(d|h) = prob of observing data d given h holds
- P(h|d) = posterior prob that h holds given observed data d

#### Bayesian approach



 Let *H* be all possible classes. Given a test instance w/ feature vector {*f*<sub>1</sub> = *v*<sub>1</sub>, ..., *f*<sub>n</sub> = *v*<sub>n</sub>}, the most probable classification is given by

$$\operatorname{argmax}_{h_j \in H} P(h_j | f_1 = v_1, \dots, f_n = v_n)$$

• Using Bayes Theorem, rewrites to

$$\operatorname{argmax}_{h_j \in H} \frac{P(f_1 = v_1, \dots, f_n = v_n | h_j) * P(h_j)}{P(f_1 = v_1, \dots, f_n = v_n)}$$

Since denominator is independent of h<sub>j</sub>, this simplifies to

$$\operatorname{argmax}_{h_j \in H} P(f_1 = v_1, \dots, f_n = v_n | h_j) * P(h_j)$$

#### Naïve Bayes



- But estimating  $P(f_1=v_1, ..., f_n=v_n/h_j)$  accurately may not be feasible unless training data set is large
- "Solved" by assuming  $f_1, ..., f_n$  are conditionally independent of each other

• Then 
$$\operatorname{argmax}_{h_j \in H} P(f_1 = v_1, \dots, f_n = v_n | h_j) * P(h_j)$$

$$= \operatorname{argmax}_{h_j \in H} \prod_{i} P(f_i = v_i | h_j) * P(h_j)$$

where  $P(h_j)$  and  $P(f_i=v_i/h_j)$  can often be estimated reliably from typical training data set

Exercise: How do you estimate  $P(h_j)$  and  $P(f_j=v_j|h_j)$ ?

### Independence vs Conditional independence

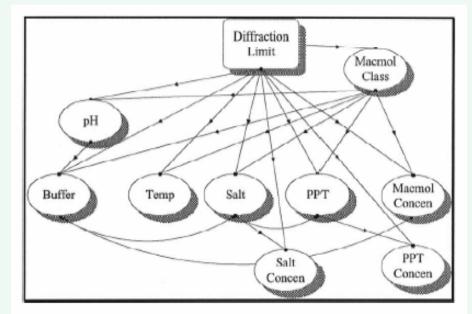


- Independence: P(A,B) = P(A) \* P(B)
- Conditional Independence: P(A,B|C) = P(A|C) \* P(B|C)
- Indep does not imply conditional indep
  - Consider tossing a fair coin twice
    - A is event of getting head in 1st toss
    - B is event of getting head in 2nd toss
    - C is event of getting exactly one head
  - Then A={HT, HH}, B={HH, TH} and C={HT, TH}
  - $P(A,B|C) = P({HH}|C)=0$
  - $P(A|C) = P(A,C)/P(C) = P({HT})/P(C)=(1/4)/(1/2) = 1/2$
  - Similarly, P(B|C) = 1/2

Source: Choi Kwok Pui



- Hennessy et al., Acta Cryst D56:817-827, 2000
- Xtallization of proteins requires search of expt settings to find right conditions for diffractionquality xtals
- BMCD is a db of known xtallization conditions
- Use Bayes to determine prob of success of a set of expt conditions based on BMCD



#### Figure 1

Crystallization parameter dependency graph. The graph represents the parameters included in the calculation of the estimated probability of success and their dependencies. A connecting arc from pH to buffer indicates that the probability distribution for the buffer may depend on the value of the pH. The lack of a connecting arc between two parameters reflects conditional independence (the probability distribution for a parameter is independent of the value of the other parameter).

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#### Hidden Markov models

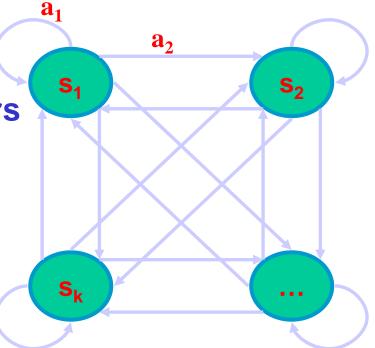


#### What is a HMM



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- HMM is a stochastic generative model for seqs
- Defined by model parameters
  - finite set of states S
  - finite alphabet A
  - transition prob matrix T
  - emission prob matrix E



• Move from state to state as per T while emitting symbols as per E

#### Order of a HMM



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- In *n*th order HMM, *T* & *E* depend on all *n* previous states
- E.g., for 1st order HMM, given emissions  $X = x_1, x_2, \dots, x_n$  & states  $S = s_1, s_2, \dots$ , the prob of this seq is

$$Prob(X,S) = \prod_{i} Prob(x_i|s_i) = \prod_{i} E(x_i|s_i) * T(s_{i-1},s_i)$$

### Using HMM



- Given the model parameters, compute the probability of a particular output sequence. Solved by the forward algorithm
- Given the model parameters, find the most likely sequence of (hidden) states which could have generated a given output sequence. Solved by the Viterbi algorithm
- Given an output sequence, find the most likely set of state transition and output probabilities. Solved by the Baum-Welch algorithm

