MCI5004: Molecular Biomarkers in Clinical Research Anna Karenina and the Careless Null Hypothesis in Omics Data Analysis

Wong Limsoon



### Anna Karenina Principle



Happy families are all alike; every unhappy family is unhappy in its own way. Leo Tolstoy www.thequotes.in

#### Translation

• There are many ways to violate the null hypothesis but only one way that is truly pertinent to the outcome of interest





#### from the book *Statistics from A to Z — Confusing Concepts Clarified.*

# **GETTING THE NULL HYPOTHESIS RIGHT**



#### **Example 1**

MCI5004, 2017

Copyright 2017 © Wong Limsoon

	Group						
SNP	Genotypes	Cont	rols [n(%)]	Cases	s [n(%)]	χ <sup>2</sup>	P value
rs123	AA	1	0.9%	0	0.0%		4.78E-21 <sup>b</sup>
	AG	38	35.2%	79	97.5%		
	GG	69	63.9%	2	2.5%		



A seemingly obvious conclusion

- A scientist claims the SNP rs123 is a great biomarker for a disease
  - If rs123 is AA or GG, unlikely to get the disease
  - If rs123 is AG, a 3:1 odd of getting the disease
- A straightforward  $\chi^2$  test. Anything more/wrong?

## **Careless null hypothesis**



6

#### "Effective" H0

 rs123 alleles are identically distributed <u>in the two samples</u>

#### Assumption

 Distributions of rs123 alleles in the two samples are identical to the two populations

#### Apparent H0

 rs123 alleles are identically distributed in the two populations

### Apparent H1

 rs123 alleles are differently distributed in the two populations

## **Refined null hypothesis**



i.e. sample

is biased

#### Refined H0

- Distributions of rs123 alleles in the two samples are identical to the two populations, **and**
- rs123 alleles are identically distributed in the two populations

- Refined H1
  - Distributions of rs123 alleles in the two samples are different from the two
    - populations, **or**
  - rs123 alleles are differently distributed in the two populations

# Sample bias is revealed by domain logic





Group							
SNP	Genotypes	Cont	rols [n(%)]	Case	s [n(%)]	χ²	P value
rs123	AA	1	0.9%	0	0.0%		4.78E-21 <sup>b</sup>
	AG	38	35.2%	79	97 <mark>.</mark> 5%		
	GG	69	63.9%	2	2.5%		

- AG = 38 + 79 = 117, controls + cases = 189 ⇒ population is ~62% AG ⇒ population is >9% AA, unless AA is lethal
- "Big data check" shows AA is non-lethal for this SNP ⇒ sample is biased

## Food for thought



9

#### Refined H0

- Distributions of rs123 alleles in the two samples are identical to the two populations, and
- rs123 alleles are identically distributed in the two populations

- Refined H1
  - Distributions of rs123 alleles in the two samples are different from the two populations, or
  - rs123 alleles are differently distributed in the two populations
- Suppose distributions of rs123 alleles in the samples are identical to the populations and the test is significant
- Can we say rs123 mutation causes the disease?



# Three types of reasoning

### Deduction

- All men are mortal
- Socrates is a man
- ⇒Socrates is mortal

### Induction

- Socrates is a man
- Socrates is mortal
- $\Rightarrow$ All men are mortal,

provided there is no counter example

### Abduction

- All men are mortal
- Socrates is mortal
- $\Rightarrow$ Socrates is a man,

provided there is no other explanation of Socrates' mortality

## Abduction in action



### Hypothesis

 If rs123 mutation causes disease, the statistical test is significant

		(	broup			
Genotypes	Cont	rols [n(%)]	Cases	s [n(%)]	χ <sup>2</sup>	P value
AA	1	0.9%	0	0.0%		4.78E-21 <sup>b</sup>
AG	38	35.2%	79	97.5%		
GG	69	63.9%	2	2.5%		
	Genotypes AA AG GG	Genotypes Cont AA 1 AG 38 GG 69	Genotypes      Controls [n(%)]        AA      1      0.9%        AG      38      35.2%        GG      69      63.9%	Genotypes      Controls [n(%)]      Cases        AA      1      0.9%      0        AG      38      35.2%      79        GG      69      63.9%      2	Genotypes      Controls [n(%)]      Cases [n(%)]        AA      1      0.9%      0      0.0%        AG      38      35.2%      79      97.5%        GG      69      63.9%      2      2.5%	Genotypes      Controls [n(%)]      Cases [n(%)]      χ²        AA      1      0.9%      0      0.0%        AG      38      35.2%      79      97.5%        GG      69      63.9%      2      2.5%

- Observation
  - Statistical test is significant
- Conclusion by abduction
  - rs123 mutation causes disease
  - provided there is no other explanation for the test to be significant

### Discussion

SNP

rs123

Group

0 0.0%

Cases [n(%)]

79 97.5%

2 2.5%

P value

4.78E-21<sup>b</sup>

Genotypes Controls [n(%)]

0.9%

38 35.2%

69 63.9%

AA

AG

GG

Abbreviation: SNP, single nucleotide polymorphism.