Exercise: Describe these algorithms

### **Example: Dishonest casino**

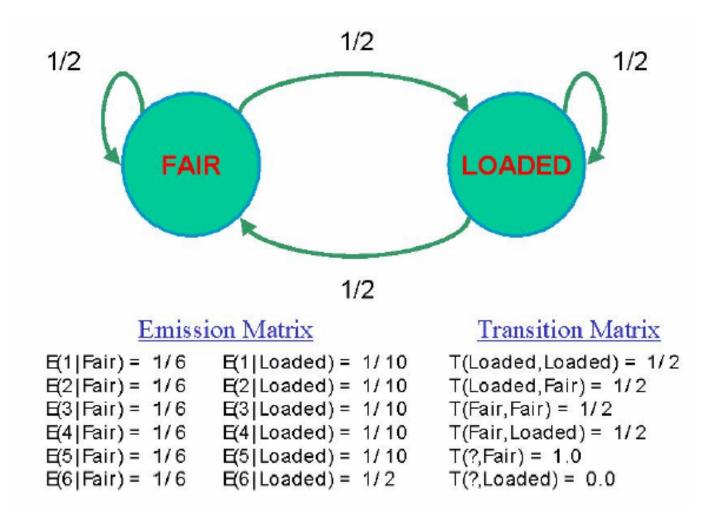


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- Casino has two dices:
  - Fair dice
    - P(i) = 1/6, i = 1..6
  - Loaded dice
    - P(i) = 1/10, i = 1..5
    - P(i) = 1/2, i = 6
- Casino switches betw fair & loaded die with prob 1/2. Initially, dice is always fair

- Game:
  - You bet \$1
  - You roll
  - Casino rolls
  - Highest number wins \$2
- Question: Suppose we played 2 games, and the sequence of rolls was 1, 6, 2, 6. Were we likely to have been cheated?





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### 1, 6, 2, 6? We were probably cheated...



$$\begin{array}{rcl} Prob(X,S=Fair,Fair,Fair,Fair) &=& E(1|Fair)*T(?,Fair)*\\ &=& E(6|Fair)*T(Fair,Fair)*\\ &=& E(2|Fair)*T(Fair,Fair)*\\ &=& E(6|Fair)*T(Fair,Fair)\\ &=& \frac{1}{6}*1*\frac{1}{6}*\frac{1}{2}*\frac{1}{6}*\frac{1}{2}*\frac{1}{6}*\frac{1}{2}\\ &=& 9.6451*10^{-5} \end{array}$$

Prob(X, S = Fair, Loaded, Fair, Loaded) = E(1|Fair) \* T(?, Fair) \* E(6|Loaded) \* T(Fair, Loaded) \*

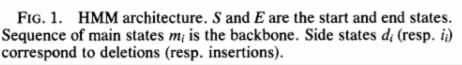
$$E(2|$$
 Fair  $) * T(Loaded, Fair) *$ 

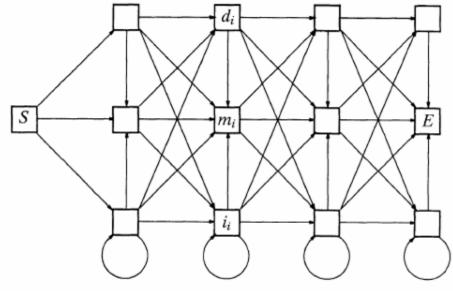
$$E(6|Loaded) * T(Fair, Loaded)$$

$$= \frac{1}{6} * 1 * \frac{1}{2} * \frac{1}{2} * \frac{1}{6} * \frac{1}{2} * \frac{1}{2} * \frac{1}{2}$$
  
= 8.6806 \* 10<sup>-4</sup>

### Example Use of HMM: Protein families model

- Baldi et al., PNAS 91:1059-1063, 1994
- HMM is used to model families of biological sequences, such as kinases, globins, & immunoglobulins
- Bateman et al., NAR 32:D138-D141, 2004
- HMM is used to model
   6190 families of protein
   domains in Pfam





#### Concluding remarks...





#### What have we learned?

- Decision trees
- Decision trees ensembles
  - Bagging
- Other methods
  - K-nearest neighbour
  - Support vector machines
  - Naïve Bayes
  - Hidden Markov models

### Any question?







- http://www.cs.waikato.ac.nz/ml/weka
- Weka is a collection of machine learning algorithms for data mining tasks. The algorithms can either be applied directly to a dataset or called from your own Java code. Weka contains tools for data pre-processing, classification, regression, clustering, association rules, and visualization.

Exercise: Download a copy of WEKA. What are the names of classifiers in WEKA that correspond to C4.5 and SVM?

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- Most of the slides used in this ppt came from a tutorial that WLS gave with Jinyan Li at the 8th European Conference on Principles and Practice of Knowledge Discovery in Databases, Pisa, Italy, 20-24 September 2004
- The dishonest casino example came from slides inherited from Ken Sung
- The "indep vs conditional indep" example came from Choi Kwok Pui

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