12

#### Hypothesis

- If rs123 mutation causes disease, the statistical test is significant
- Observation

#### - Statistical test is significant

#### Conclusion by abduction

- rs123 mutation causes disease
- provided there is no other explanation for the test to be significant
- How to incorporate "provided there is no other explanation" into the analysis?

### How about this?



13

- Choose a sample of Cases and a sample of Controls such that for each stratification p1/p2, the distribution of p1/p2 in Cases is same as the distribution of p1/p2 in Controls
  - i.e. equalize / control for other factors
- Then test:
  - H0
    - X's alleles are identically distributed in the two samples

- H1
  - X's alleles are differently distributed in the two samples

- This makes the significance of the test independent of other explanations
- It does not say "no other explanation"

### Or this?



14

#### • Look for another gene X such that

• H0

- Distributions of X's alleles in the two samples are identical to the two populations, and
- X's alleles are identically distributed in the two populations

#### • H1

- Distributions of X's alleles in the two samples are different from the two populations, **Or**
- X's alleles are differently distributed in the two populations
- When the red part of H1 is false, this implies gene X mutation is an alternative explanation for the significance of rs123 mutation and thus the disease. Why?



#### Example 2

MCI5004, 2017

Copyright 2017 © Wong Limsoon



# A seemingly obvious conclusion



Overall

	Α	В
lived	60	65
died	100	165

Looks like treatment A is better

## What is happening here?

#### Women

Ν/	^	n
IVI	e	
	_	

	Α	В
lived	40	15
died	20	5

	A	В
lived	20	50
died	80	160

Looks like treatment B is better

## **Careless null hypothesis**



#### "Effective" H0

 Treatments are identically distributed in the two samples

### Assumption

 All other factors are equalized in the two samples



Treatments are identically distributed in the two populations

### Apparent H1

 Treatments are differently distributed in the two populations

# **Refined null hypothesis**



18

#### Refined H0

- All other factors are equalized in the two samples, and
- Treatments are identically distributed in the two samples

### Refined H1

- Some factors are not equalized in the two samples, **Or**
- Treatments are differently distributed in the two populations
- Any other thing missing?



# A/B sample not equalized in other attributes, viz. sex



#### Overall

Men

	Α	В
lived	60	65
died	100	165

Women

	Α	В
lived	40	15
died	20	5

	Α	В
lived	20	50
died	80	160

### Taking A

- Men = 100 (63%)
- Women = 60 (37%)

### Taking B

- Men = 210 (91%)
- Women = 20 (9%)

 Exercise: Explain what causes A to be better than B overall



In statistical hypothesis testing, the **null distribution** is the probability **distribution** of the test statistic when the **null** hypothesis is true. For example, in an F-test, the **null distribution** is an F-**distribution**.



# GETTING THE NULL DISTRIBUTION RIGHT



#### **Example 3**

MCI5004, 2017

Copyright 2017 © Wong Limsoon





# A seemingly obvious conclusion

- A multi-gene signature is claimed as a good biomarker for breast cancer survival
  - Cox's survival model p-value << 0.05</li>
- A straightforward Cox's proportional hazard analysis. Anything more/wrong?



### Almost all random signatures also have p-value < 0.05

- Theoretical null distribution used in Cox's proportion hazard analysis does not match the empirical null distribution
- What can we do about this?

 $\log_{10}(0.05)$ 



p–value (log<sub>10</sub>)

Venet et al., PLOS Comput Biol, 2011

MCI5004, 2017

Copyright 2017 © Wong Limsoon

## **Careless null hypothesis**



#### "Effective" H0

- The biomarker's values are identically distributed in the two populations
- Assumption
  - The null distribution models real world



The biomarker's values are identically distributed in the two populations

### Apparent H1

The biomarker's values are differently distributed in the two populations

## Refined null hypothesis

### Refined H0

- The biomarker's values are identically distributed in the two populations, and
- The null distribution models real world

### Refined

- The biomarker's values are differently distributed in the two populations, **Or**
- The null distribution does not model real world





#### **Example 4**

MCI5004, 2017

Copyright 2017 © Wong Limsoon

# Gene-selection methods have poor reproducibility



- Low % of overlapping genes from diff expt in general
  - Prostate cancer
    - Lapointe et al, 2004
    - Singh et al, 2002
  - Lung cancer
    - Garber et al, 2001
    - Bhattacharjee et al, 2001
  - DMD
    - Haslett et al, 2002
    - Pescatori et al, 2007

Datasets	DEG	POG
Prostate	Top 10	0.30
Cancer	Тор 50	0.14
	<b>Top100</b>	0.15
Lung	Тор 10	0.00
Cancer	Тор 50	0.20
	<b>Top100</b>	0.31
DMD	Тор 10	0.20
טועוט	Тор 50	0.42
	Top100	0.54

Zhang et al, *Bioinformatics*, 2009

#### MCI5004, 2017

# Contextualizing based on pathways may help



28



- Each disease phenotype has some underlying cause
- There is some unifying biological theme for genes that are truly associated with a disease subtype
- Uncertainty in selected genes can be reduced by considering biological processes of the genes
- The unifying biological theme is basis for inferring the underlying cause of disease subtype

### **ORA-Paired**



29

- Let g<sub>i</sub> be genes in a given pathway P
- Let p<sub>i</sub> be a patient
- Let q<sub>k</sub> be a normal

- Let  $\Delta_{i,j,k} = \text{Expr}(g_i,p_j) \text{Expr}(g_i,q_k)$
- H0: Pathway P is irrelevant to the diff betw patients and normals, so genes in P behave similarly in patients and normals
- $\Rightarrow$  t-test whether  $\Delta_{i,j,k}$  is a distribution with mean 0

Lim et al., JBCB, 13(4):1550018, 2015.

Copyright 2017 © Wong Limsoon

### What null distribution is appropriate?



30

- degrees of freedom
  t-distribution with n+m degrees of freedom
  - Generate null distribution by genelabel permutation

t-distribution with n\*m

 Generate null distribution by classlabel permutation

- ORA-Paired
- Let g<sub>i</sub> be genes in a given pathway P
- Let p<sub>j</sub> be a patient
- Let q<sub>k</sub> be a normal
- Let ∆<sub>i,j,k</sub> = Expr(g<sub>i</sub>,p<sub>j</sub>) -Expr(g<sub>i</sub>,q<sub>k</sub>)
- H0: Pathway P is irrelevant to the diff betw patients and normals, so genes in P behave similarly in patients and normals
- $\Rightarrow$  t-test whether  $\Delta_{i,j,k}$  is a distribution with mean 0

# and so, the genes in P behave similarly in patients and normals"

By the null hypothesis, a dataset and any of its class-label permutations are exchangeable

Testing the null hypothesis

- $\Rightarrow$  Get null distribution by class-label permutations
  - What happens when sample size is small?

Lim et al., JBCB, 13(4):1550018, 2015.





31

# SOMETIMES CHANGING PERSPECTIVE HELPS





### Almost all random signatures also have p-value < 0.05

 Instead of asking whether a signature is significant, ask what makes a signature (random or otherwise) significant



Venet et al., PLOS Comput Biol, 2011

Wilson Goh, private communication, 2017

- Proliferation is a hallmark of cancer
- Hypothesis: proliferationassociated genes make a signature significant







#### Copyright 2017 © Wong Limsoon

#### MCI5004, 2017





# **SUMMARY**

MCI5004, 2017

Copyright 2017 © Wong Limsoon

### Anna Karenina Principle



36

- Careless null / alternative hypothesis due to forgotten assumptions
  - Distributions of the feature of interest in the two samples are identical to the two populations
  - Features not of interest are equalized / controlled for in the two samples
  - No other explanation for significance of the test
  - Null distribution models the real world
- These make it easy to reject the carelessly stated null hypothesis and accept an incorrect alternative hypothesis

### Avoiding wrong conclusion, Getting deeper insight



37

- Check for sampling bias
  - Are the distributions of the feature of interest in the two samples same as that in the two populations?
- Check for exceptions
  - Are there large subpopulations for which the test outcome is opposite?
  - Are there large subpopulations for which the test outcome becomes much more significant?
- Check for validity of the null distribution
  - Can you derive it from the null hypothesis?